

第18回 若手科学者によるプラズマ研究会 主題：プラズマ計測・制御技術の結集  
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# マイクロ波-ミリ波-テラヘルツ波を用いた 磁場閉じ込め核融合プラズマ計測

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核融合科学研究所



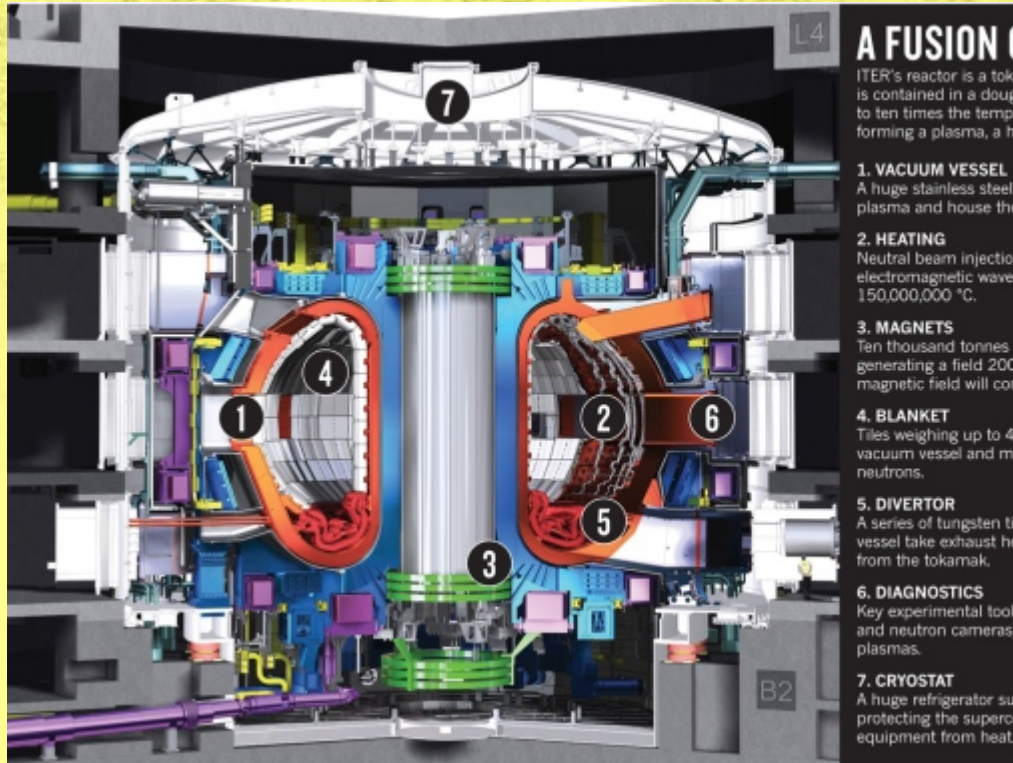
資料協力：長山、久保、田中、秋山(核融合研)、西浦(東大)

# Contents

- はじめに
- 干渉計
  - マイクロ波干渉計、FIRレーザー干渉計、分散干渉計
- 反射計
  - ドップラー反射計、パルスレーダー
- 協同トムソン散乱
- まとめ



# ITER Diagnostics



## A FUSION OF IDEAS

ITER's reactor is a tokamak in which the fuel is contained in a doughnut-shaped chamber heated to ten times the temperature of the sun, forming a plasma, a hot ionized gas.

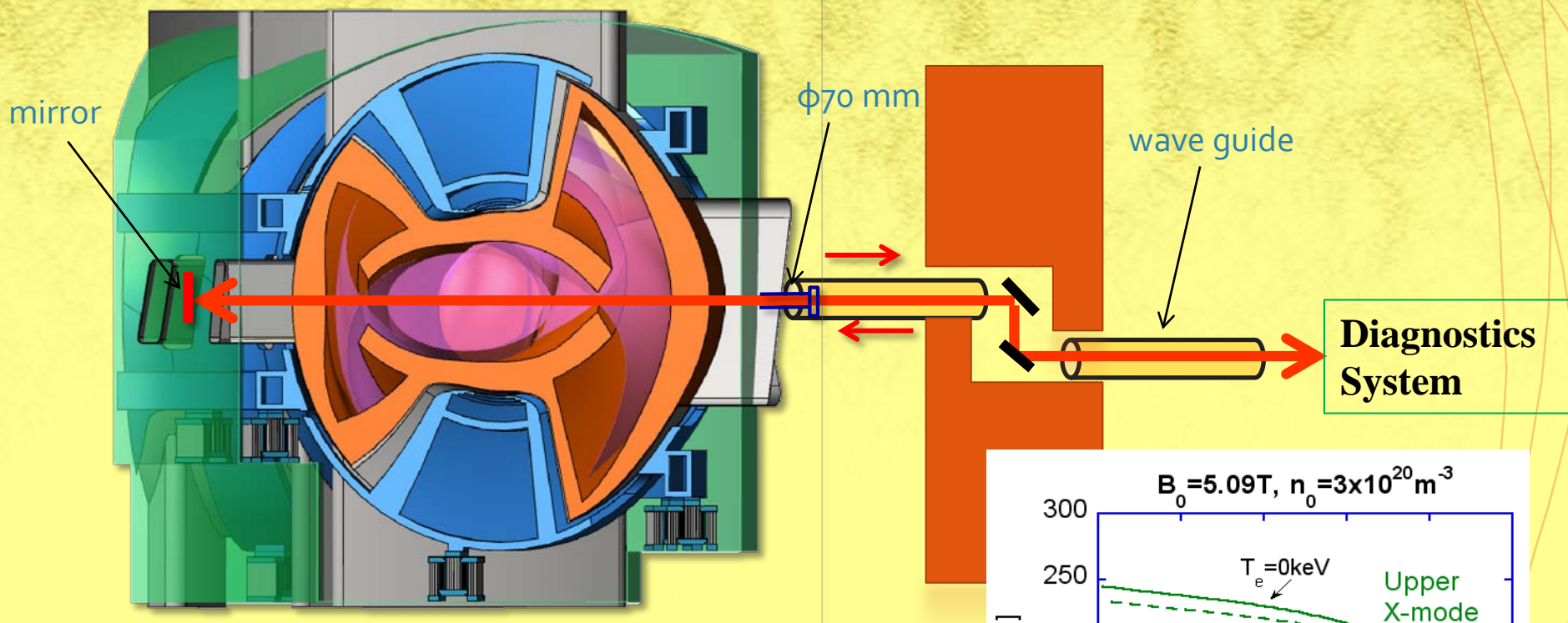
- 1. VACUUM VESSEL**  
A huge stainless steel chamber to contain the plasma and house the heating systems.
- 2. HEATING**  
Neutral beam injection and radio-frequency electromagnetic waves to heat the plasma to 150,000,000 °C.
- 3. MAGNETS**  
Ten thousand tonnes of superconducting magnets generating a field 200 times that of the Earth to confine the plasma.
- 4. BLANKET**  
Tiles weighing up to 4 tonnes will surround the vacuum vessel and maintain the temperature of the plasma.
- 5. DIVERTOR**  
A series of tungsten tiles will divert the exhaust heat from the tokamak.
- 6. DIAGNOSTICS**  
Key experimental tools and neutron cameras for monitoring the plasma.
- 7. CRYOSTAT**  
A huge refrigerator surrounding the tokamak to protect the superconducting magnets from heat.

The **diagnostics system** will comprise about **50 individual measuring systems** drawn from the full range of modern plasma diagnostic techniques, including lasers, X-rays, neutron cameras, impurity monitors, particle spectrometers, radiation bolometers, pressure and gas analysis, and optical fibres.

