

# Relation between poloidal ion flow and magnetism of toroidal field in multi-pulsing CHI driven ST

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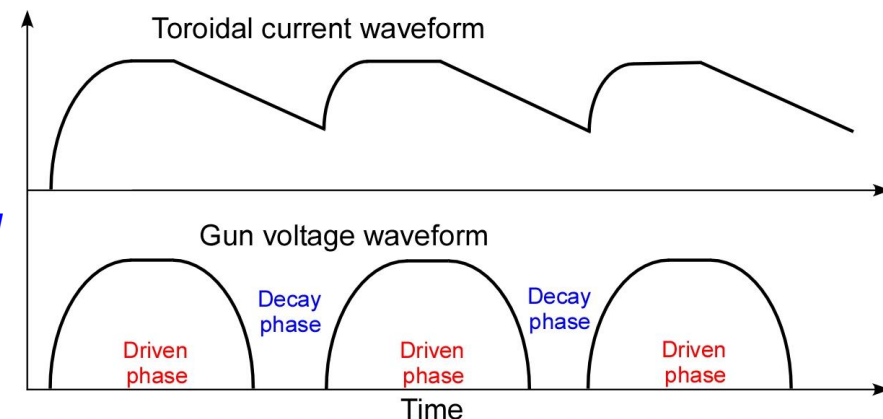
## Outline:

- 1) Introduction: Background and purpose
- 2) Double-pulsing CHI experiment on HIST:  
Radial profile (flow velocity, number density, and radial electric field)
- 3) Axisymmetric two-fluid equilibrium equations
- 4) Numerical results: Relation between poloidal ion flow velocity and toroidal field
- 5) Summary

# Introduction



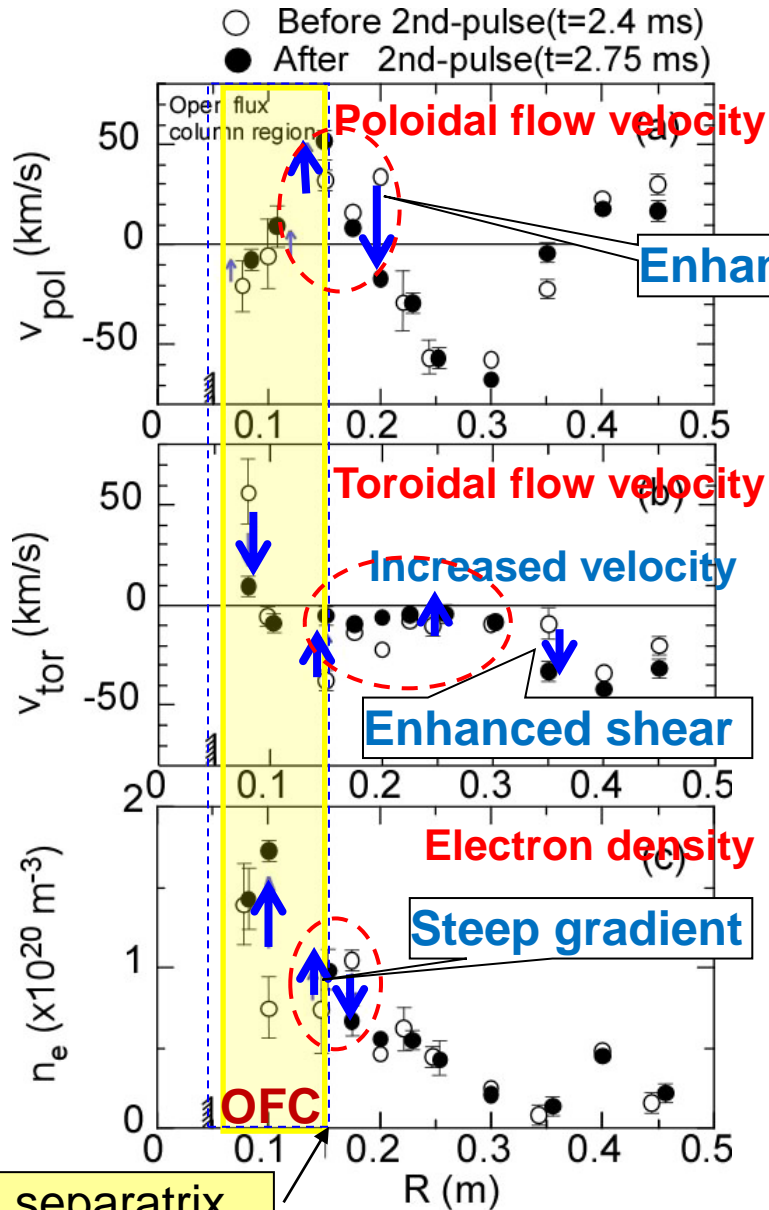
- Coaxial helicity injection (CHI): **Non-inductive CHI** and inductive CHI  
Non-inductive CHI has been used as plasma start-up (Transient CHI) and **quasi-steady state current drive (Driven CHI)** in a spherical torus (ST)
  - ➔ In the driven phase, the fluctuations deteriorate the confinement.
  - ➔ In the decay phase, the closed flux surfaces are formed, resulting in the good confinement.
- **Multi-pulsing CHI (M-CHI)**: after the plasma current partially decays, a new CHI pulse is applied and the cycle process is repeated.
  - ➔ To achieve a **quasi-steady sustainment and good confinement**
- Double-pulsing CHI experiment in the HIST device
  - ✓ **Observation around the Central open flux column (OFC) region**
    - Steep density gradient (width of OFC  $w_{\text{OFC}} \sim 7\text{cm}$ , ion skin depth  $\ell_i \sim 3\text{cm}$ )
    - Poloidal shear flow and the radial electric field shear
    - *Diamagnetic toroidal field*
    - *Two-fluid effect is important.*
  - ✓ **Two-fluid flowing equilibrium**  
*Relation between poloidal ion flow and toroidal field caused by applying the CHI pulse again*



[1] S. Woodruff, et al., PRL **90**, 205002-1 (2004).

