



# Local gyrokinetic turbulence simulations with realistic tokamak geometries towards ITER and JT-60SA

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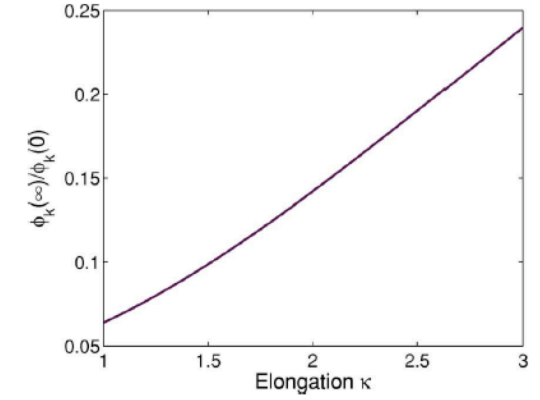
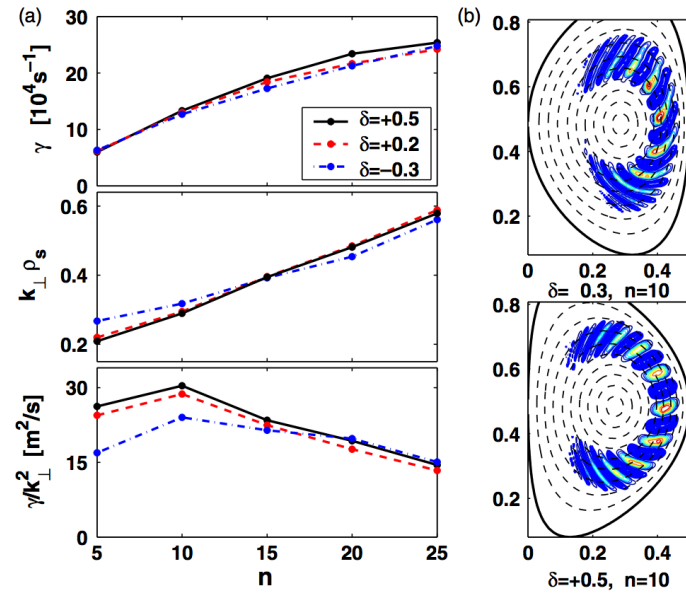
# Outline

- Introduction
- Current status of local gyrokinetic Vlasov code GKV
- Interface between MEUDAS(2D equilibrium solver) and GKV
- Application to realistic plasma shapes on JT-60SA
  - Linear ITG mode stability
  - Residual zonal flow levels
  - Nonlinear zonal flow generations
- Summary

# Introduction

- Turbulent transport properties can be strongly affected by the plasma shaping effects, through the change of the linear frequencies, mode-structures, and trapped/passing boundary.

Impact of the negative triangularity on stabilization of TEMs: global-GK analyses for TCV shape.  
Camenen et al., NF2007



Enhanced residual-ZF levels by plasma elongation: Analytic analyses for Solov'ev like equilibrium. Xiao and Catto, PoP2006

- Implementation of realistic shaped MHD-equilibrium to gyrokinetic code is useful for analyzing plasma shape effects, and for validation/prediction study against experiments.

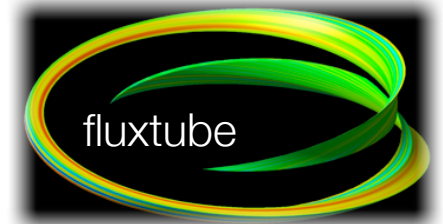
---> In this study, tokamak equilibria calculated by a free-boundary 2D Grad-Shafranov solver MEUDAS are incorporated into a local fluxtube gyrokinetic code GKV.

---> Micro-stability and zonal flow generation in several equilibria on JT-60SA are investigated.

# Current status of GKV code

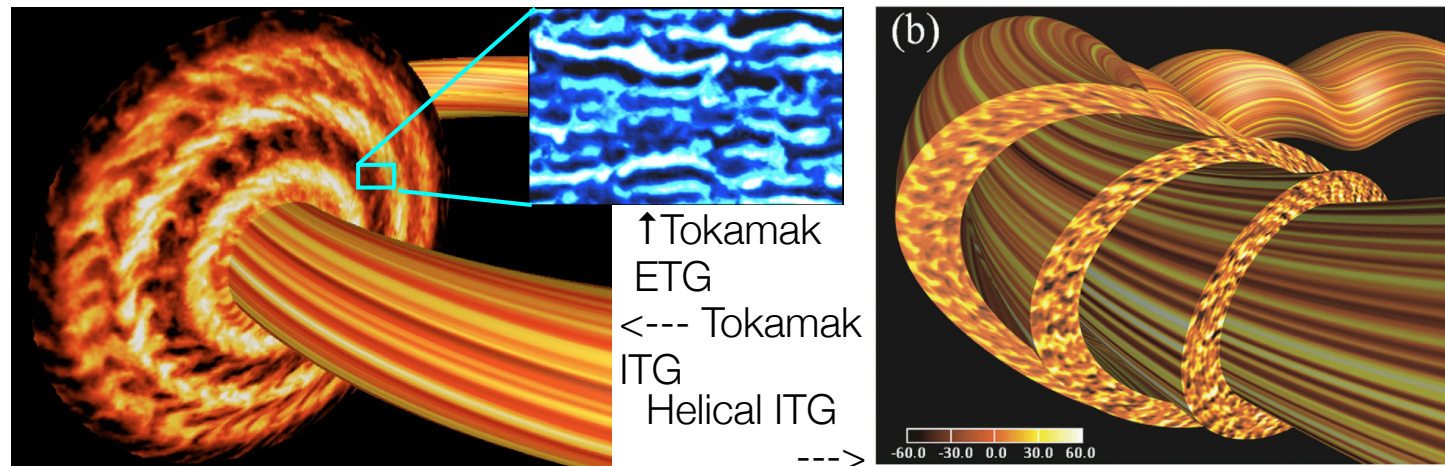
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- Local fluxtube 5D gyrokinetic solver, originally developed by [T. -H. Watanabe, NF2006]
  - > Solving the evolution of delta-f in 5D phase space
  - > Eulerian (or Vlasov) solver: spectral in 2D k-space, Finite-Difference in 3D ( $z, v_{||}, \mu$ )-space
  - > Electro-static, Electro-magnetic, Arbitrary numbers of species
  - > Helical geometries from VMEC, Tokamak geometries from MEUDAS(this talk)
  - > Entropy balance/transfer diagnostics



[T. -H. Watanabe PRL2008, M. Nunami PFR2011, M. Nakata PoP2012, S. Maeyama CPC2013]

- GKV code is now ready for turbulence simulations of burning plasmas composed of D, T, e, He-ash, C, W, etc.

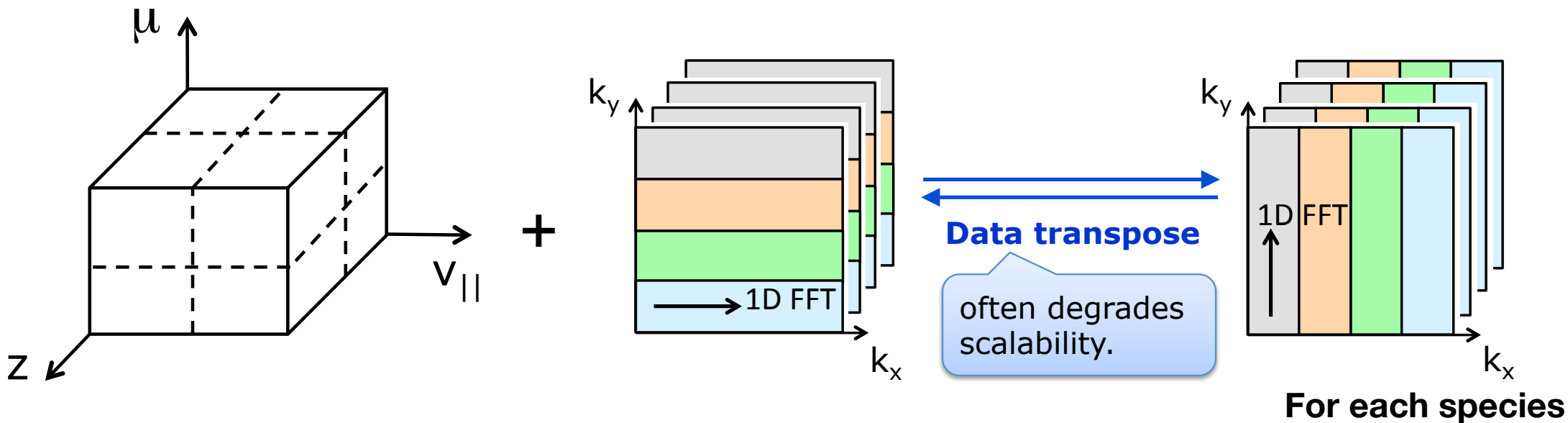


# Advanced parallelization towards PETA/EXA computing

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- 5D domain-decompositions with MPI and Thread parallelization with OPENMP

**Decomposition in  $(z, v_{||}, \mu)$  + Decomposition in k-space ( $k_x$  or  $k_y$ ) + Species**



- Parallel 2D FFT (including data-transpose) for the nonlinear ExB advection term is the most time-consuming.