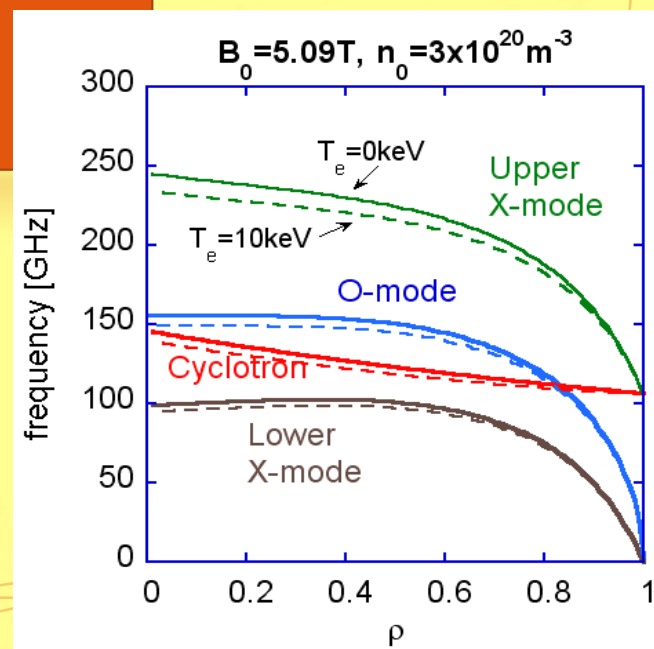
Magnetic Diagnostics	Spectroscopic and NPA Systems
Vessel Magnetics	CXRS Active Spectroscopy (+DNB)
In-vessel magnetics	H Alpha Spectroscopy
Divertor Coils	VUV Impurity Monitoring (Main Plasma)
Continuous Rogowski Coils	Visible & UV Impurity Monitoring (Divertor)
Diamagnetic Loop	
Halo Current Sensors	
Neutron Diagnostics	X-Ray Crystal Spectrometers
Radial Neutron Camera	Visible Continuum Array
Vertical Neutron Camera	Soft X-Ray Array
Microfission chambers (in-vessel)	Neutral Particle Analyzers
Neutron Flux Monitors (ex-vessel)	Laser Induced Fluorescence
Gamma-Ray Spectrometers	MSE based on Heating Beam
Neutron Activation Systems	
Lost Alpha Detectors	
Knock-on Tail Neutron Spectrometer	
Optical/IR Systems	Microwave Diagnostics
Thomson Scattering (Core)	ECE Diagnostics for Main Plasma
Thomson Scattering (Edge)	Reflectometers for Main Plasma
Thomson Scattering (X-point)	Reflectometers for Plasma Position
Thomson Scattering (Divertor)	Reflectometers for Divertor Plasma
Toroidal Interferometer/Polarimeter	ECA for Divertor Plasma
Polooidal Polarimeter	Microwave Scattering (Main Plasma)
Collective Thomson scattering	Fast Wave Reflectometry
Bolometric Systems	Plasma-Facing Component & Operational Diagnostics
Bolometric Array (Main Plasma)	IR Cameras, visible/IR TV
Bolometric Array (Divertor)	Thermocouples
	Pressure Gauges
	Residual Gas Analyzers
	IR Thermography Divertor
	Langmuir Probes

Table 1. Overview of the diagnostics foreseen at ITER  
A.J.H. Donne, FST, 61, 357 (2012)