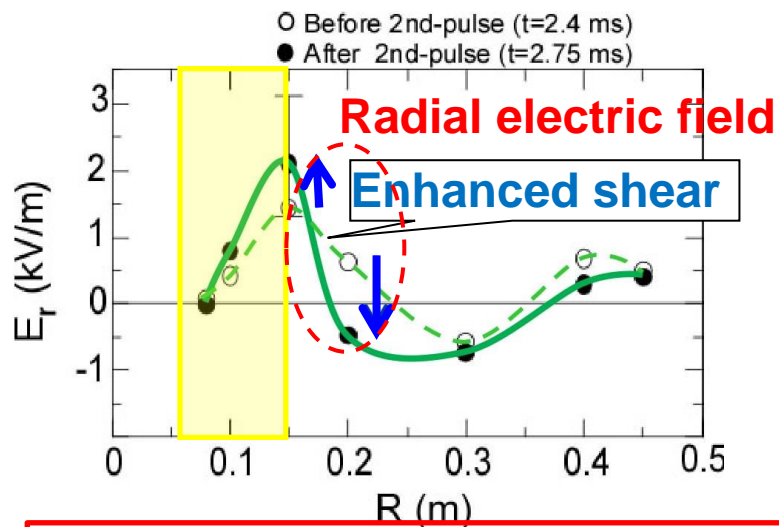
[2] E.B. Hooper, PPCF **53**, 085008 (2011).

# Radial profiles in double-pulsing CHI experiment on HIST

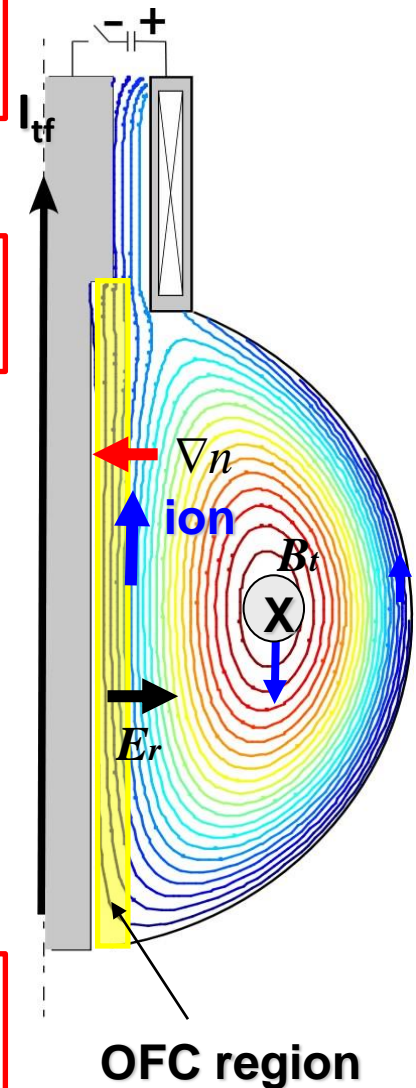


The poloidal flow velocity is increased around the separatrix, and its shear is enhanced there.

The toroidal flow velocity is increased in the closed flux region.



The density gradient and the radial electric field shear is enhanced around the separatrix.



# Normalized non-dissipative two-fluid equations in a steady state



Equation of ion motion  $\mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p_i / n + \mathbf{E} + (1/\varepsilon) \mathbf{u} \times \mathbf{B}$

Equation of electron motion  $0 = -\nabla p_e / n - \mathbf{E} - (1/\varepsilon) \mathbf{u}_e \times \mathbf{B}$

Equations of continuity  $\nabla \cdot (n\mathbf{u}) = 0 \quad \nabla \cdot (n\mathbf{u}_e) = 0$

Entropy conservation  $\mathbf{u} \cdot \nabla s_i = 0 \quad \mathbf{u}_e \cdot \nabla s_e = 0$

Equations of state  $p_i = n^\gamma \exp[(\gamma - 1)s_i] \quad p_e = n^\gamma \exp[(\gamma - 1)s_e]$

Gauss' law for magnetic field  $\nabla \cdot \mathbf{B} = 0$

Ampere's law  $n(\mathbf{u} - \mathbf{u}_e) = \varepsilon \nabla \times \mathbf{B}$

Faraday's law  $\nabla \times \mathbf{E} = 0 \Rightarrow \mathbf{E} = -\nabla \phi_E$

*Two-fluid parameter:  $\varepsilon \equiv \ell_i / L$*

ion skin depth:  $\ell_i \equiv c / \omega_{pi}$ ,  $L$ : system scale length

$\ell_i \propto m_i^{1/2} \rightarrow \varepsilon$ : ion inertial effect

HIST	$\varepsilon = 0.072$
NSTX	$\varepsilon = 0.034$
TS-3(FRC)	$\varepsilon = 0.20$

# Axisymmetric two-fluid equilibrium equations



## Generalized Grad-Shafranov equations for ion and electron surface variables

$$\text{ion: } \underbrace{\bar{\psi}'_i r^2 \nabla \cdot \left( \frac{\bar{\psi}'_i \nabla Y}{n r^2} \right)}_{\text{poloidal flow inertia}} = \underbrace{\frac{r}{\varepsilon} (B_\theta \bar{\psi}'_i - n u_\theta)}_{\mathbf{u} \times \mathbf{B} \text{ force}} + \underbrace{n r^2 (H'_i - T_i S'_i)}_{\text{gradient of pressure, flow energy, and electrostatic potential}} \rightarrow u_\theta$$

Arbitrary surface functions

$$\begin{aligned} &\bar{\psi}_e(\psi), \bar{\psi}_i(Y), \\ &H_e(\psi), H_i(Y), \\ &S_e(\psi), S_i(Y) \end{aligned}$$

$$\text{electron: } r^2 \nabla \cdot \left( \frac{\nabla \psi}{r^2} \right) = \frac{r}{\varepsilon} (B_\theta \bar{\psi}'_e - n u_\theta) - n r^2 (H'_e - T_e S'_e) \rightarrow \psi$$