---> **Segmented 3D rank-allocation technique (for MESH/TORUS network)**

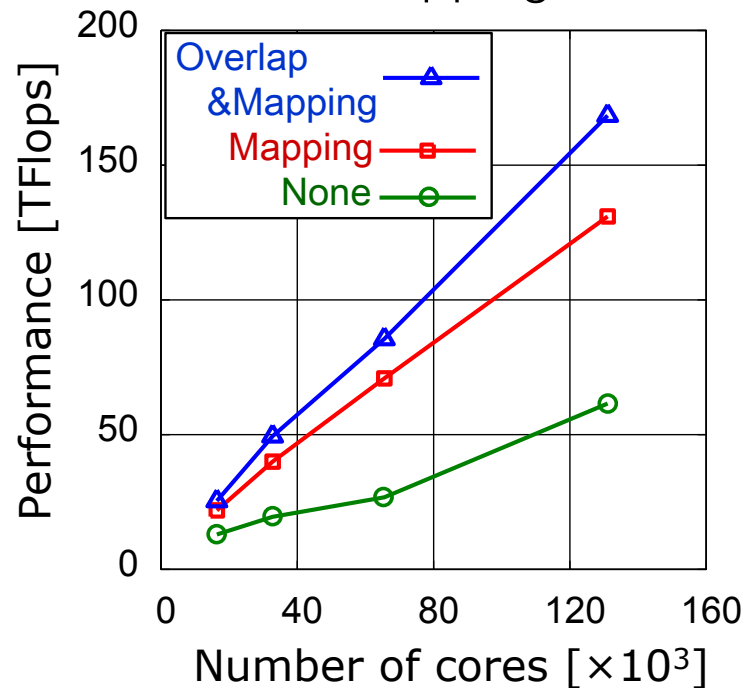
---> **Communication/Computation Overlap technique (for FFT and/or FD)**

# Fantastic scaling over 0.6M cores on K computer

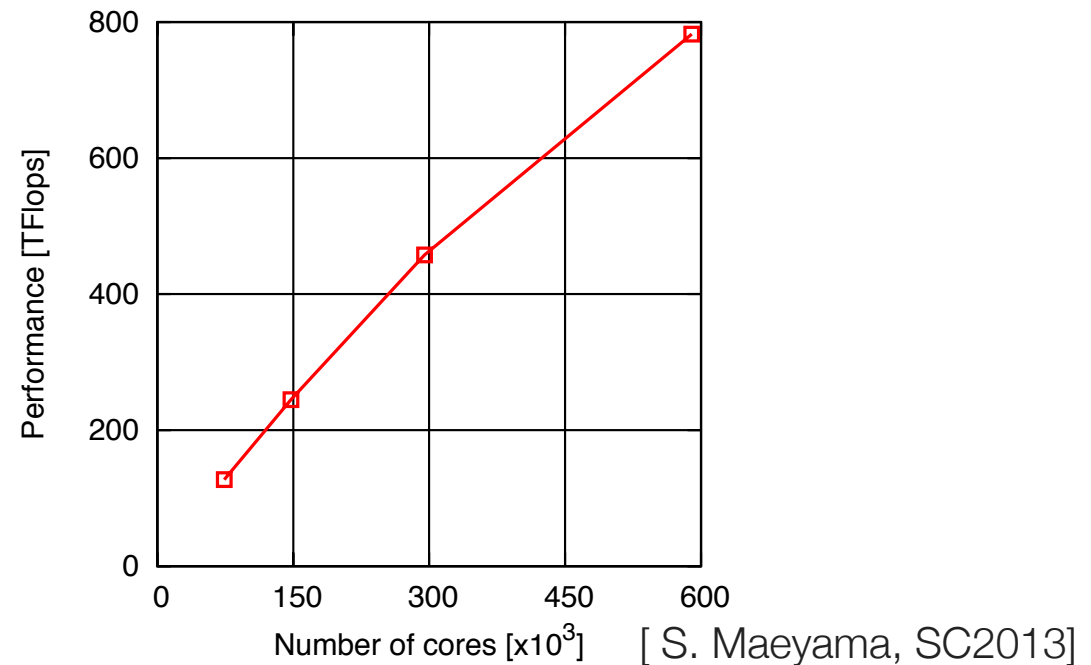
## Problem size for Multi-scale turbulence simulations (e.g. ITG-ETG)

$$\left( \begin{array}{l} N_x=1024, N_y=1024, N_z=128, N_v=64, N_\mu=32 \sim 274 \text{ billion grids} \\ P_k=8-64, P_z=16, P_v=8, P_\mu=4, 8 \text{ threads} > 600 \text{ thousand cores} \end{array} \right)$$

Effects of Rank-Mapping and Overlap



Strong scaling on K computer



**Fantastic scalability over 0.6Mcores has been achieved with 99.99994% efficiency.**  
**---> Multi-scale/Multi-species turbulence simulation is now accessible with GKV.**

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# Gyrokinetic equation in flux coordinates

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- Gyrokinetic and Poisson equations: electro-static limit, multi-species

$$\left\{ \begin{array}{l} \left[ \frac{\partial}{\partial t} + v_{\parallel} \mathbf{b} \cdot \nabla + i \mathbf{k}_{\perp} \cdot \mathbf{v}_{ds} - \frac{\mu}{m_s} \mathbf{b} \cdot \nabla B \frac{\partial}{\partial v_{\parallel}} \right] \delta f_{s \mathbf{k}_{\perp}} + \mathcal{N}(\delta f_{s \mathbf{k}_{\perp}}, \delta \psi_{s \mathbf{k}_{\perp}}) \\ = F_{Ms} \left[ i \mathbf{k}_{\perp} \cdot \mathbf{v}_{*Ts} - i \mathbf{k}_{\perp} \cdot \mathbf{v}_{ds} - v_{\parallel} \mathbf{b} \cdot \nabla \right] \frac{e_s \delta \psi_{s \mathbf{k}_{\perp}}}{T_s} + C_s(h_{s \mathbf{k}_{\perp}}) \\ k_{\perp}^2 \delta \phi_{\mathbf{k}_{\perp}} = 4\pi \sum_s e_s \left[ \int d\mathbf{v} J_{0s} \delta f_{s \mathbf{k}_{\perp}} - n_{s0} \frac{e_s \delta \phi_{\mathbf{k}_{\perp}}}{T_s} (1 - \Gamma_{0s}) \right] \end{array} \right.$$

- Fluxtube coordinates  $(x, y, z)$  defined by general SFL flux coordinates  $(\rho, \theta, \zeta)$ :

coordinates:  $x = c_x(\rho - \rho_0), y = c_y[q(\rho)\theta - \zeta], z = \theta$

$\Psi = \Psi(\rho)$  : poloidal flux

magnetic field:  $\mathbf{B} = c_b \nabla x \times \nabla y, c_b = \dot{\Psi} / c_x c_y$

$\Phi = \Phi(\rho)$  : toroidal flux

Jacobian:  $\sqrt{g}_{xyz} = (\nabla x \times \nabla y \cdot \nabla z)^{-1} = (c_x c_y)^{-1} \sqrt{g}_{\rho\theta\zeta}$

Derivatives:  $\frac{\partial}{\partial x} = \frac{1}{c_x} \frac{\partial}{\partial \rho} + \frac{\dot{q}(\rho)\theta}{c_x} \frac{\partial}{\partial \zeta}, \frac{\partial}{\partial y} = -\frac{1}{c_y} \frac{\partial}{\partial \zeta}, \frac{\partial}{\partial z} = \frac{\partial}{\partial \theta} + q(\rho) \frac{\partial}{\partial \zeta}$

safety factor and magnetic shear:  $q(\rho) = \frac{d\Phi}{d\Psi}, \hat{s}(\rho) = \frac{\rho}{q} \frac{dq}{d\rho}$



# Gyrokinetic equation in flux coordinates

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- Metric tensor

$$g^{xx} = \nabla x \cdot \nabla x = c_x^2 g^{\rho\rho}$$

$$g^{xy} = \nabla x \cdot \nabla y = c_x c_y [\dot{q}\theta g^{\rho\rho} + q g^{\rho\theta} - g^{\rho\zeta}]$$

$$g^{xz} = \nabla x \cdot \nabla z = c_x g^{\rho\theta}$$

$$g^{yy} = \nabla y \cdot \nabla y = c_y^2 [(\dot{q}\theta)^2 g^{\rho\rho} + q^2 g^{\theta\theta} + g^{\zeta\zeta} + 2q\dot{q}\theta g^{\rho\theta} - 2qg^{\theta\zeta} - 2\dot{q}\theta g^{\rho\zeta}]$$

$$g^{yz} = \nabla y \cdot \nabla z = c_y [\dot{q}\theta g^{\rho\theta} + q g^{\theta\theta} - g^{\theta\zeta}]$$

$$g^{zz} = \nabla z \cdot \nabla z = g^{\theta\theta}$$

- Advection operators in general forms for arbitrary flux coordinate systems:

$$\mathbf{b} \cdot \nabla = \frac{c_b}{B\sqrt{g_{xyz}}} \frac{\partial}{\partial z}, \quad k_{\perp}^2 = k_x^2 g^{xx} + 2k_x k_y g^{xy} + k_y^2 g^{yy}, \quad \frac{1}{L_{n_s}} = -\frac{d \ln n_s}{dx}, \quad \frac{1}{L_{T_s}} = -\frac{d \ln T_s}{dx}$$

$$\mathbf{k}_{\perp} \cdot \mathbf{v}_{ds} = \frac{m_s v_{\parallel}^2 + \mu B}{e_s c_b} [\mathcal{K}_x k_x + \mathcal{K}_y k_y], \quad \mathbf{k}_{\perp} \cdot \mathbf{v}_{*s} = -\frac{T_s}{e_s c_b} \left[ \frac{1}{L_{n_s}} + \frac{1}{L_{T_s}} \left( \frac{m_s v_{\parallel}^2}{2T_s} + \frac{\mu B}{T_s} - \frac{3}{2} \right) \right] k_y$$

$$\mathcal{K}_x = \frac{g^{xz} g^{xy} - g^{xx} g^{xz}}{B^2/c_b^2} \frac{\partial \ln B}{\partial z} - \frac{\partial \ln B}{\partial y}, \quad \mathcal{K}_y = \frac{g^{xz} g^{yy} - g^{xy} g^{yz}}{B^2/c_b^2} \frac{\partial \ln B}{\partial z} + \frac{\partial \ln B}{\partial x}$$

---> Only B-intensity, and its derivatives, and the contra-variant metric components are necessary to calculate these operators.