# 将来の核燃焼炉でも電磁波計測は有用



- ✓ 迷路構造の伝送導波路の適用可
- ✓ 狭小な真空窓でのアクセスに対応可
- ✓ 高信頼性の確立



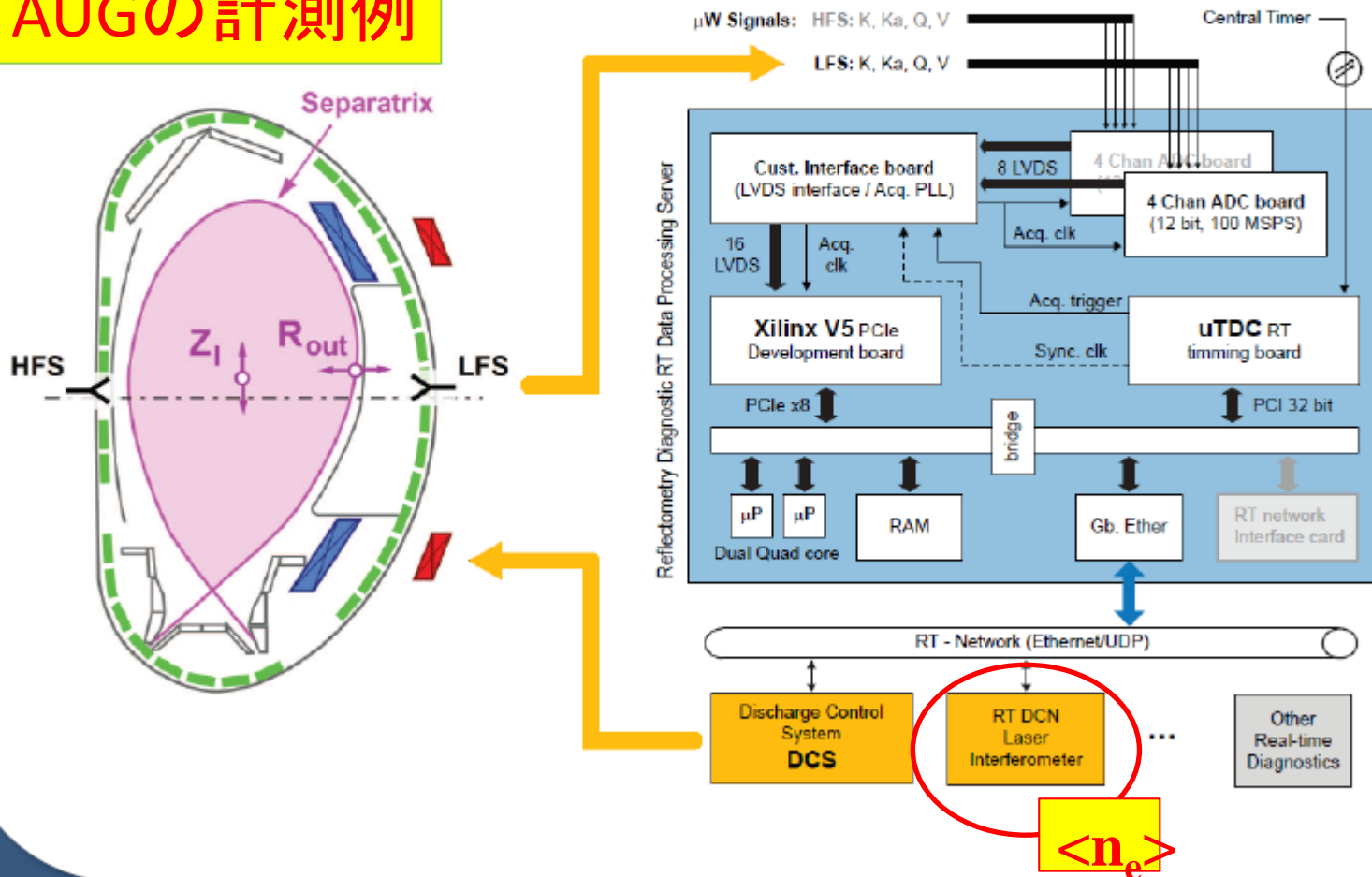
# 計測器への要求

- 高精度化：精緻な計測システムにより、新しい物理の解明に貢献
- 高信頼化：安定な運転制御のために必要なパラメータの提供



# Real-time diagnostic / system integration

## AUGの計測例



# Reflectometry PP demonstration on AUG

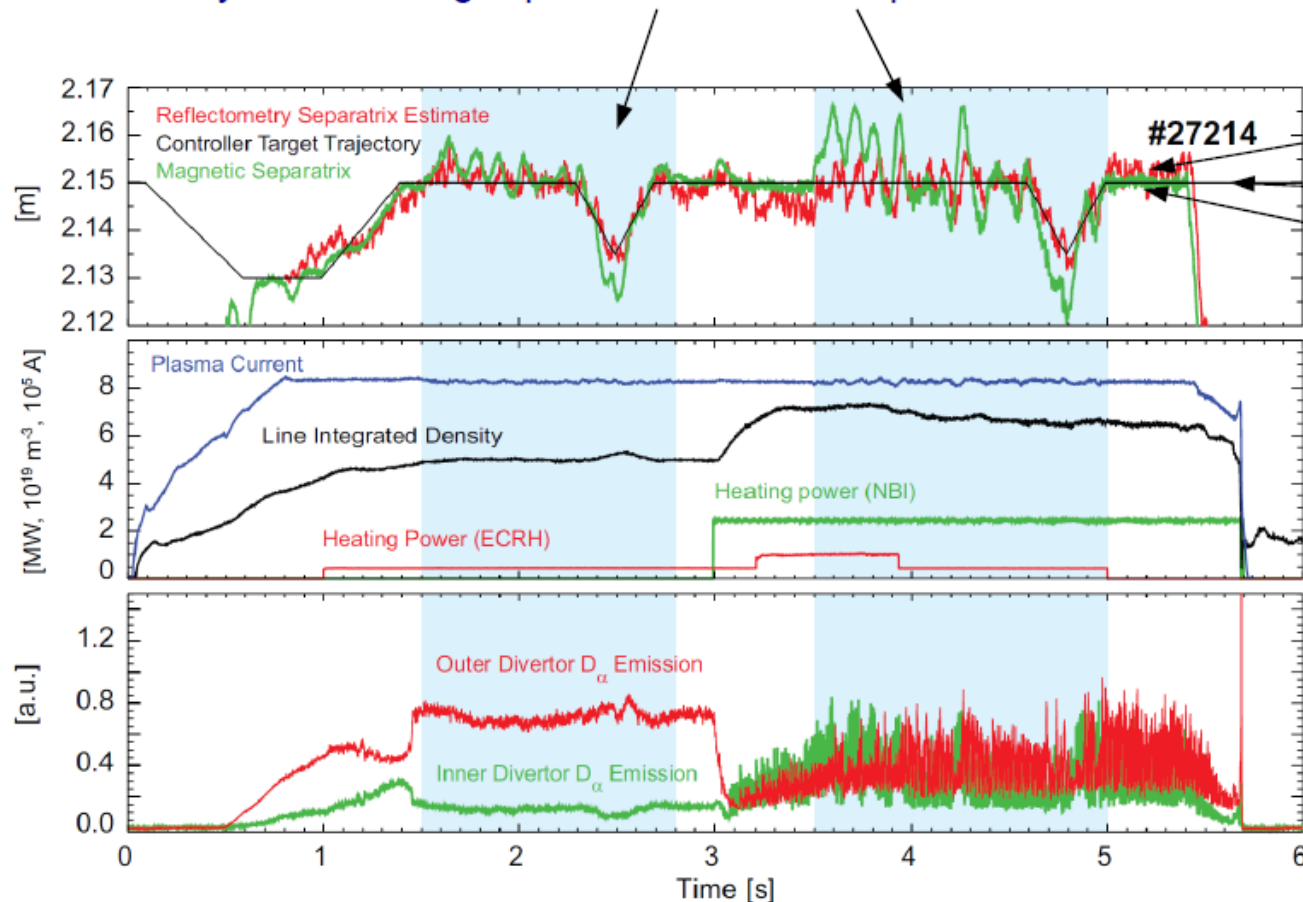
J.Santos



## L-mode、H-mode (type-I ELM付)における位置制御に成功

### First demonstration discharge

Reflectometry control during separate L and H-mode phases



- $R_{out}$ : outer (LFS) plasma position
- Reflectometer Requested Magnetic
- Refl. tracks mag. during non-control phases (ramp-up & down)
- Refl. maintains good control when in change – even during programmed radial movement
- Overshots in mag. signal t.b. resolved

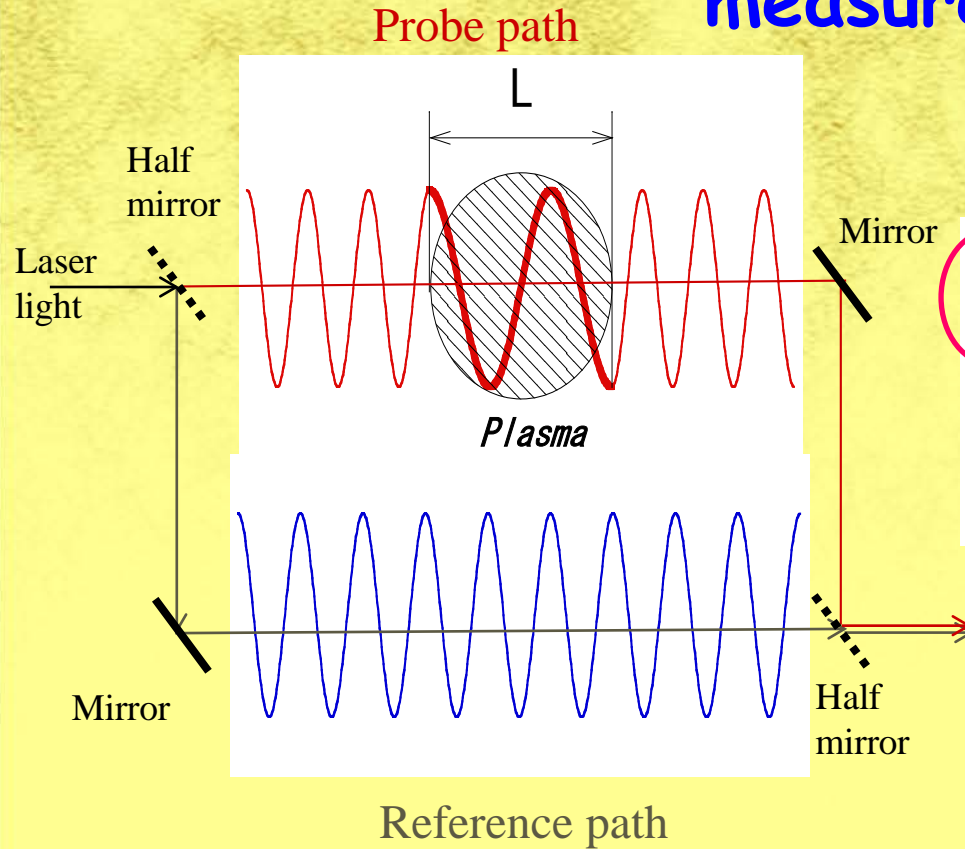
# Contents

- はじめに
- 干渉計
  - マイクロ波干渉計、FIRレーザー干渉計、分散干渉計
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# Principle of interferometer for electron density measurements



Phase difference with plasma is given by

$$\delta\phi = k\delta\mu L = 2\pi \frac{\delta\mu L}{\lambda} = \frac{2\pi}{\lambda} \frac{1}{2} \frac{\lambda^2 e^2}{4\pi c^2 \epsilon_0 m_e} \bar{n} L$$