Auxiliary equations

$$Y(r, z) \equiv \psi + \varepsilon r u_\theta$$

$$B_\theta = \frac{1}{\varepsilon r} (\bar{\psi}_i - \bar{\psi}_e)$$

$$\mathbf{u}_p = \frac{\nabla \bar{\psi}_i}{n r}$$

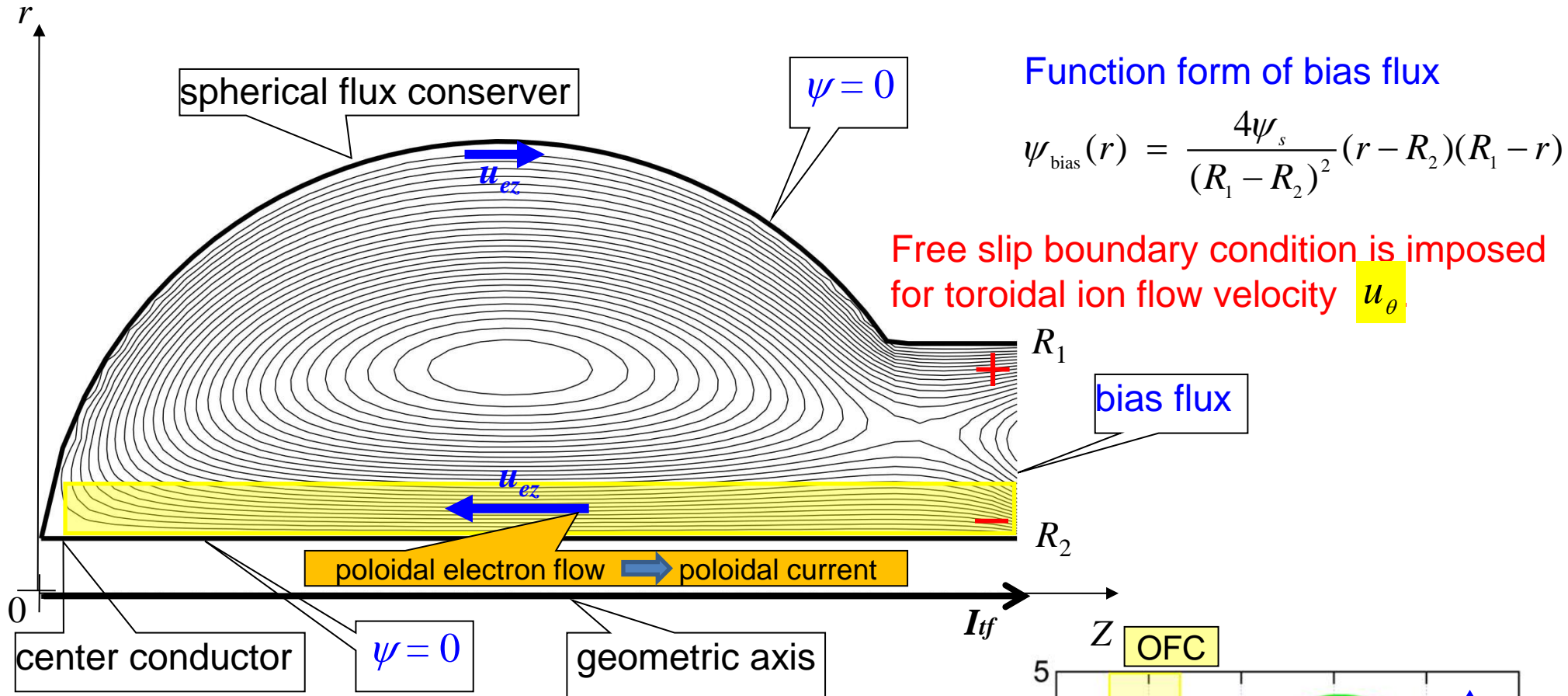
$$T_\alpha = n^{\gamma-1} \exp[(\gamma-1)S_\alpha]$$

## Generalized Bernoulli equations for density

$$\text{ion: } \underbrace{\frac{\gamma}{\gamma-1} n^{\gamma-1} \exp[(\gamma-1)S_i]}_{\text{enthalpy}} + \frac{u^2}{2} + \phi_E = H_i \rightarrow n$$

$$\text{electron: } \frac{\gamma}{\gamma-1} n^{\gamma-1} \exp[(\gamma-1)S_e] - \phi_E = H_e$$

# Boundary condition and assumption



Function form of bias flux

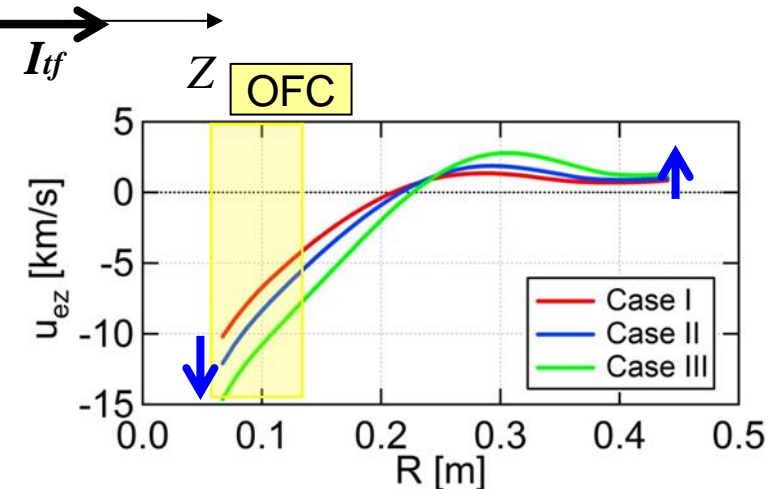
$$\psi_{\text{bias}}(r) = \frac{4\psi_s}{(R_1 - R_2)^2} (r - R_2)(R_1 - r)$$

Free slip boundary condition is imposed for toroidal ion flow velocity  $u_\theta$

## ✓ Assumption

The poloidal electron flow along the open field lines is mainly driven by applying the CHI pulse.

I change to decrease the poloidal flow velocity in the OFC region.





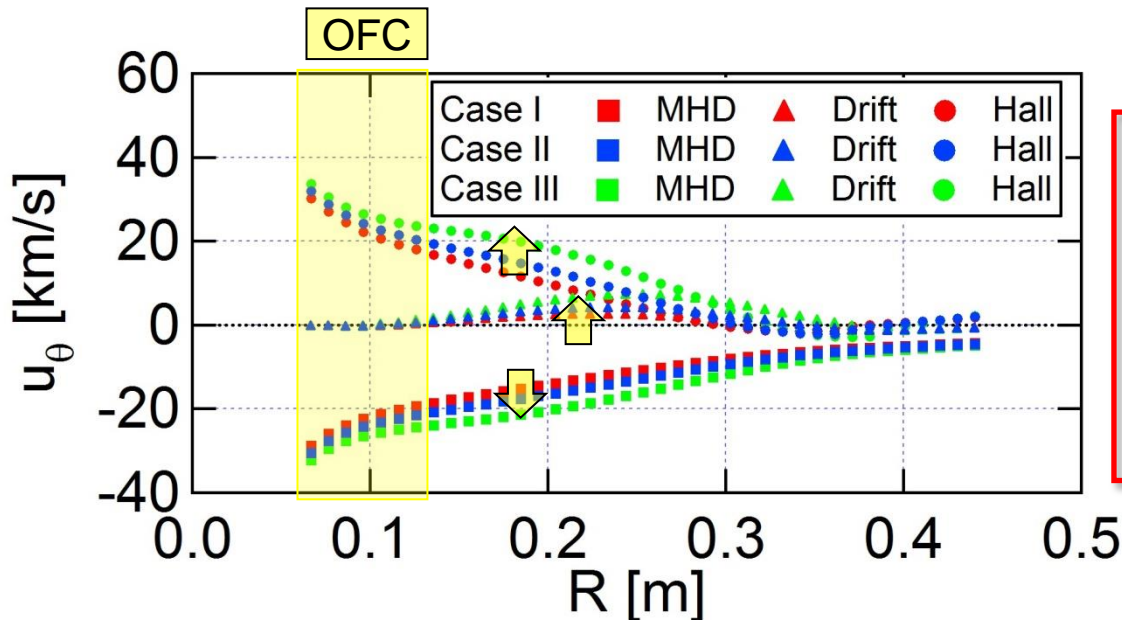
# Numerical results



- ✓ The toroidal ion flow velocity is increased in the closed flux region due to the increase of the electron drift velocity and the Hall effect.