# Construction of SFL flux coordinates from MEUDAS

Data flow

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MEUDAS (developed in JAEA)

2D Free-boundary Grad-Shafranov solver

$$P = P(\Psi), \quad I = I(\Psi)$$

IGS [Matsuyama]

$$\Psi = \Psi(R, Z)$$

Flux coordinate Interface

Interpolation, tracing flux surfaces

Constructing Axisymmetric, Hamada, and Boozer coordinates

The radial label :

$$\rho = \sqrt{\Phi/\Phi_{\text{edge}}}, \quad \rho = \sqrt{\Psi/\Psi_{\text{edge}}}$$

The minor radius :

$$a = \sqrt{V_{\text{edge}}/2\pi^2 R_{\text{ax}}}, \quad a = \sqrt{2\Phi_{\text{edge}}/B_{\text{ax}}},$$

$$a = \sqrt{2\Psi_{\text{edge}}/B_{\text{ax}}}$$

GKV

Local fluxtube code

Calculating metric components and advection operators

Turbulence simulation

$$R = R[\rho, \theta], \quad Z = Z[\rho, \theta], \quad \phi = \zeta - q(\rho)G[\rho, \theta]$$

$$B = B[\rho, \theta], \quad dB/d\rho, \quad dB/d\theta$$

Co-variant metric components are calculated by

$$g_{ij} = \frac{\partial R}{\partial u_i} \frac{\partial R}{\partial u_j} + \frac{\partial Z}{\partial u_i} \frac{\partial Z}{\partial u_j} + R^2 \frac{\partial \phi}{\partial u_i} \frac{\partial \phi}{\partial u_j}$$

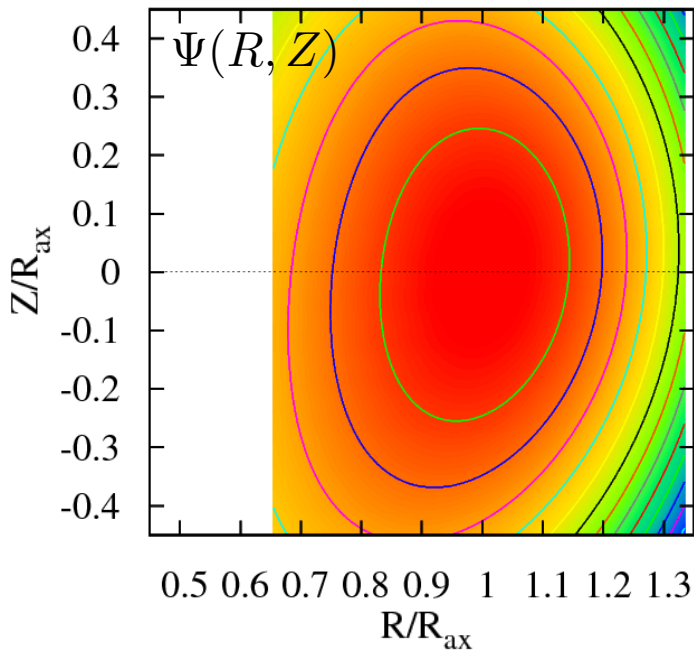
$$u_i = \{\rho, \theta, \zeta\}$$

, then converted to contra-variant components.

# Verification of flux coordinates with solovev equilibrium

- Analytic expression of solovev equilibrium with finite elongation, triangularity, and up-down asymmetry:

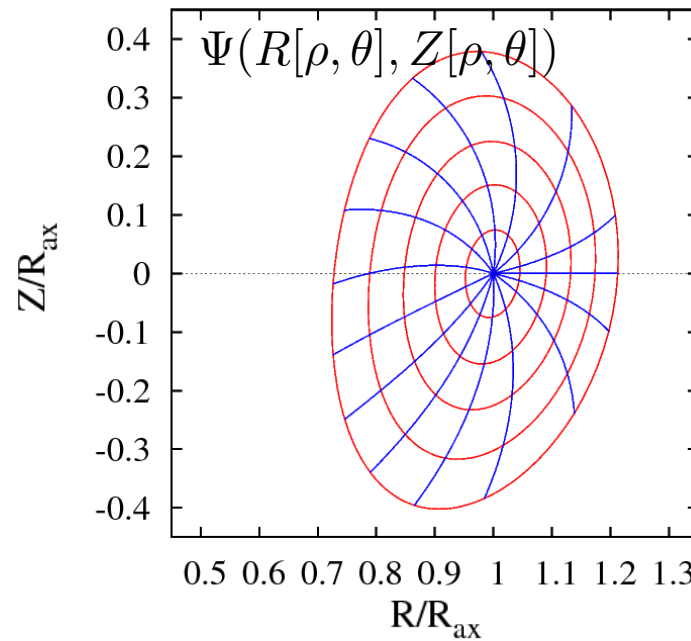
$$\frac{\Psi(\bar{R}, \bar{Z})}{\Psi_{\text{edge}}} = \frac{1}{\epsilon_a^2} \left[ \frac{(1-d)\bar{R}^2\bar{Z}^2 + d\bar{Z}^2}{E^2} + \frac{1}{4}(\bar{R}^2 - 1)^2 \right] + \frac{\nu_{\text{asym}}}{\epsilon_a} (\bar{R}^2 - 1)\bar{Z}, \quad \bar{R} = R/R_{\text{ax}}, \bar{Z} = Z/R_{\text{ax}}$$



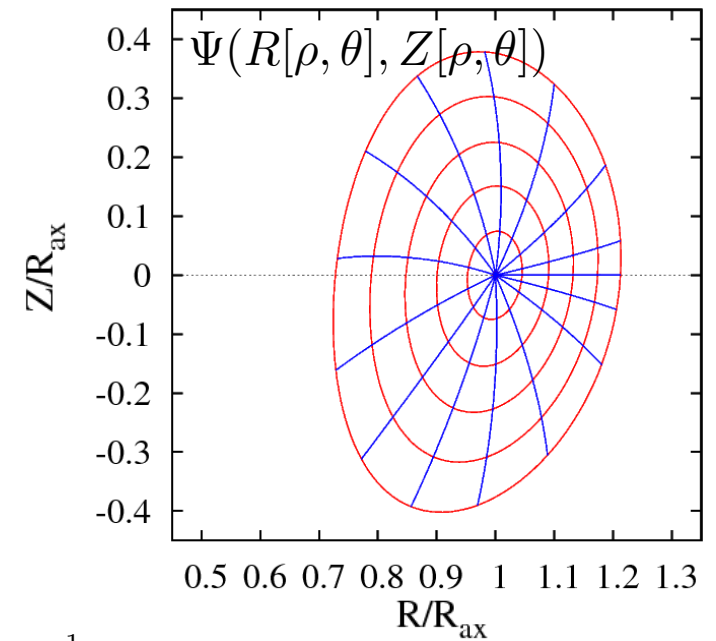
Original 2D equilibrium data with

$$E = 1.6, d = 0.05,$$

$$\epsilon_a = 0.25, \nu_{\text{asym}} = -0.3$$



Boozer coord. with  $\rho = (\Psi/\Psi_{\text{edge}})^{\frac{1}{2}}$



Hamada coord.

Less deformation of constant  $\theta$ -surface near the edge for Hamada coord. (especially, out-board side)

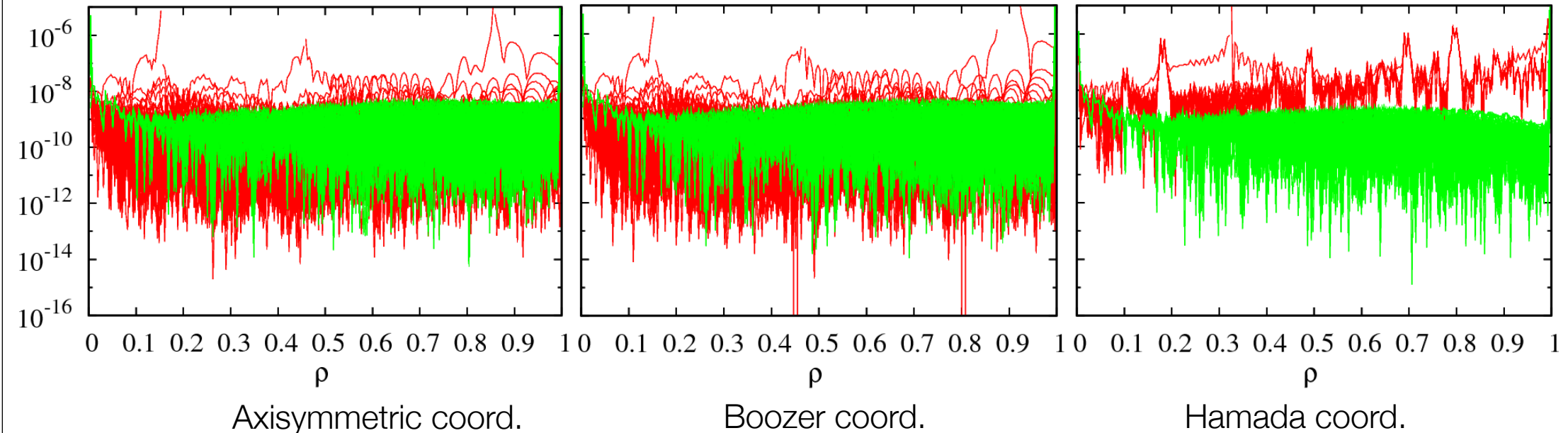
# Verification of flux coordinates with solovev equilibrium

- Consistency is verified by the following analytical expressions:

$$\frac{\partial R[\rho, \theta]}{\partial \theta} = -\frac{\sqrt{g}}{R} \frac{\partial \rho(R, Z)}{\partial Z}$$

$$g^{\rho\rho} = \left\| \frac{\partial \rho}{\partial R} \nabla R + \frac{\partial \rho}{\partial Z} \nabla Z \right\|^2$$

Relative error to analytical expressions



All the constructed coordinate systems show sufficient accuracy (up to  $\sim 10^{-8}$ ) for turbulent transport analyses.