$$\propto \lambda \bar{n} L$$

$\bar{n}$  ; line averaged electron density

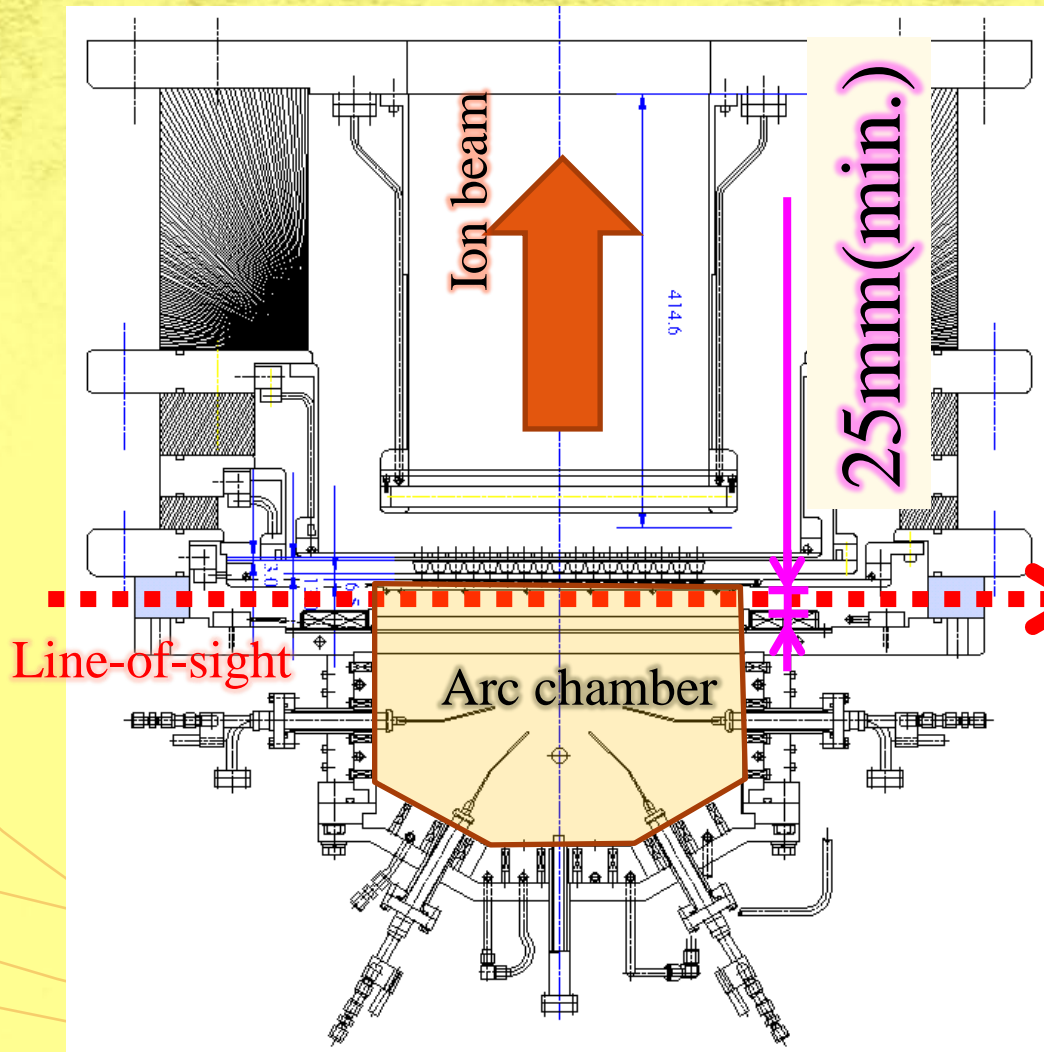
Since,  $\delta\phi \propto \lambda, \delta\phi \propto \omega^{-1}$

As long as  $\omega \gg \omega_p, \omega_c$  is satisfied.

longer wavelength (lower frequency) is preferable to get larger phase shift.

低密度プラズマ → マイクロ波、ミリ波  
高密度プラズマ → FIR、IR

# Interferometer for 1/3 scaled Negative Ions Source



## [目的]

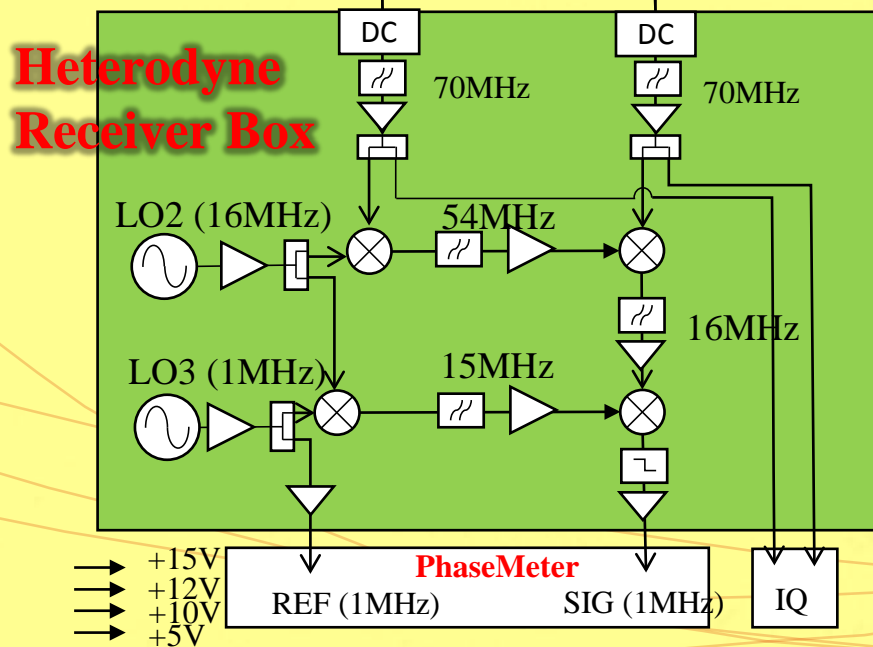
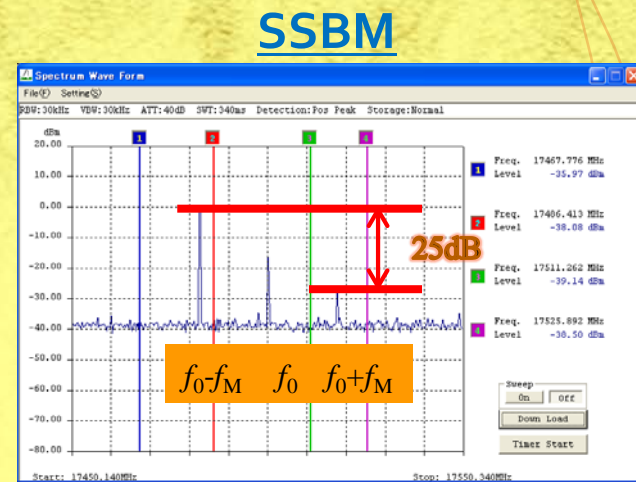
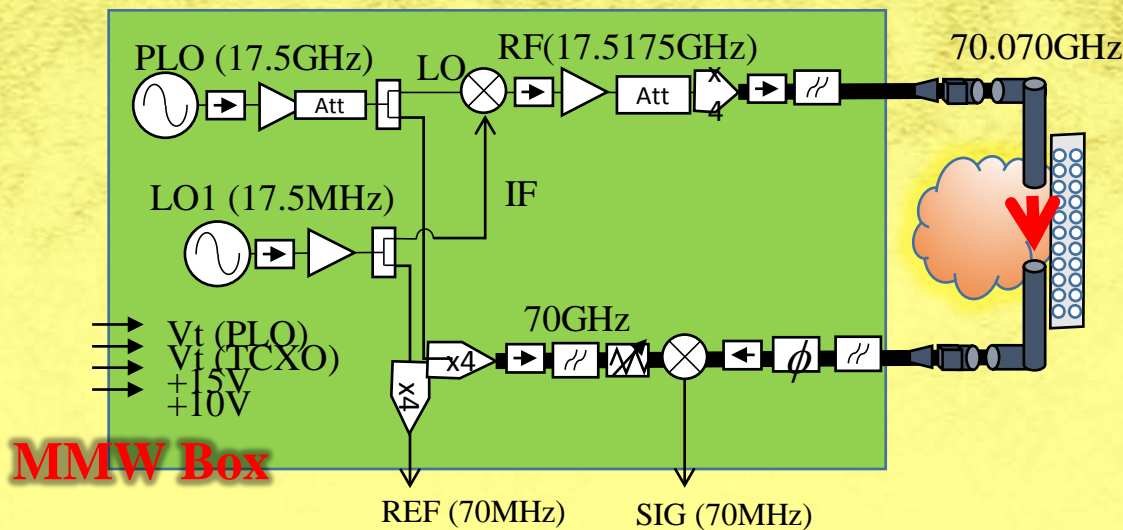
NBI負イオン源内における、Cs添加→負イオン増大時の電子密度の減少量の計測