Generalized Grad-Shafranov equation for electron

$$u_{\theta} = \underbrace{\frac{\bar{\psi}'_e}{n} B_{\theta}}_{\text{MHD term}} - \underbrace{\varepsilon r (H'_e - T_e S'_e)}_{\text{Electron drift velocity}} - \underbrace{\varepsilon \frac{r}{n} \nabla \cdot \left( \frac{\nabla \psi}{r^2} \right)}_{\text{Hall effect}}$$



- ✓ The MHD term is almost cancelled by the Hall term.
- ✓ The electron drift velocity term survives, causing the toroidal ion flow velocity in the closed flux region.

- ✓ The ion flow energy increases with the toroidal ion flow velocity in the closed flux region.
- ✓ The increase in the ion flow energy causes the decrease in the enthalpy in accordance with the generalized Bernoulli law.

Summed generalized Bernoulli equation

$$\underbrace{h_i + h_e}_{\text{Enthalpy}} + \frac{u^2}{2} = H_i + H_e, \quad h_\alpha = \frac{\gamma}{\gamma - 1} n^{\gamma-1} \exp[(\gamma - 1)S_\alpha]$$

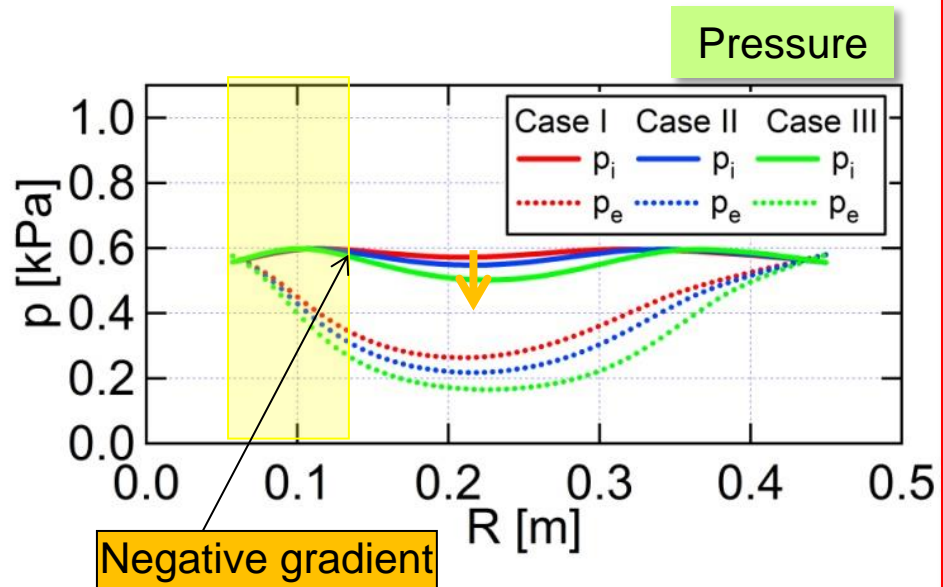
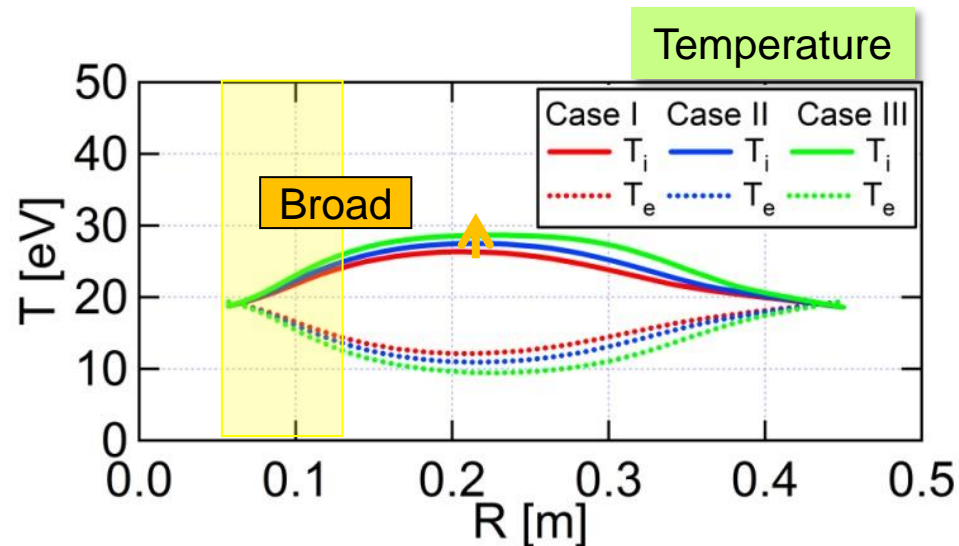
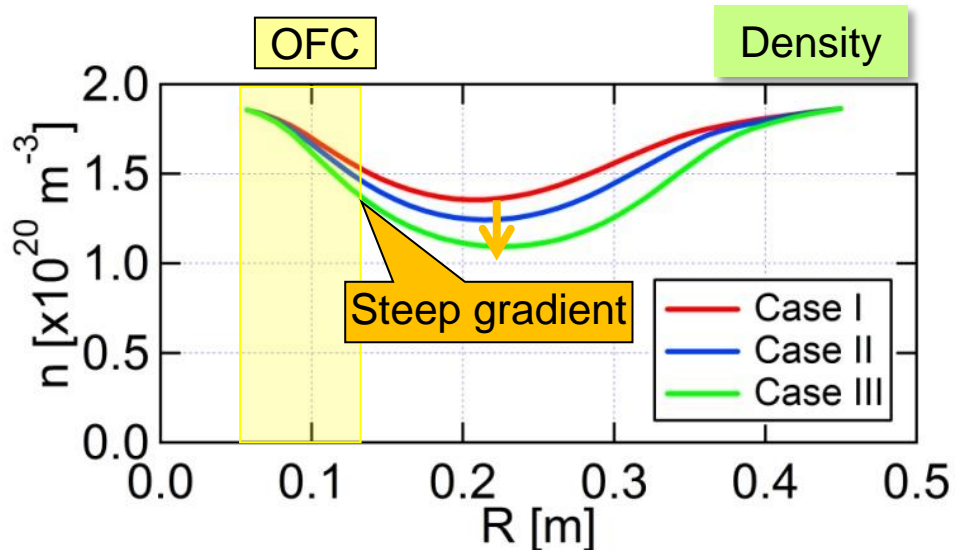
*Ion flow energy* (arrow pointing to  $\frac{u^2}{2}$ )

*Density* (arrow pointing to  $n$ )

- ✓ The decrease in the enthalpy causes the drop in the density.
- ✓ The density is decreased in the closed flux region, and its gradient steepens around the separatrix in the high field side.