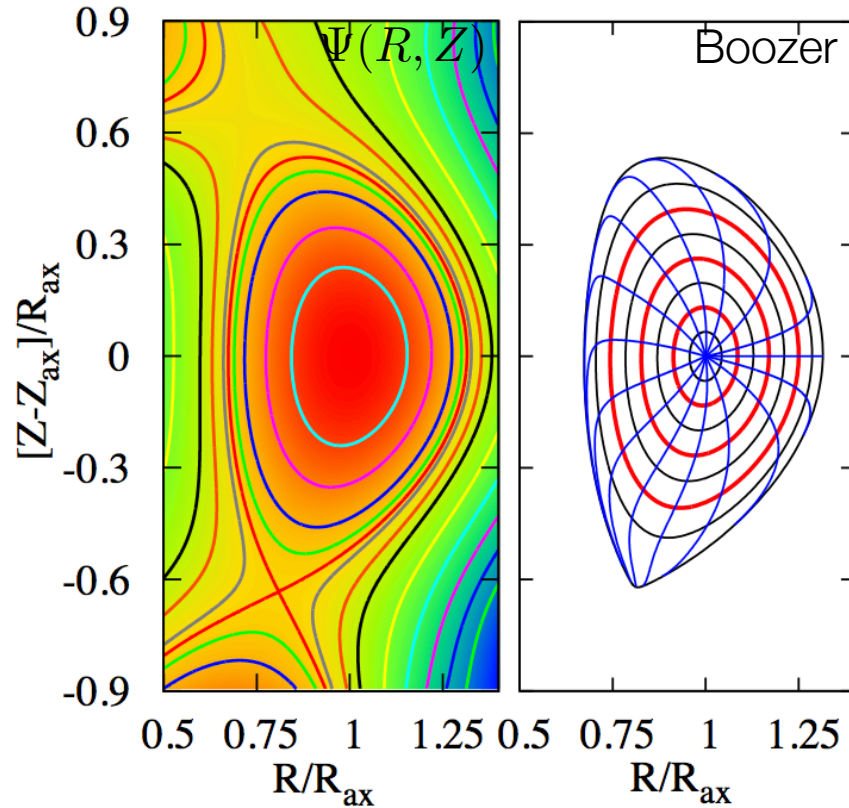
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# Application to realistic plasmas on JT-60SA

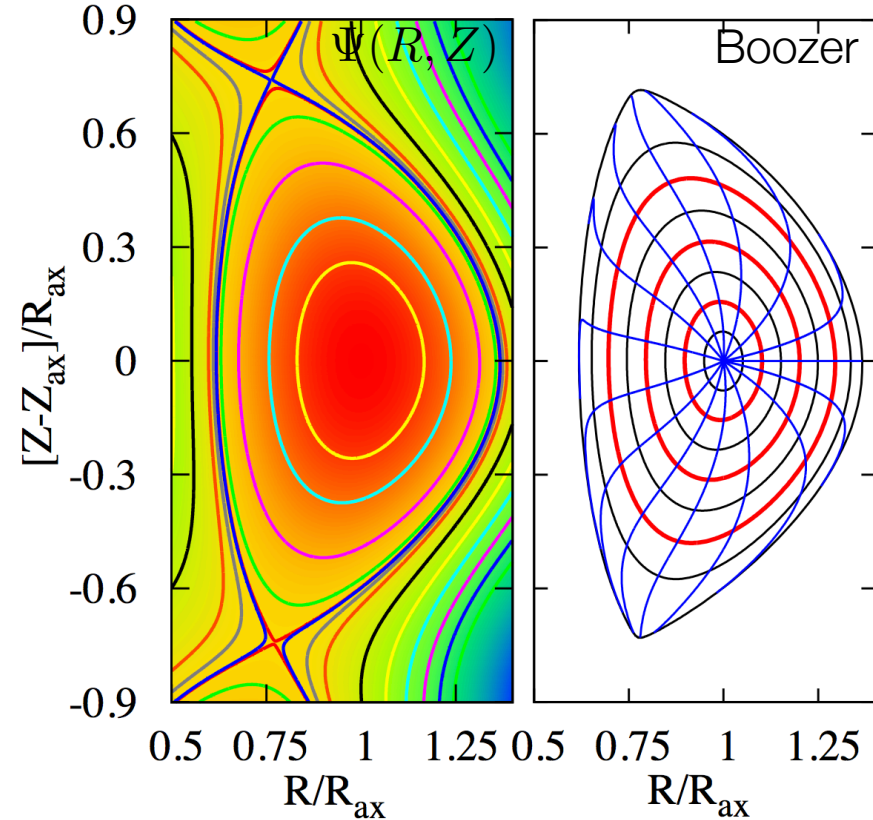
- Two L-mode plasmas are considered (The MHD stability has been well investigated: N. Aiba PFR2007 ):

ITER-like plasma with single null: “IT”



$$\begin{aligned} R_{ax} &= 3.02\text{m}, \quad a = 1.29\text{m}, \quad V = 90.7\text{m}^3, \\ B_{ax} &= 2.64\text{T}, \quad q_{ax} = 1.82, \quad q_{95} = 3.88, \\ I_p &= 2.59\text{MA}, \quad S = q_{95}I_p/B_{ax}a = 2.95 \end{aligned}$$

Highly-Shaped plasma with quasi double null: “HS”

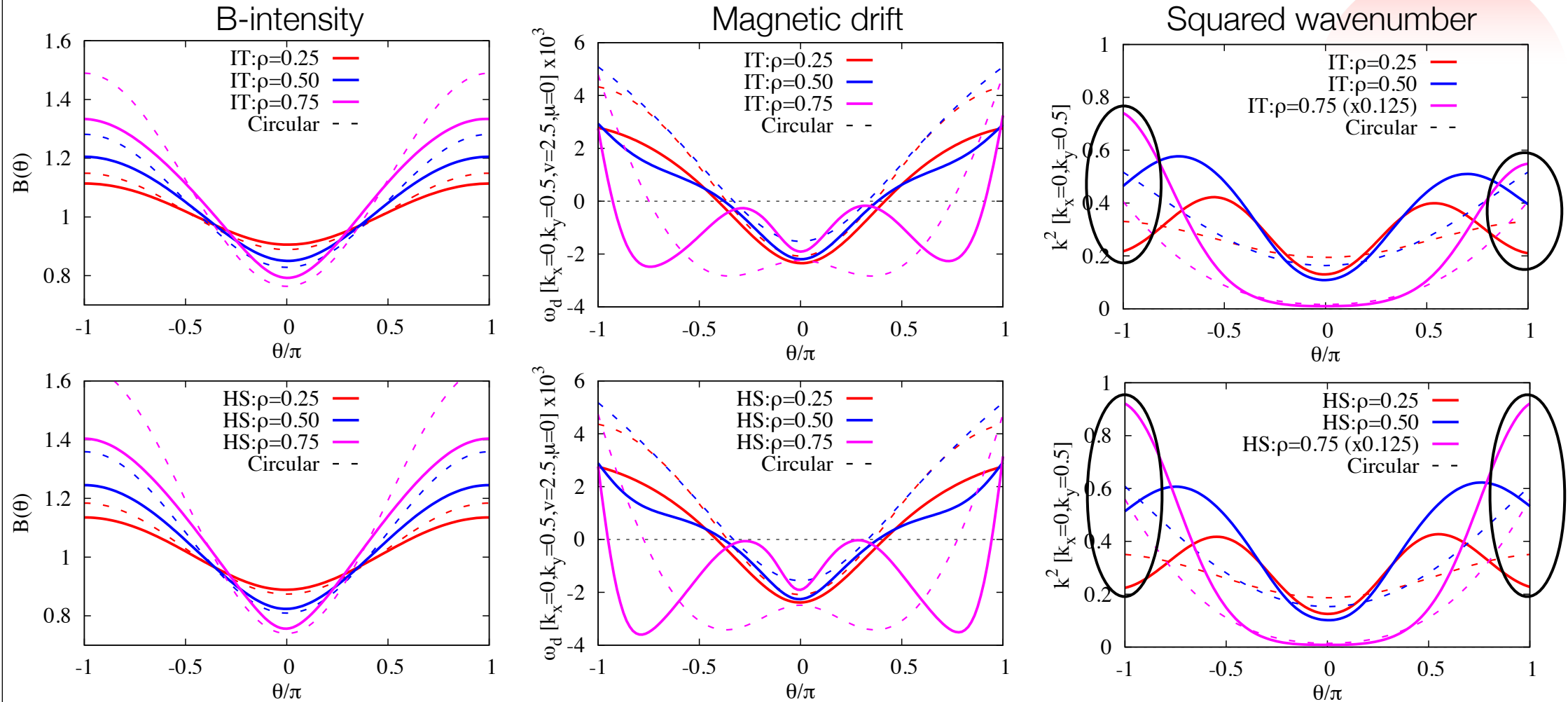


$$\begin{aligned} R_{ax} &= 3.05\text{m}, \quad a = 1.53\text{m}, \quad V = 129.5\text{m}^3, \\ B_{ax} &= 2.88\text{T}, \quad q_{ax} = 1.41, \quad q_{95} = 3.59, \\ I_p &= 5.00\text{MA}, \quad S = q_{95}I_p/B_{ax}a = 4.07 \end{aligned}$$