ターゲット電子密度 :  $10^{16-17} \text{m}^{-3}$

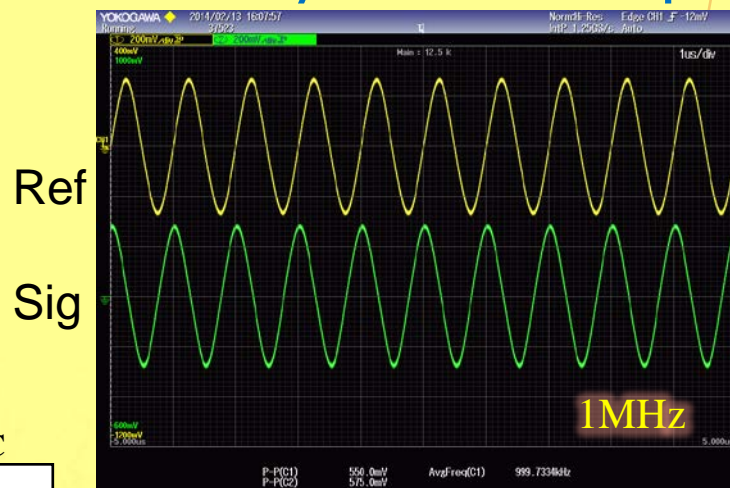
## [課題]

- ✓ 狭小なアクセス路→金属導波管
- ✓ 加速高電圧印加→絶縁導波
- ✓ 干渉計波長の選択→ミリ波
- ✓ 位相計測→高感度1/2000フリンジ位相計

# Millimeter wave interferometer



## Heterodyne receiver output



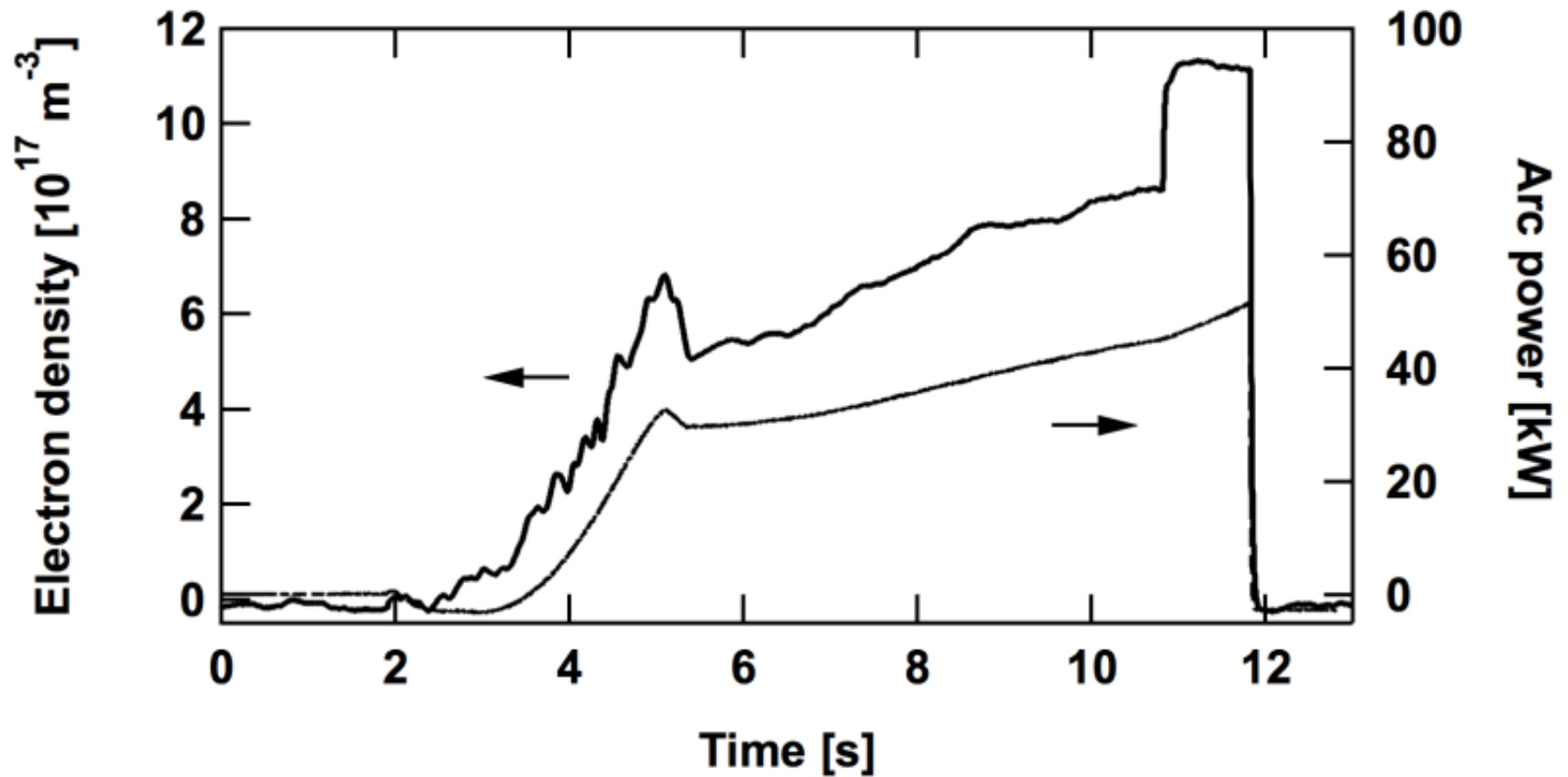


Figure 1 shows the time evolution of the electron density obtained with improved millimeter-wave interferometer in the pure hydrogen plasma. The beam was extracted from 10.8 s to 11.8 s. The electron density changes with the arc power and rapidly rises when the extraction voltage is applied. Amount of the electron density change before and after the beam extraction is  $2.6 \times 10^{17} \text{ m}^{-3}$ . It has been observed that the negative ion density shows the different response to the extraction voltage and it rapidly drops with beam extraction.

# Choice of probe beam wavelength

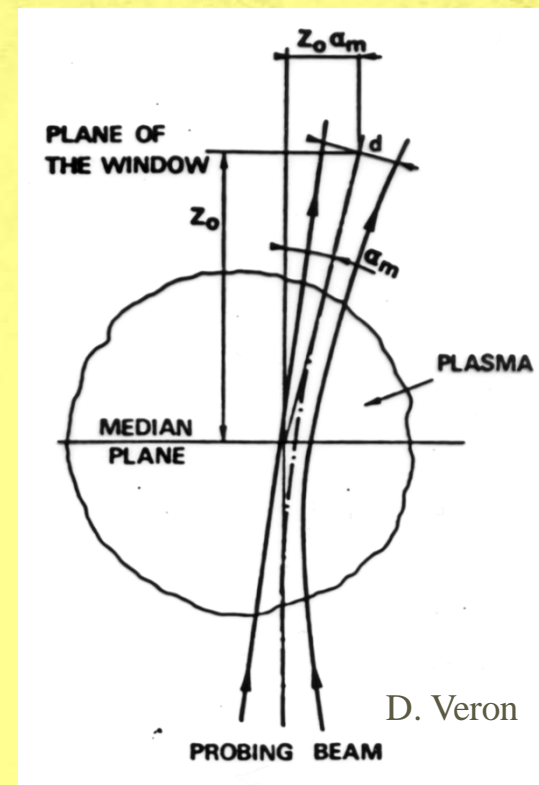
- Low frequency (long wavelength) limit
  - Refraction problem due to plasma density gradient sets the long wavelength limit

$$\alpha_m = \sin^{-1}\left(\frac{n_o}{n_c}\right) \cong \frac{n_o}{n_c} = 8.97 \times 10^{-16} n_o \lambda^2$$

$$\lambda \leq 1.16 \times 10^{10} (Z_o n_o^2)^{-1/3} m$$

- Example:  $Z_o = 3.8 m$ ,  $n_e(0) = 2 \times 10^{20}/m^3$  leads to  $\lambda < 210 \mu m$