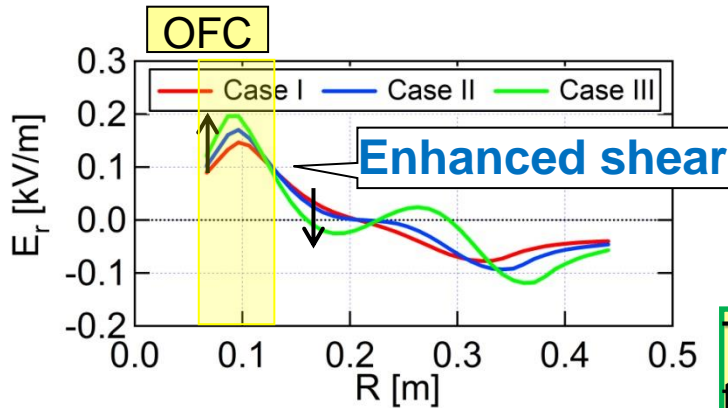


# Number density, temperature, and pressure profiles at the midplane

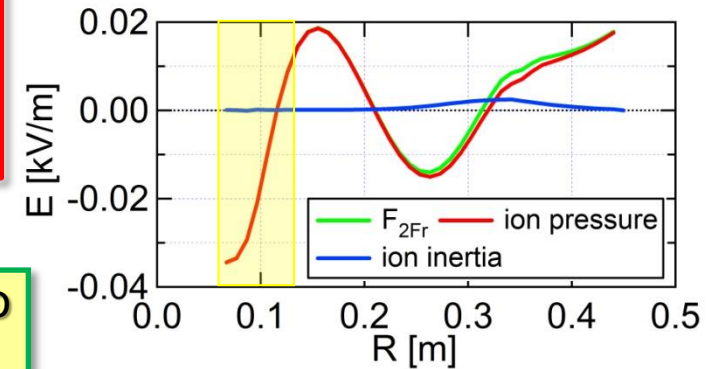


- ✓ The density is decreased in the closed flux region and its **negative gradient** around the separatrix **steepens**.
- ✓ The ion temperature is slightly increased in the closed flux region, and becomes to the **broad** profile.
- ✓ In the electron temperature, the **hollow profile** is enhanced.
- ✓ The gradient of the ion pressure becomes **negative** around the separatrix.
- ✓ In the electron pressure, the **hollow profile** is enhanced.

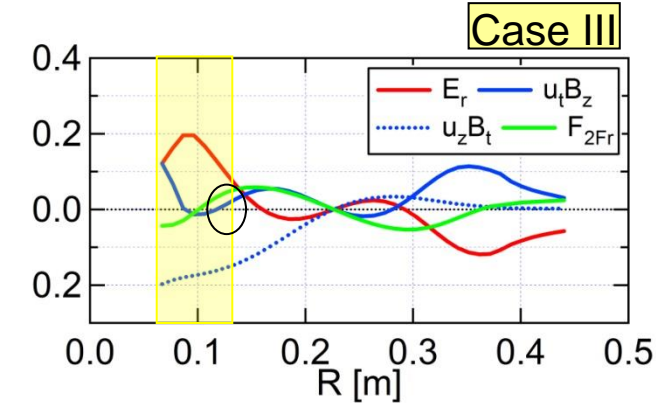
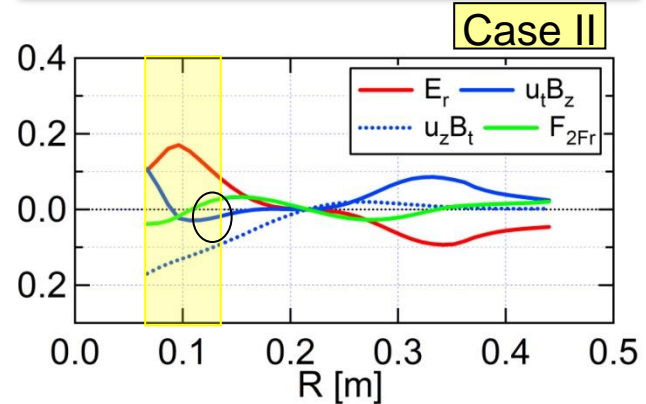
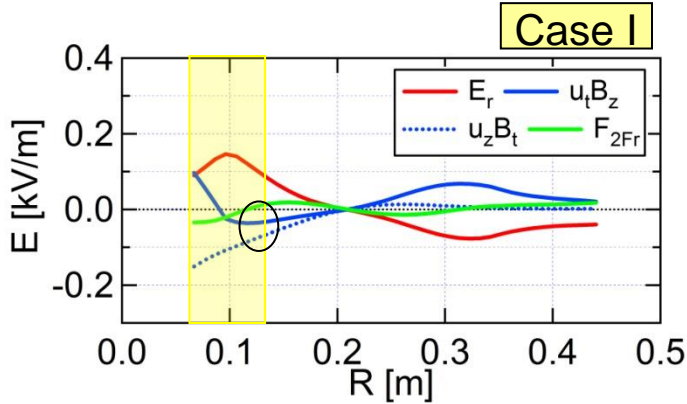
# Radial electric field and two-fluid effect



The radial electric field is enhanced around the separatrix.



The two-fluid effect is due to the ion diamagnetic effect.