# Field aligned structures of $B$ -intensity, $\omega_d$ , and $k^2$

IT: ITER-like, HS: Highly shaped

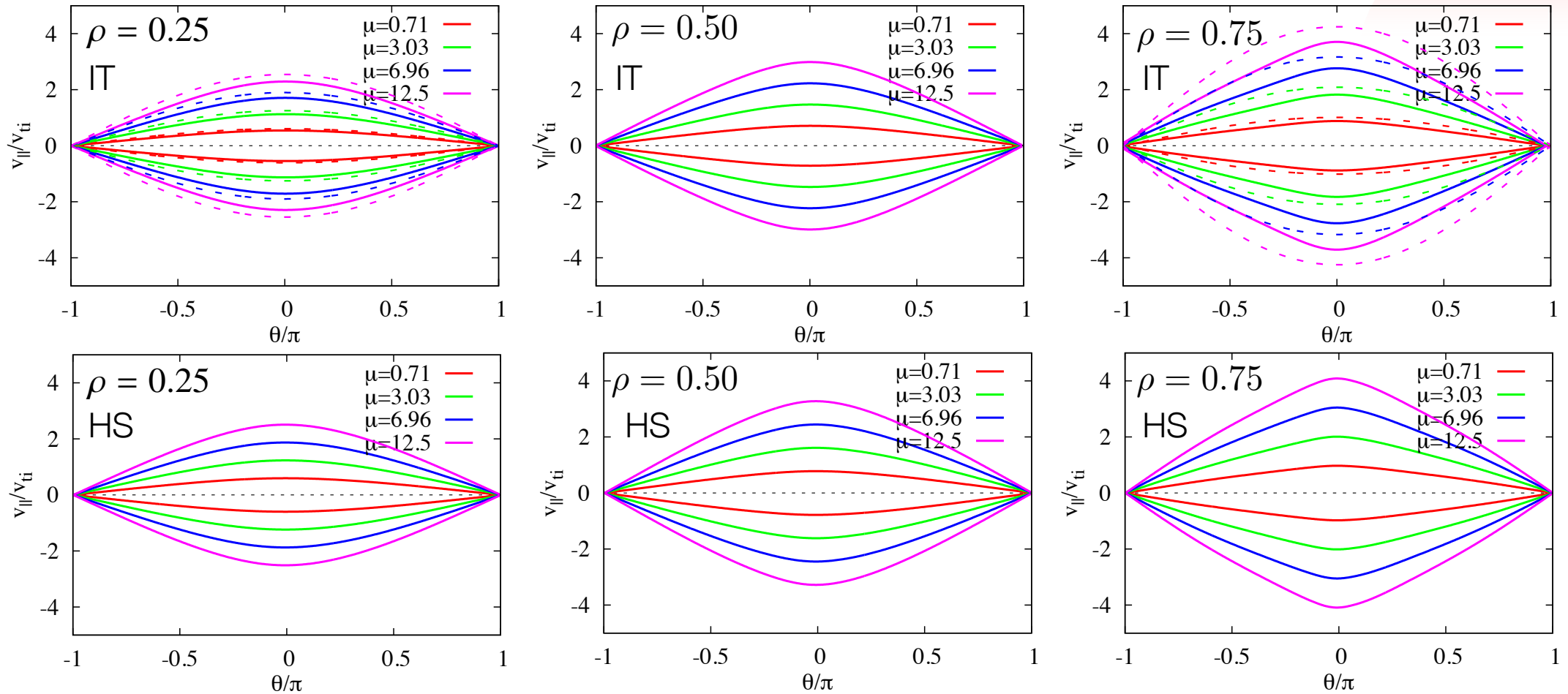
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- Field aligned structures in shaped plasmas deviate from those in circular plasmas (outer sides).
- Stronger asymmetry in  $k^2$  for ITER-like plasma than that in Highly-Shaped plasma.

# Trapped/Passing boundaries

IT: ITER-like, HS: Highly shaped

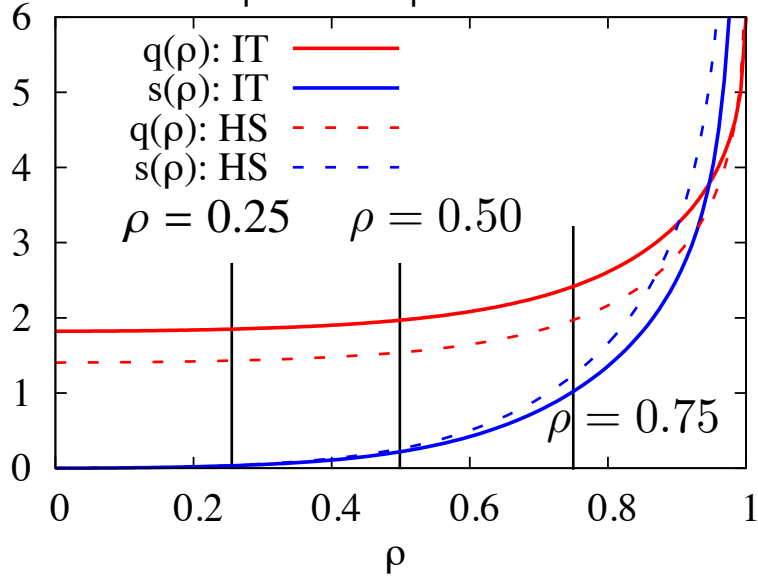


- More sharp boundary, but less trapped region for shaped plasmas compared with circular ones.
- > Strong impacts on ITG with kinetic elec. and TEM turbulence dynamics.

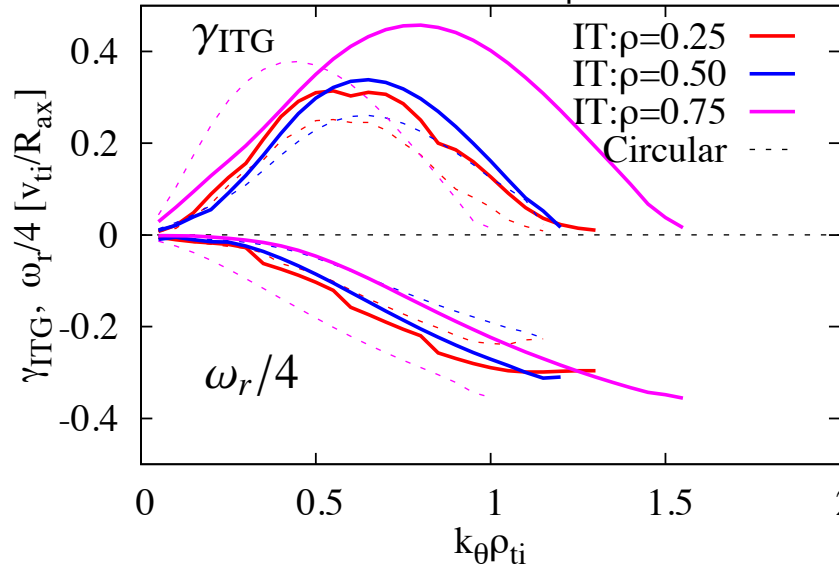


# Linear ITG mode stability for the ITER-like plasma

q- and s-profiles

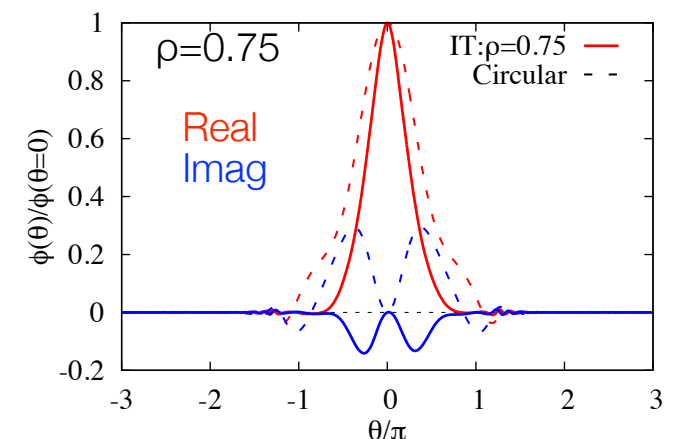
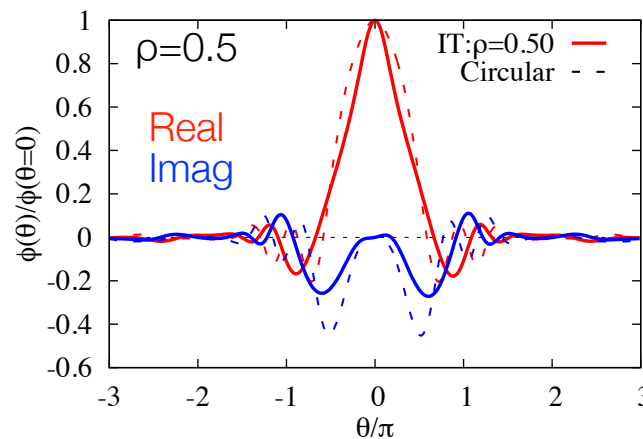
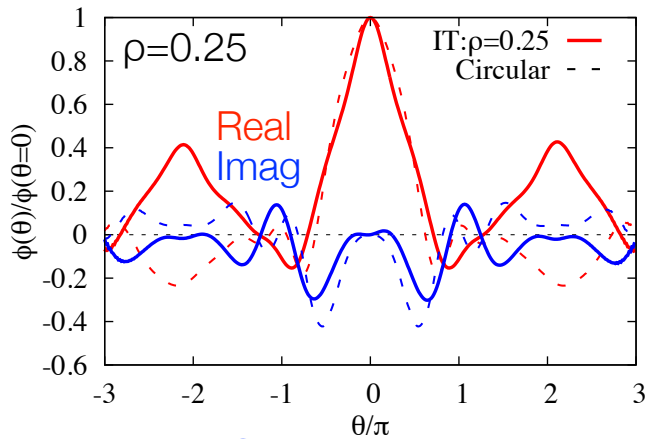


ITG-ae mode spectra



IT	0.25	0.50	0.75
$r/R_{ax}$	0.104	0.214	0.322
$q$	1.85	1.97	2.43
$s$	0.03	0.23	1.06

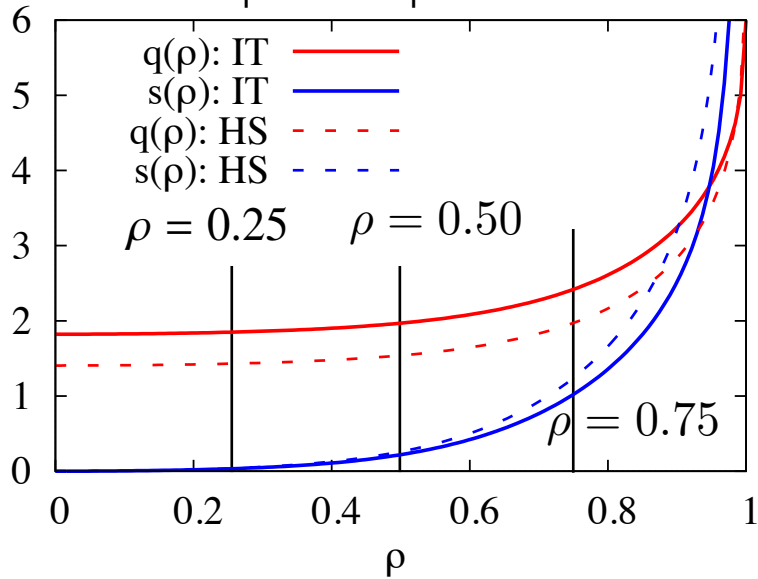
$R_{ax}/L_n = 3.0$ ,  $R_{ax}/L_T = 6.0$ ,  
 $T_e/T_i = 1$ ,  $k_{y(\min)} = 0.05$