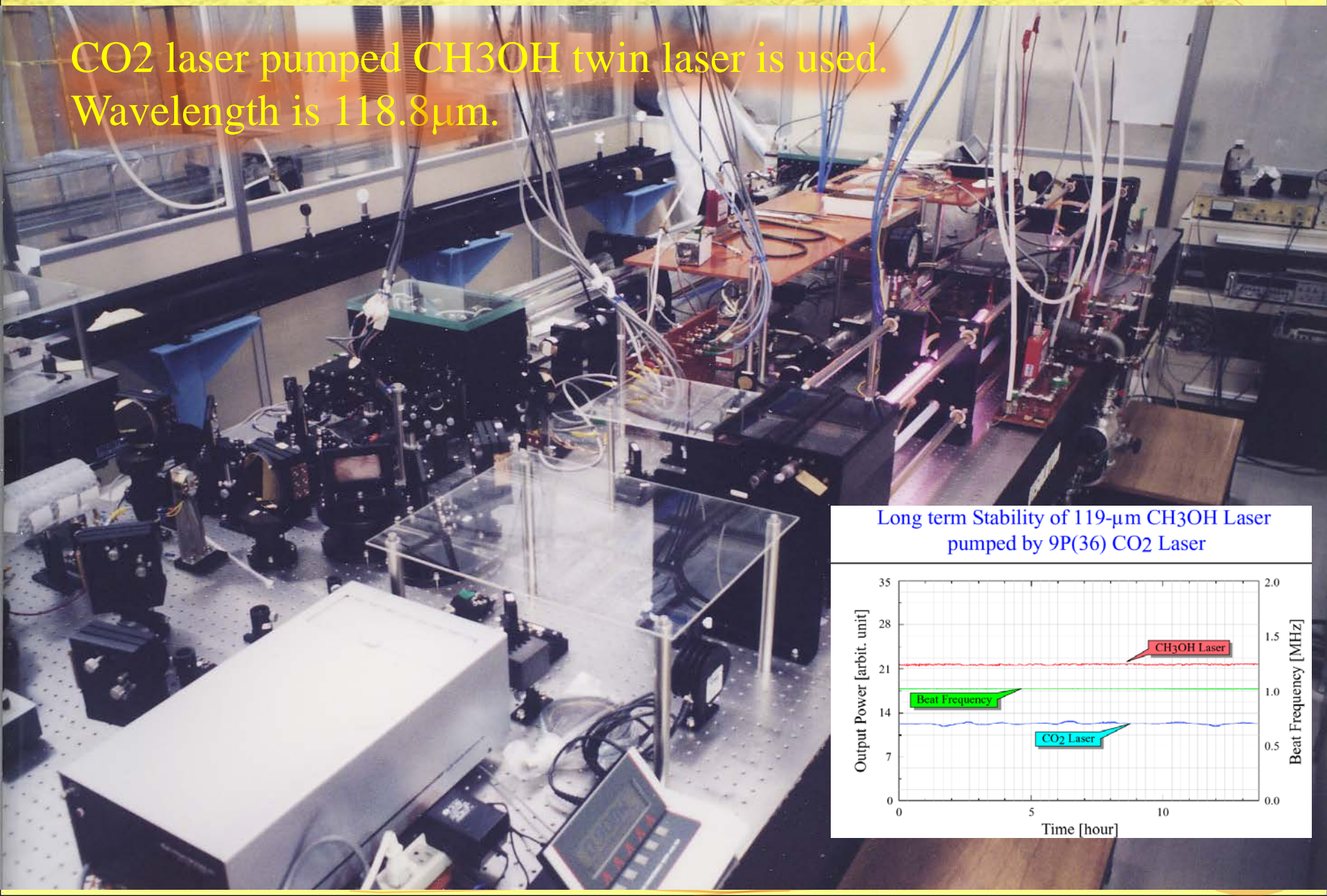
$$d = 2\left(\frac{\lambda Z_o}{\pi}\right)^{1/2} \rightarrow Z_o \alpha_m \leq 2\left(\frac{\lambda Z_o}{\pi}\right)^{1/2}$$



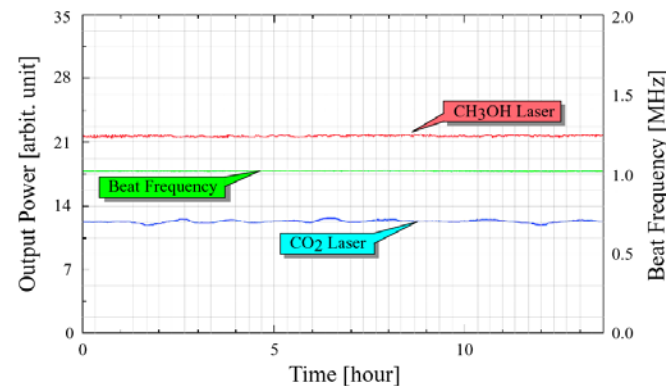
波長が長いほど、屈折の効果が大きい。

# 119- $\mu\text{m}$ CH<sub>3</sub>OH Laser System on LHD

CO<sub>2</sub> laser pumped CH<sub>3</sub>OH twin laser is used.  
Wavelength is 118.8 $\mu\text{m}$ .



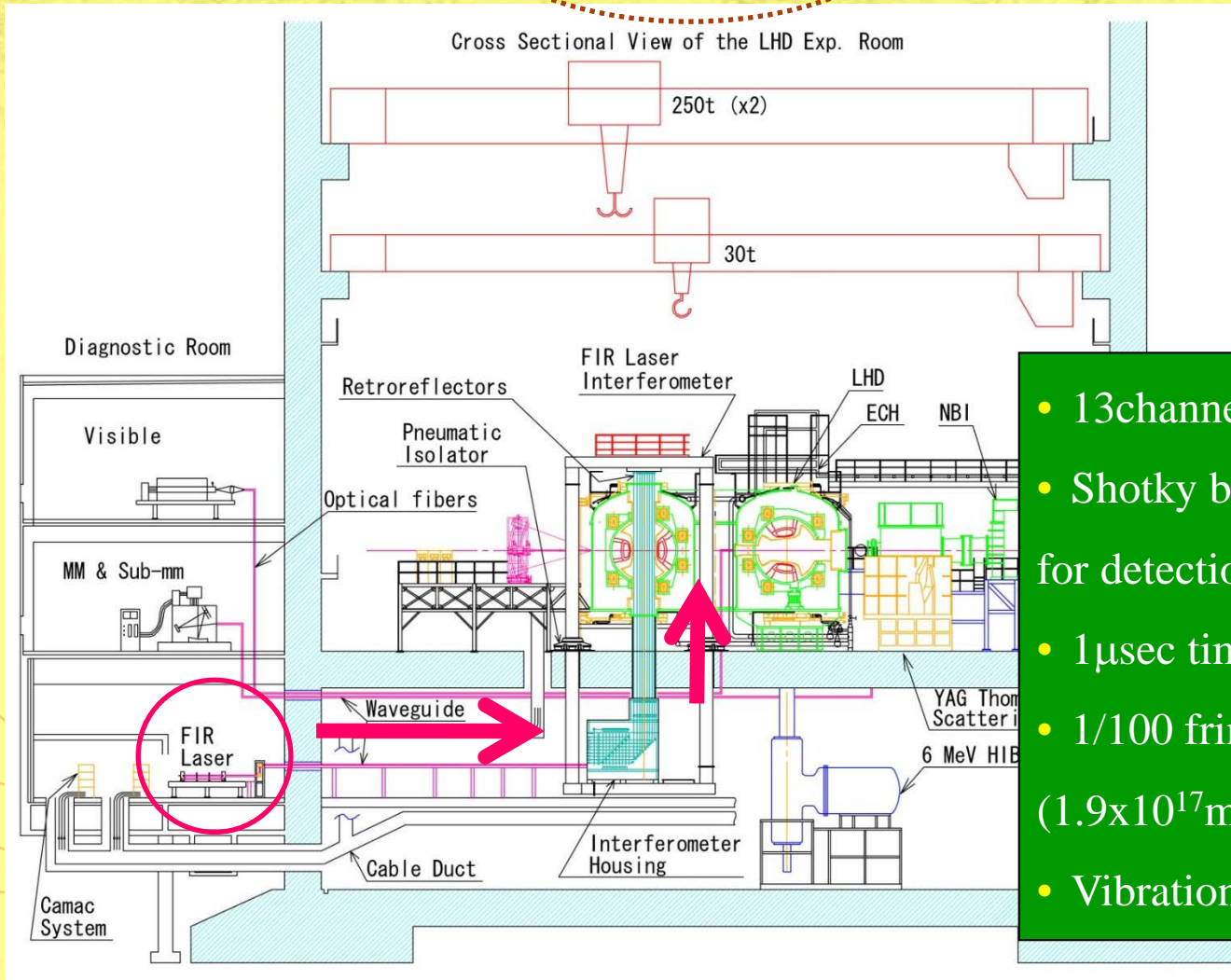
Long term Stability of 119- $\mu\text{m}$  CH<sub>3</sub>OH Laser  
pumped by 9P(36) CO<sub>2</sub> Laser