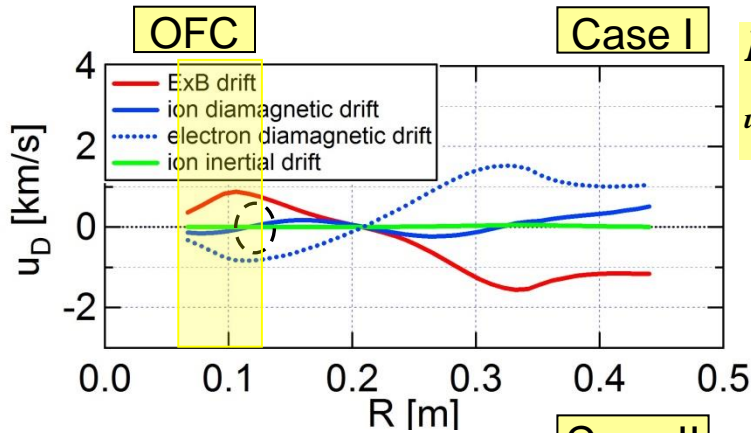
The radial electric field strongly depends on the magnetic force  $1/\epsilon u_t B_z$ .

Ohm's law: 
$$\mathbf{E} + \frac{1}{\epsilon} \mathbf{u} \times \mathbf{B} + \mathbf{F}_{2F} = 0, \quad E_r + \frac{1}{\epsilon} (u_t B_z + u_z B_t) + F_{2Fr} = 0$$

Two-fluid effect: 
$$\mathbf{F}_{2F} = -\nabla p_i / n - \mathbf{u} \cdot \nabla \mathbf{u}$$

↑ Ion diamagnetic effect      ↑ Ion inertial effect

# Poloidal component of drift velocity



$E \times B$  drift velocity

$$\mathbf{u}_E = \varepsilon \frac{\mathbf{E} \times \mathbf{B}}{B^2}$$

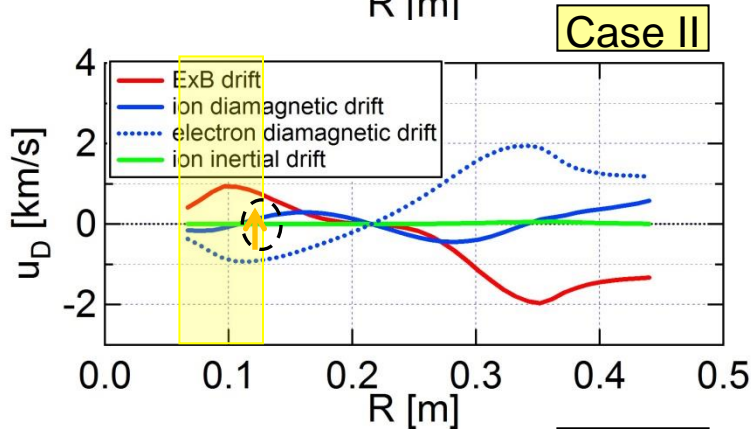
Diamagnetic drift velocity

$$\mathbf{u}_D = \varepsilon \frac{\mathbf{B} \times \nabla p_i}{B^2 n}$$

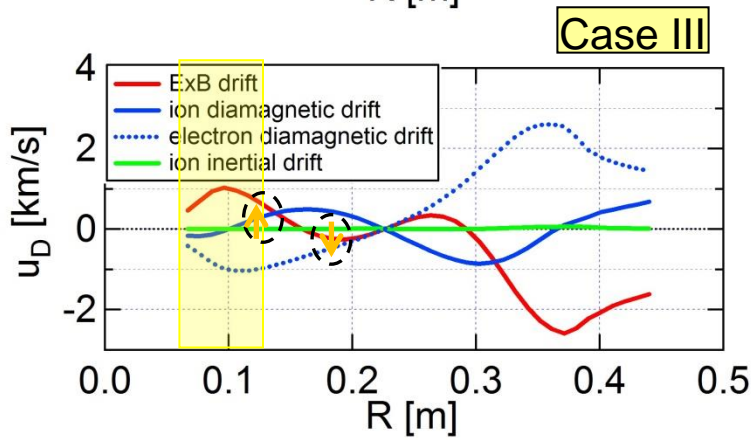
Inertial drift velocity

$$\mathbf{u}_i = \varepsilon \frac{\mathbf{B} \times (\mathbf{u}_i \cdot \nabla \mathbf{u}_i)}{B^2}$$

- ✓ The ion diamagnetic drift velocity is comparable to the  $ExB$  and electron diamagnetic ones, but the ion inertial drift velocity is small.



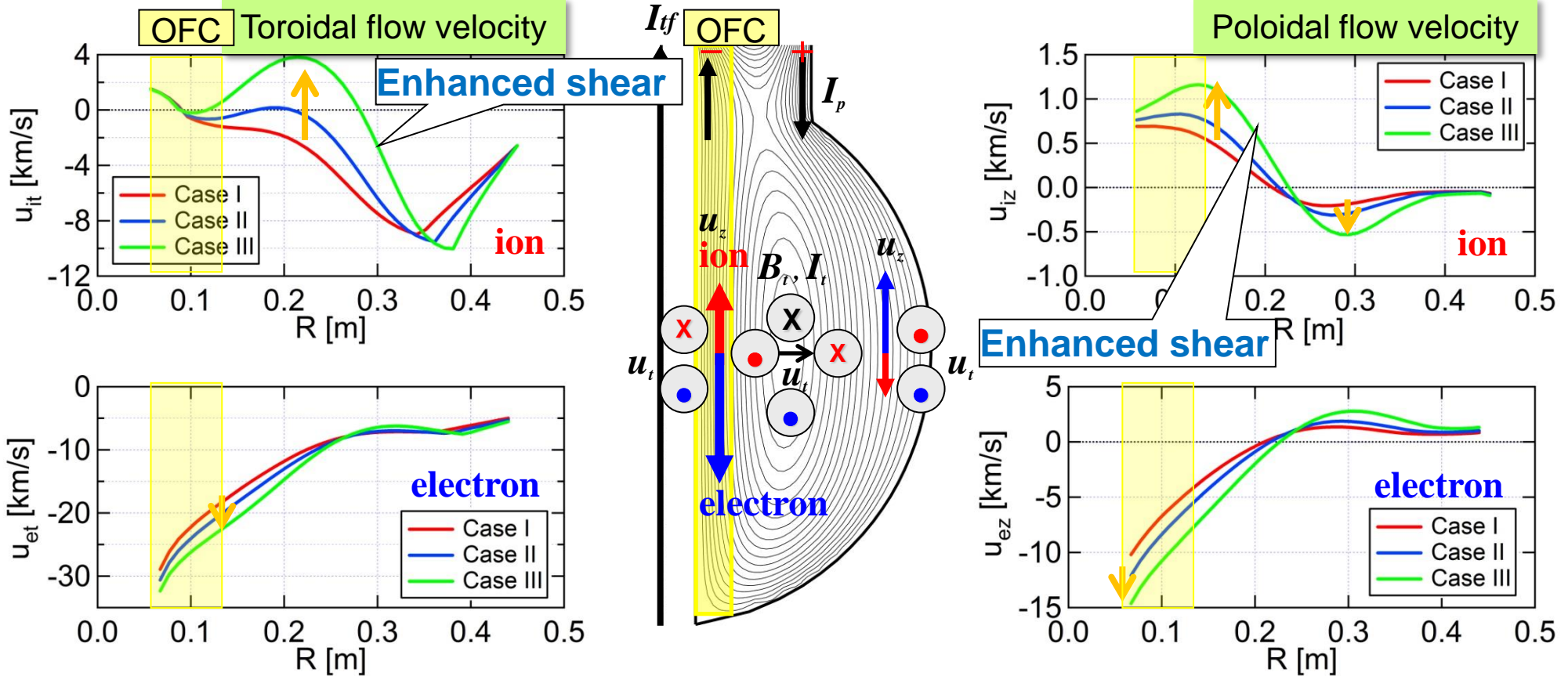
- ✓ The ion diamagnetic drift velocity is increased around the separatrix, changing the same direction as the the  $ExB$  one there.
  - ➡ increase in the poloidal flow velocity