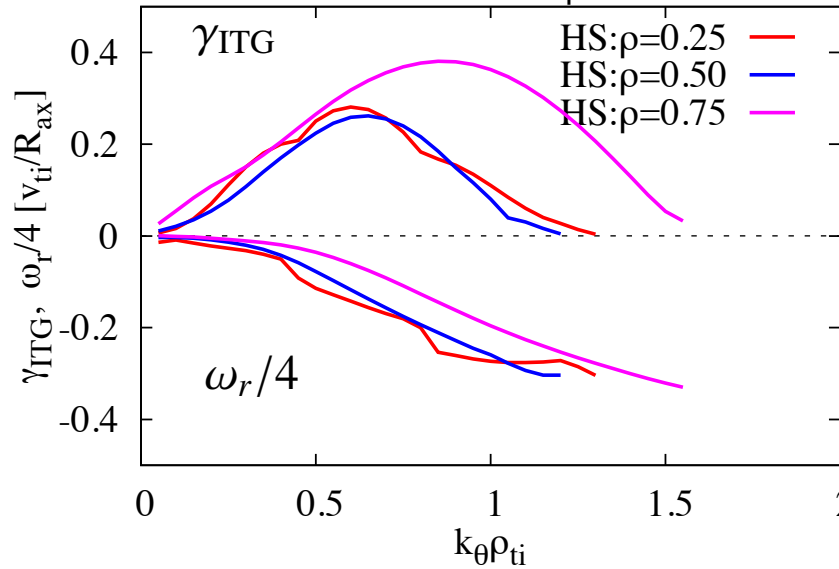
- Broader ITG-spectra with more localized eigenmode appear especially in strongly shaped region (outer side).

# Linear ITG mode stability for the Highly-Shaped plasma

q- and s-profiles

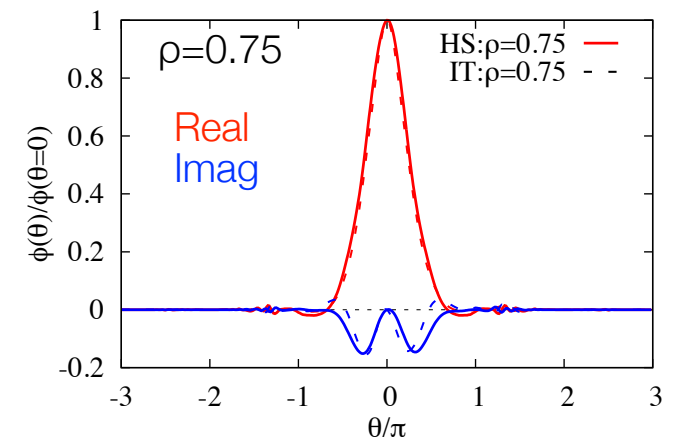
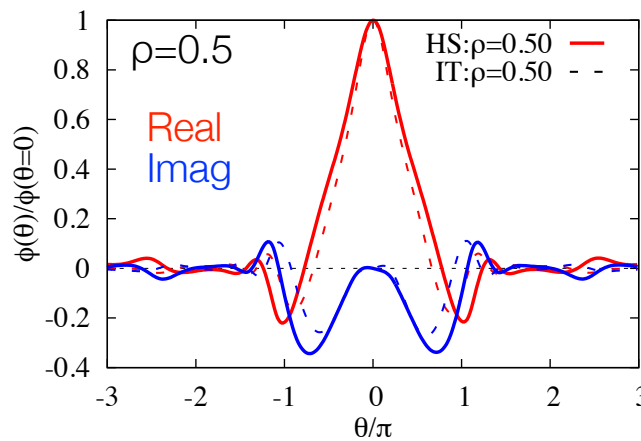
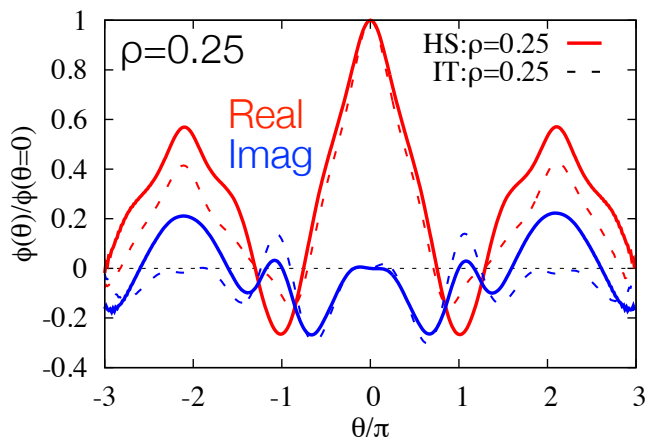


ITG-ae mode spectra



HS	0.25	0.50	0.75
$r/R_{ax}$	0.123	0.250	0.38
q	1.43	1.54	1.97
s	0.03	0.35	1.23

$R_{ax}/L_n = 3.0$ ,  $R_{ax}/L_T = 6.0$ ,  
 $T_e/T_i = 1$ ,  $k_{y(\min)} = 0.05$

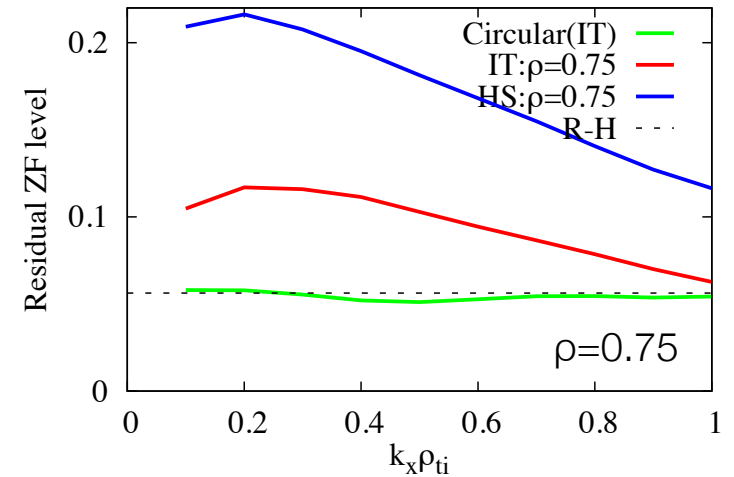
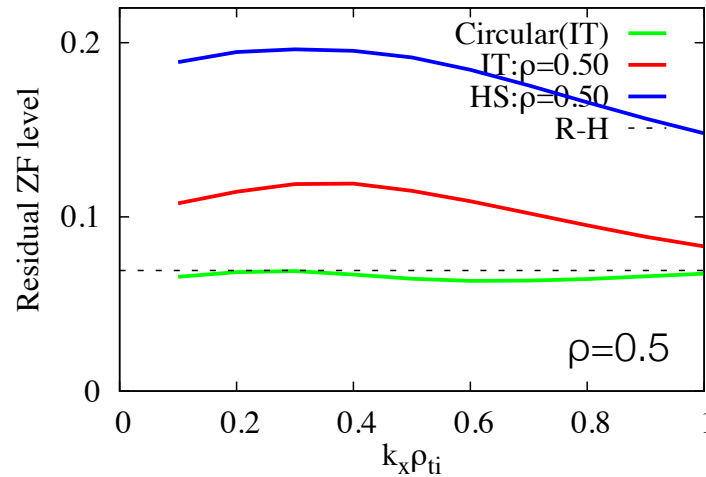
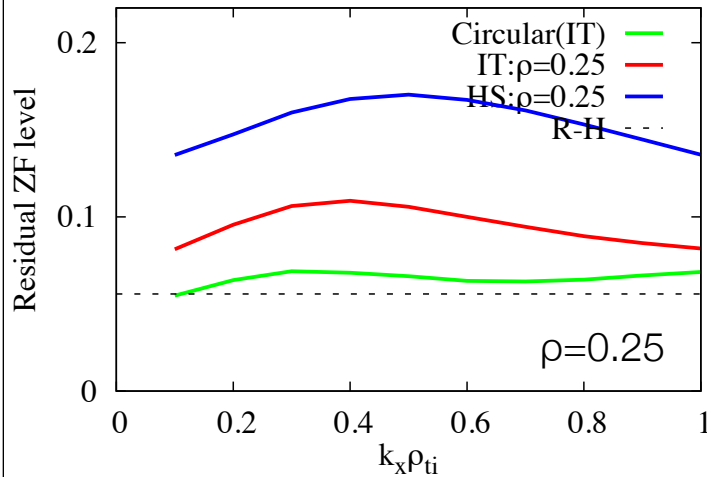
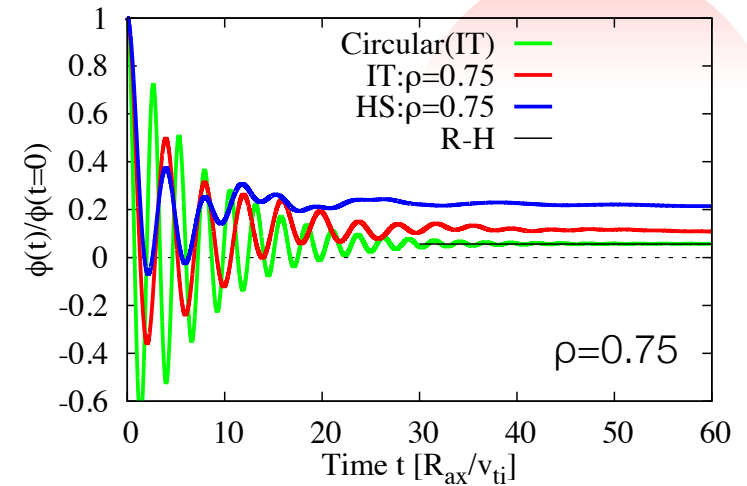
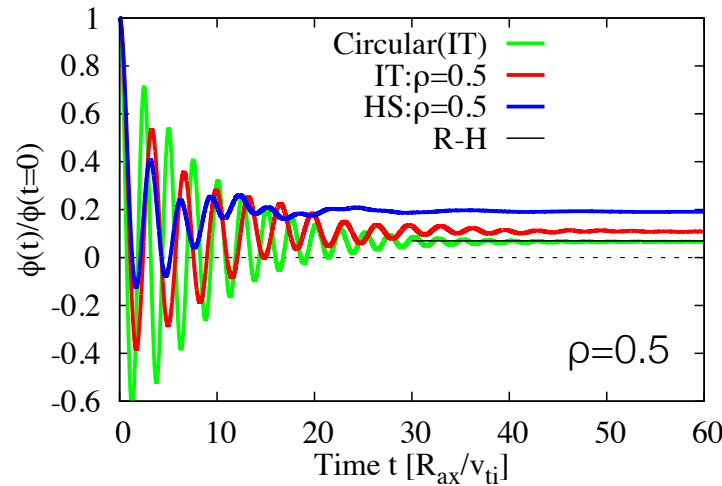
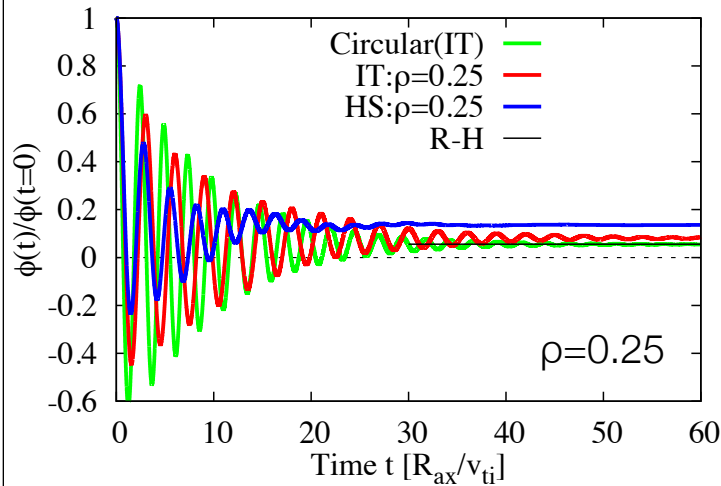