# Cross Sectional View of the LHD Exp. Room

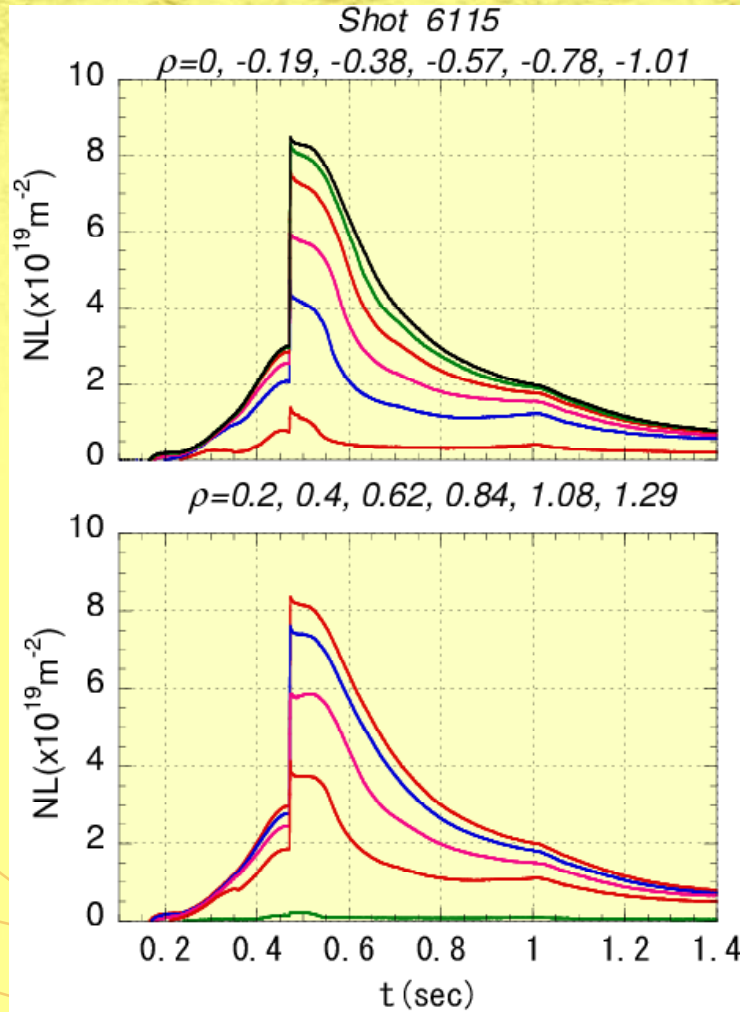
$$\Delta\phi = 2.8 \times 10^{-15} \lambda \int_{Y_1}^{Y_2} n_e(r) dy + \frac{3.9 \times 10^{-29}}{\lambda} \int_{Y_1}^{Y_2} n_n(r) dy + \frac{2\pi\Delta L}{\lambda}$$

振動成分

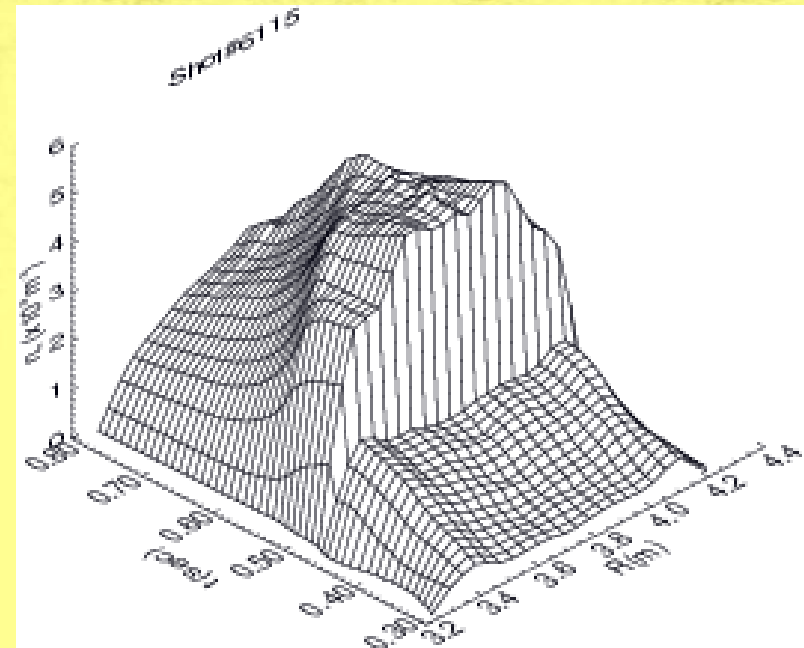


- 13 channels 90mm spacing.
- Shotky barrier diodes are used for detection
- 1 μsec time resolution.
- 1/100 fringe resolution (1.9x10<sup>17</sup> m<sup>-2</sup>)
- Vibration is negligible.

# 電子密度の再構成分布の例



## Density profile



Change of Density profiles after single pellet injection.  $R_{ax}=3.75m$ ,  
 $B_t=1.5T$ , NBI heated



# 1. What is dispersion interferometer?

## Conventional Interferometer

(for electron density measurement)

### Advantages

1. High temporal and density resolutions
2. Widely used (well matured technique)

### Disadvantages

1. Errors due to mechanical vibrations

solution

- Vibration isolation system
- Two color interferometer

2. Fringe jump errors in high density range

solution

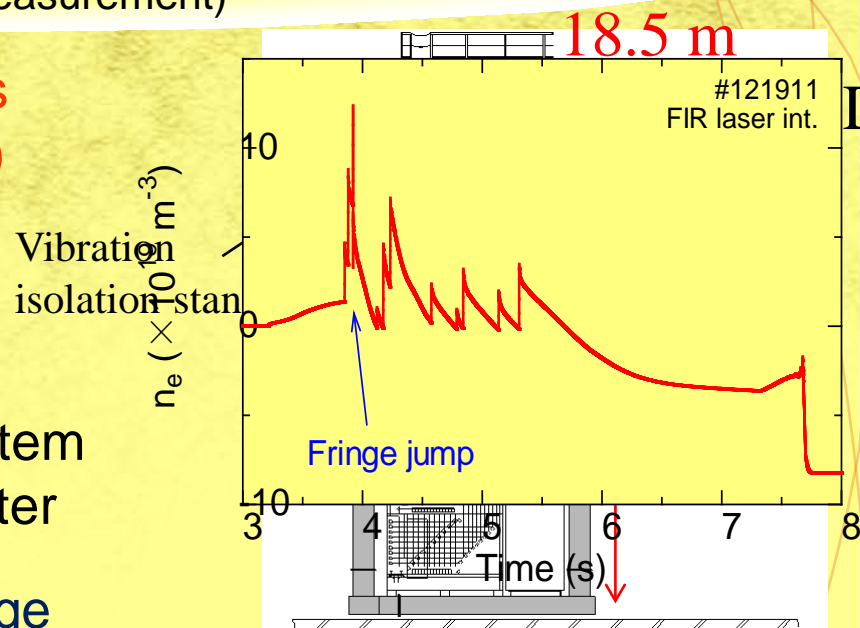
Short-wavelength lasers ( $57\ \mu\text{m}$ ,  $10\ \mu\text{m}$ )