- ✓ The  $ExB$  drift velocity is decreased in the closed flux region, changing the opposite direction to the ion diamagnetic drift velocity there.
  - ➡ decrease in the poloidal flow velocity
  - ➡ increase in the flow shear



# Flow velocity profiles at the midplane



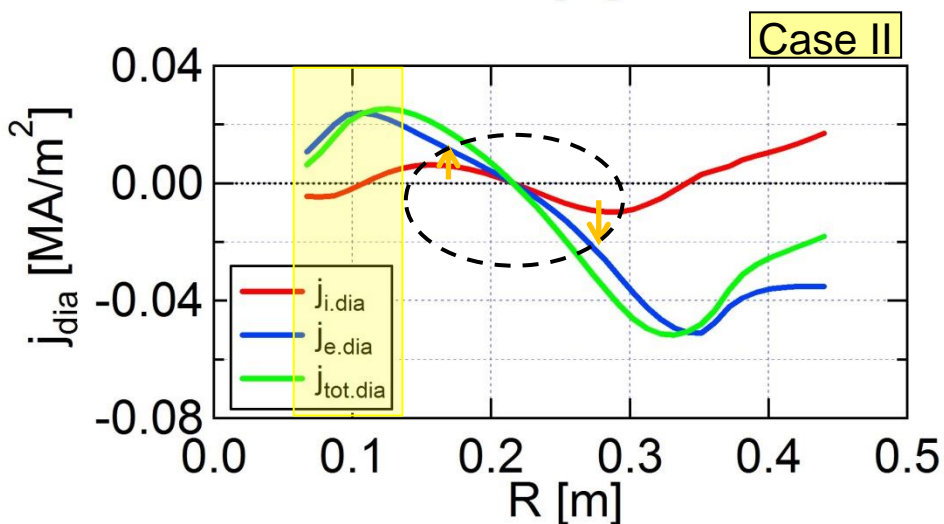
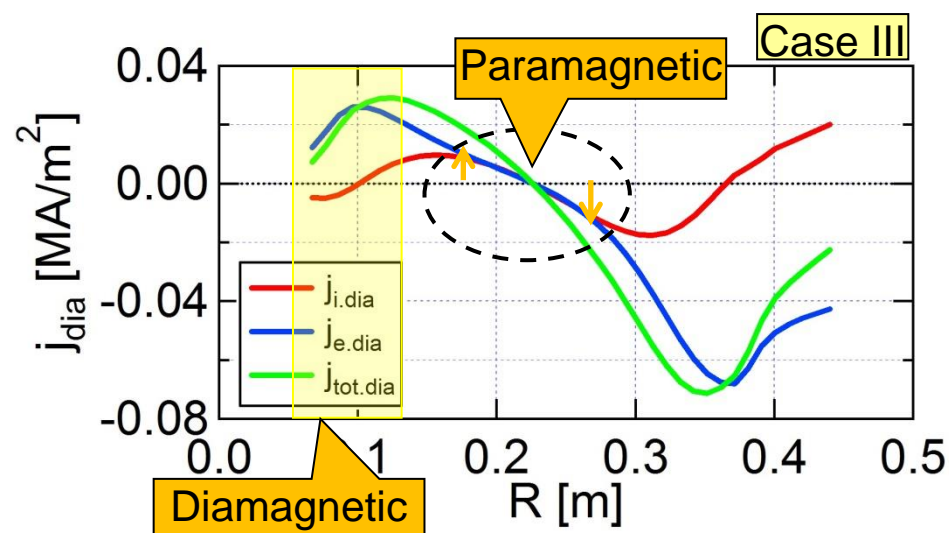
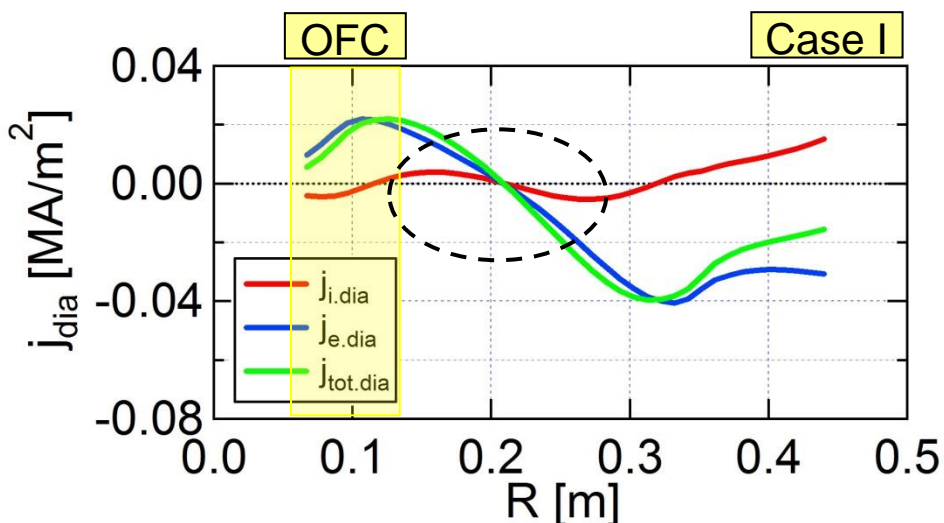
Toroidal flow velocity

- ✓ The ion flow velocity is increased from negative to positive values in the closed flux region, enhancing the flow shear and contributing to the increase in the current.
- ✓ The electron flow velocity is slightly decreased in the OFC region.

Poloidal flow velocity

- ✓ The ion flow velocity is increased in the OFC region, enhancing the flow shear around the separatrix, and contributing to the increase in the current.