- ITG mode growth rates in Highly-shaped case is slightly lower than those in the ITER-like cases.

# Geometric dependence of residual zonal flow levels

IT: ITER-like, HS: Highly shaped

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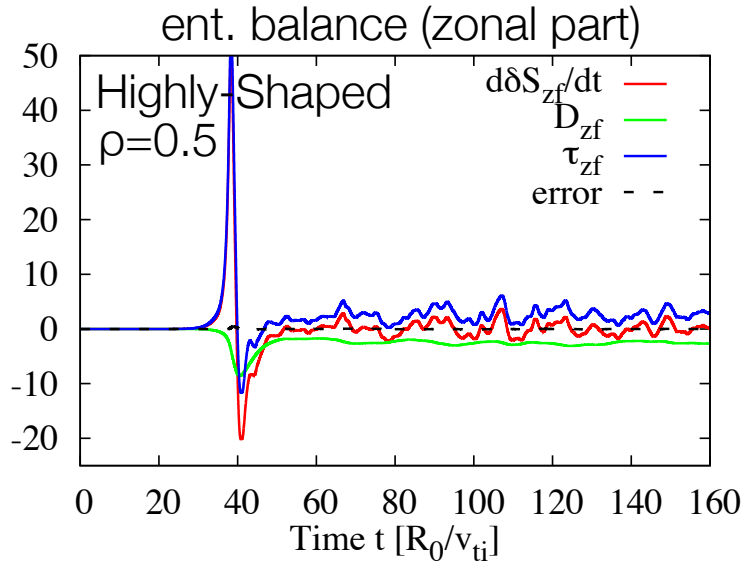
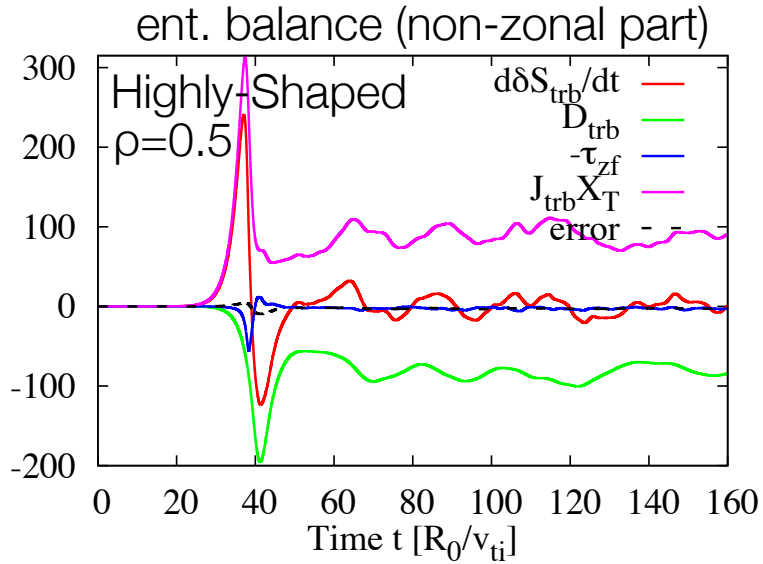
- Shaping effects in IT- and HS- plasmas lead to
  - > significant enhancement of residual zonal flow levels
  - > stronger  $k_x$ - (or  $k_r$ -) dependence compared with circular plasmas.

HS is expected to be more favorable to ITG-stability and ZF-response!

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# Nonlinear simulation and entropy balance



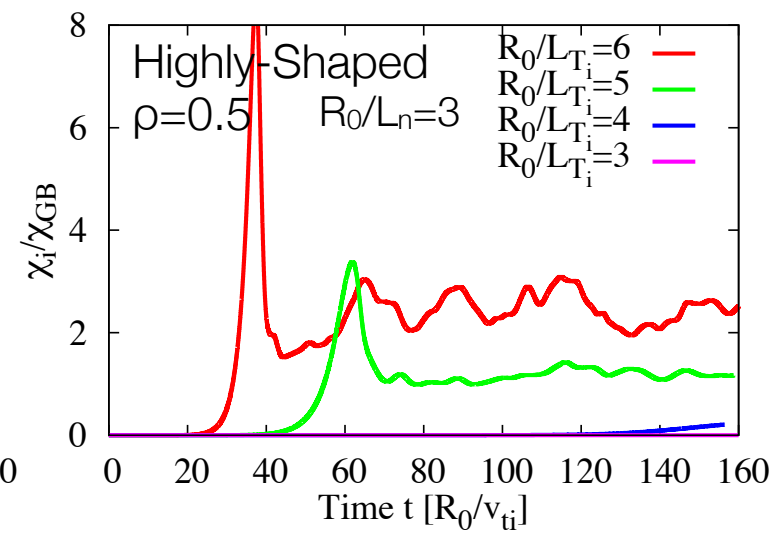
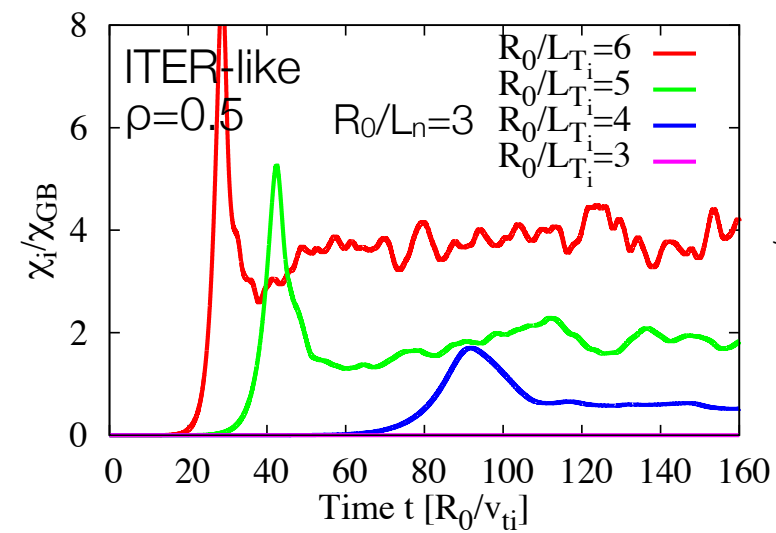
entropy variable

$$\frac{d\delta S_{trb}}{dt} = \underbrace{J_{trb} X_T}_{\text{(flux) x (thermo. force)}} - \tau_{zf} + \underbrace{D_{trb}}_{\text{col. dissipation}}$$

$$\frac{d\delta S_{zf}}{dt} = \underbrace{\tau_{zf}}_{\text{transfer from NZ to Z}} + D_{zf}$$