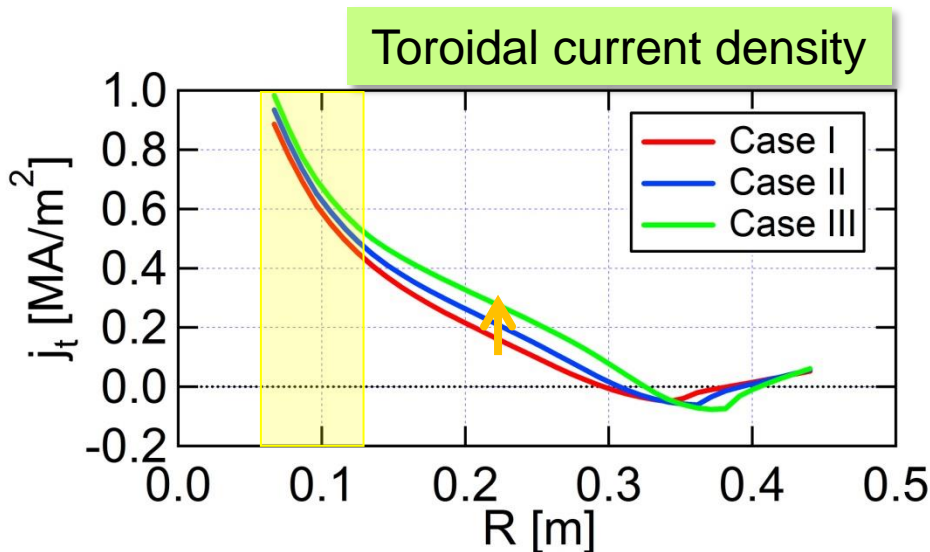
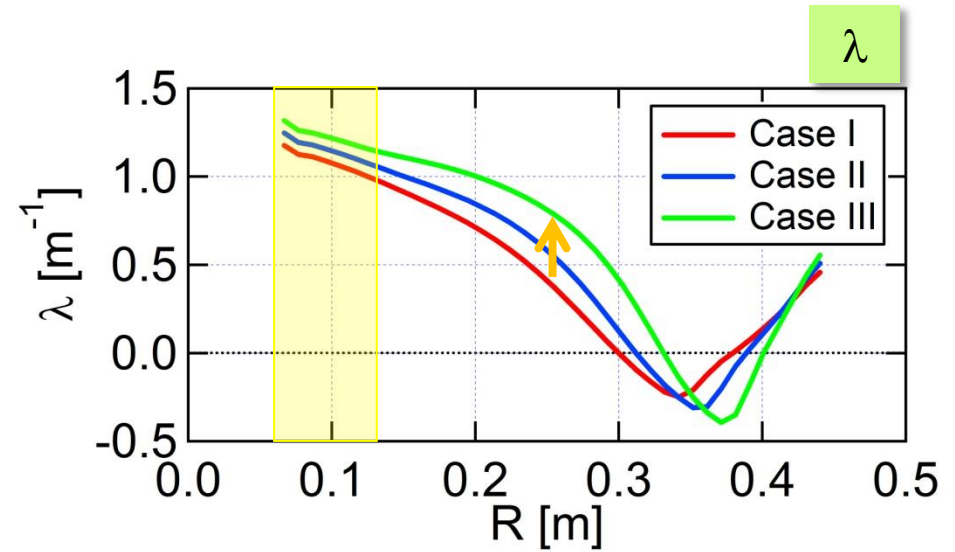
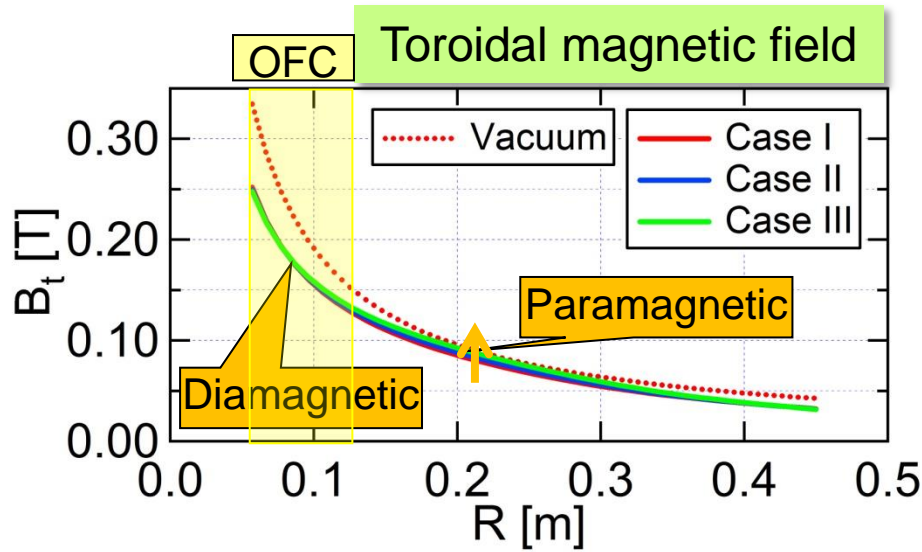
# Poloidal diamagnetic current density



- ✓ The strength of diamagnetic ion current density is increased in the closed flux region, approaching that of diamagnetic electron current density.
- ✓ The total diamagnetic current is carried by both ion and electron fluids.
- ✓ The total current profile becomes steep in the closed flux.

➔ The **paramagnetic toroidal field** is generated in the closed flux region.

# Magnetic field and current density profiles at the midplane



✓ The toroidal magnetic field becomes from a **diamagnetic** to a **paramagnetic** profile in the closed flux region, while the diamagnetic profile is kept in the OFC region.

✓ The toroidal current density and  $\lambda$  have the **hollow profiles**, and are increased in the closed flux region.

➡ Increased closed poloidal flux



# Summary



We have investigated the relation between poloidal ion flow velocity and toroidal field due to applying the CHI pulse again.

- The CHI pulse causes **the steep density gradient around the separatrix** in the high field side.
- The ion diamagnetic drift velocity is changed to **the same direction as the the  $ExB$  one** around the separatrix as the ion pressure gradient steepens there. The  $ExB$  drift velocity is decreased in the closed flux region, changing **the opposite direction to the ion diamagnetic drift velocity** there.
- The poloidal ion flow velocity is increased around the separatrix but decreased in the closed flux region, **enhancing the flow shear**.
- The toroidal magnetic field becomes **from a diamagnetic to a paramagnetic profile** in the closed flux region, because the poloidal diamagnetic current profile becomes steep there.