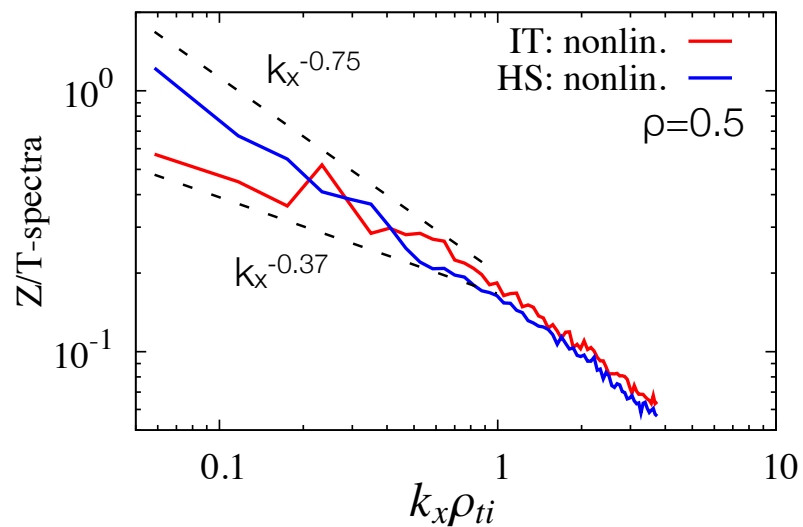
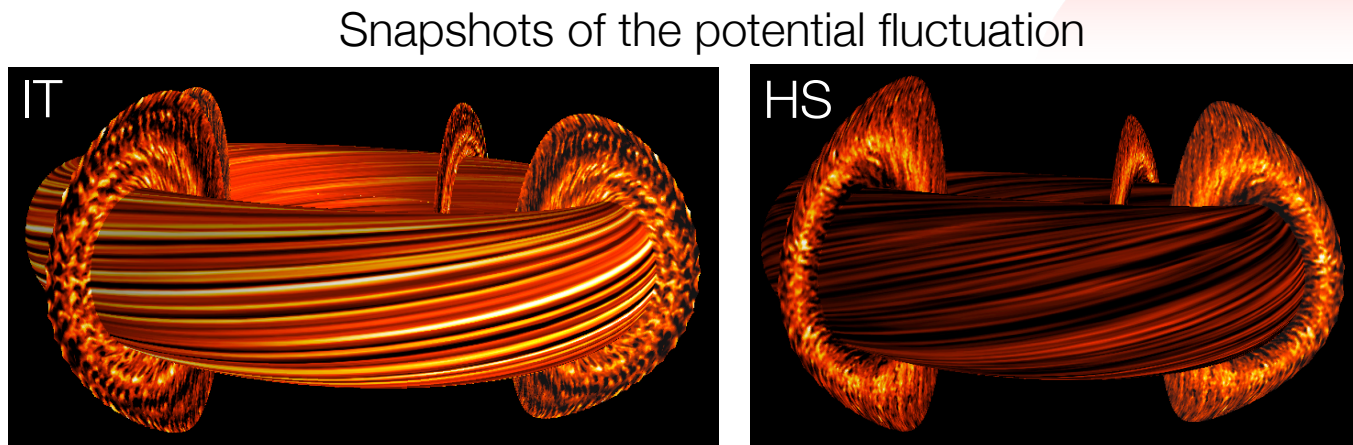
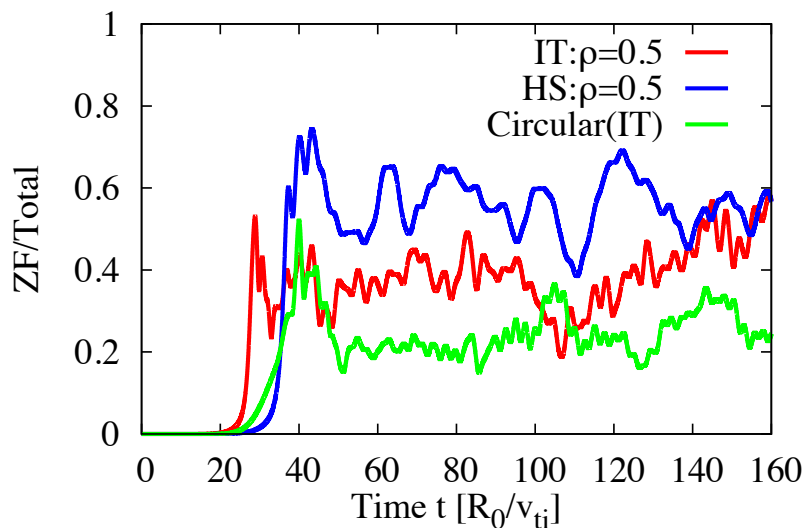
- The entropy balance relations are well satisfied both in the non-zonal and zonal parts.

- Highly-Shaped cases show lower transport levels with higher critical temperature gradient.



# Nonlinear zonal flow generation

IT: ITER-like, HS: Highly shaped



- As is expected by linear ZF-damping analyses, more efficient ZF generation is observed in the nonlinear phase of the Highly-Shaped case.

- Stronger  $k_x$ -dependence of Z/T is also identified in the Highly-Shaped case. (Z: ZF-intensity, T: turbulence intensity)

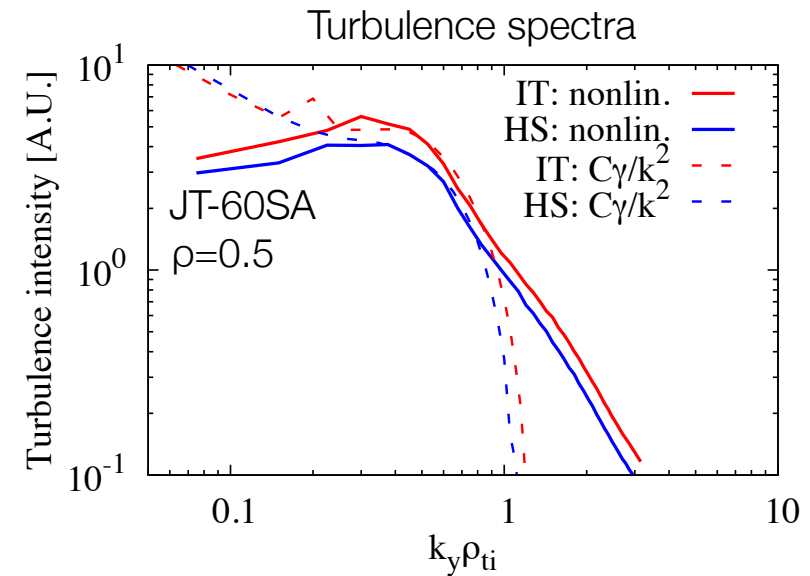
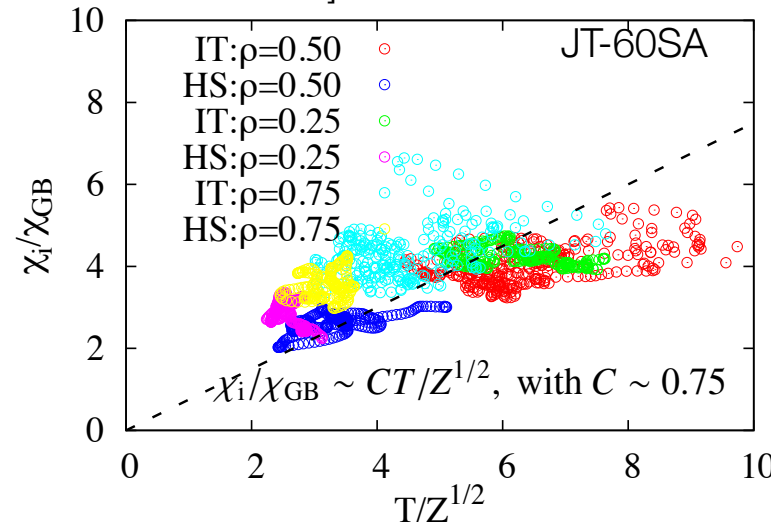
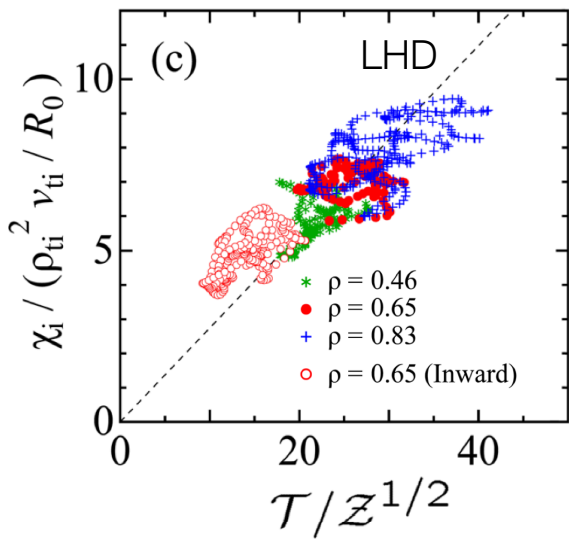
---> Qualitative features on the amplitude and  $k_x$ -dependence are well agreed with linear results shown in the previous slides.

# Towards the transport modeling

- ITG turbulence simulations on LHD show that the ion heat diffusivity well scales with  $T/Z^{1/2}$ , and GK-simulation-based transport model including zonal-flow effects has been developed.

[M. Nunami PoP2012, 2013]

Scaling on LHD [M. Nunami PoP2012] and JT-60SA



- Good scaling between  $\chi_i$  and  $T/Z^{1/2}$  is also observed in JT-60SA case.
- Turbulence spectra near the peak region are well characterized with linear spectra,  $\gamma_{ITG}/k_y^2$ .
- > Promising to construct the similar reduced transport model produced by the linear spectra and residual ZF levels. (currently underway...)

# Summary

- An interface code to generate flux coordinates system from realistic plasma equilibria calculated by free-boundary 2D Grad-Shafranov solver MEUDAS is successfully implemented to a local fluxtube code GKV.
- The accuracy of the flux coordinates, i.e., Axisymmetric, Boozer, and Hamada, are verified with an analytical solovev equilibrium model.
- Linear ITG-ae stability (ae: adiabatic electrons) is investigated for two types of shaped plasmas in JT-60SA, i.e., ITER-like plasma(IT) and Highly shaped one(HS), then the difference from the concentric circular equilibrium, which is conventionally used in gyrokinetic code, has been clarified.
  - > Highly-shaped configuration shows less ITG-driven transport than that in the standard ITER-like configuration, due to stronger generation of zonal flows.
  - > The turbulent ion heat diffusivity well scales with  $T/Z^{1/2}$ , which suggests the applicability of a GK-simulation based transport model.

More detailed analyses including a multi-species/scales stability analysis, nonlinear simulations, and constructing the GK-based transport model are in progress.