One of the fundamental solutions is a **Dispersion Interferometer (DI)**

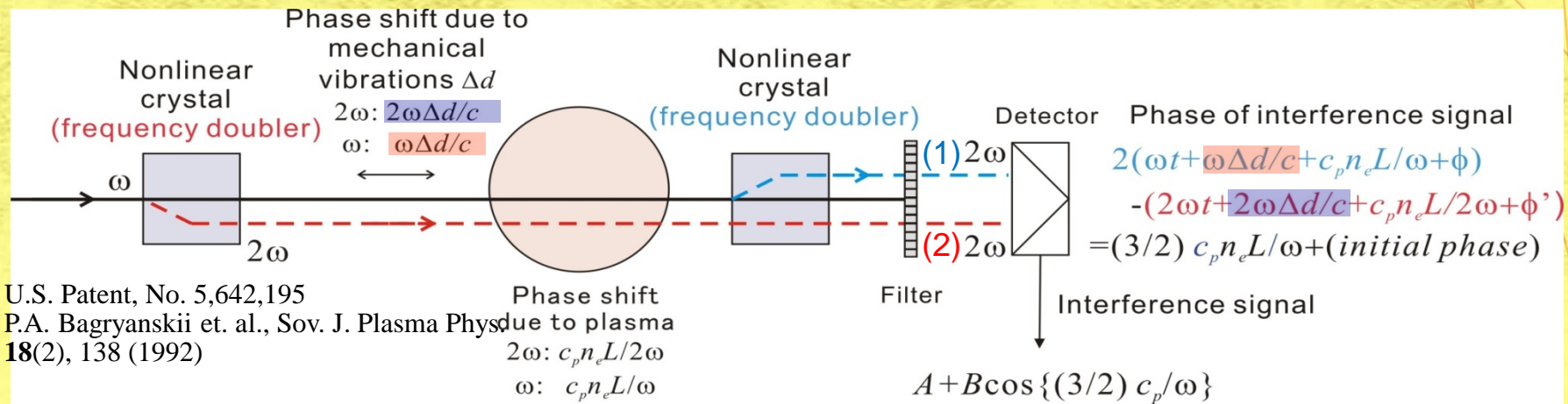
V. P. Drachev *et. al.*, RSI **64** 1010 (1993)., P. A. Bagryansky *et. al.*, RSI **77** 053501 (2006).

**low sensitivity to vibrations, no fringe jumps** (by selecting appropriate wavelength)

**DI is attractive for high density, large and steady-state fusion devices**



# 2. Principle of Basic Dispersion Interferometer (DI)



## Phases of 2nd harmonic beams

$$(1): 2(\omega t + \omega \Delta d / c + c_p \bar{n}_e L / \omega + \phi_1) \equiv \phi_1$$

$$(2): 2\omega t + 2\omega \Delta d / c + c_p \bar{n}_e L / (2\omega) + \phi_2 \equiv \phi_2$$

( $c_p$ : Constant)

## Interference signal between two 2nd harmonics

$$I = A + B \cos(\phi_1 - \phi_2) = A + B \cos\left(\frac{3}{2} \frac{c_p \bar{n}_e L}{\omega} + \phi\right)$$

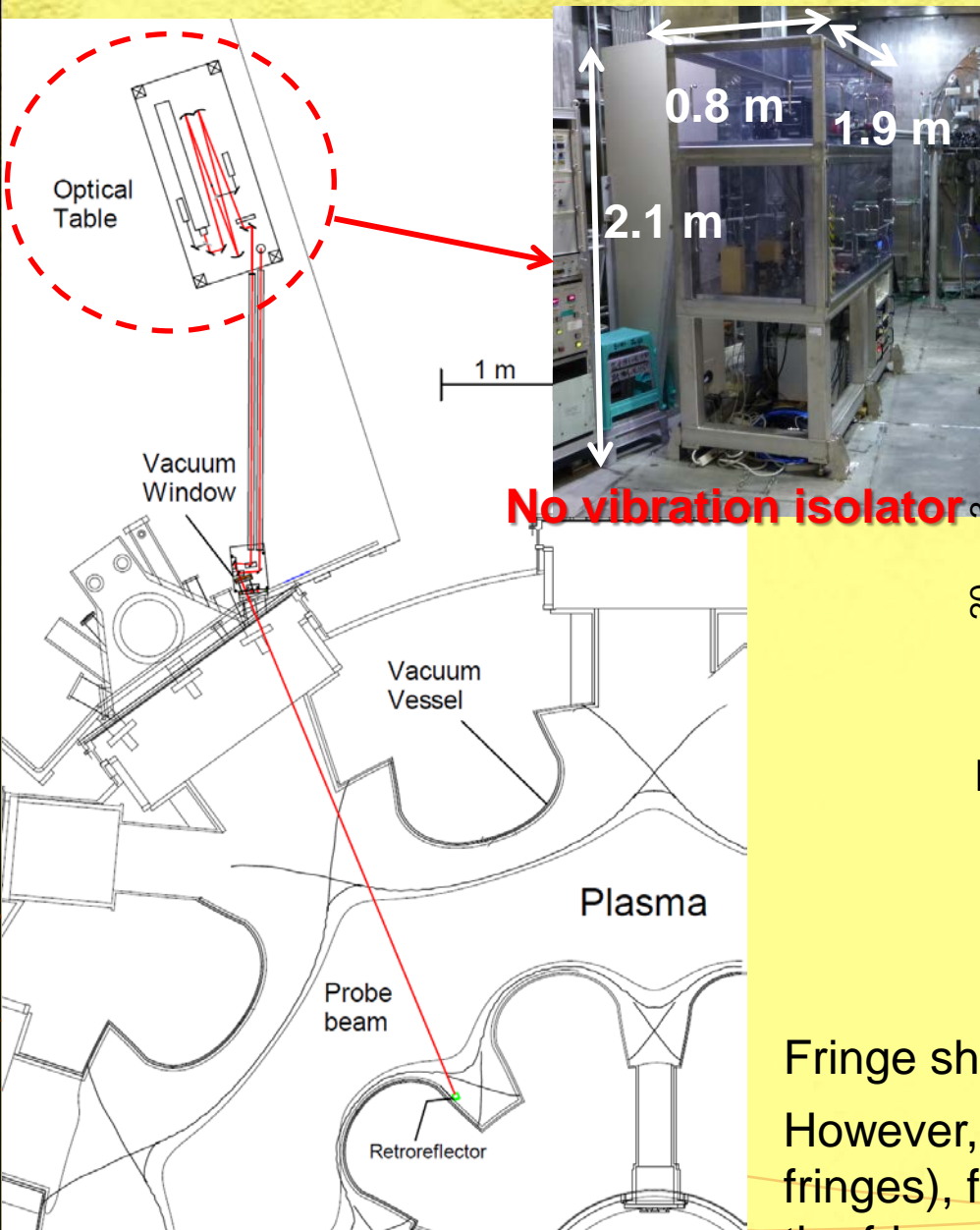
$$A = I_1 + I_2, B = 2\sqrt{I_1 I_2}$$

$I_1, I_2$ : intensities of 2nd harmonics

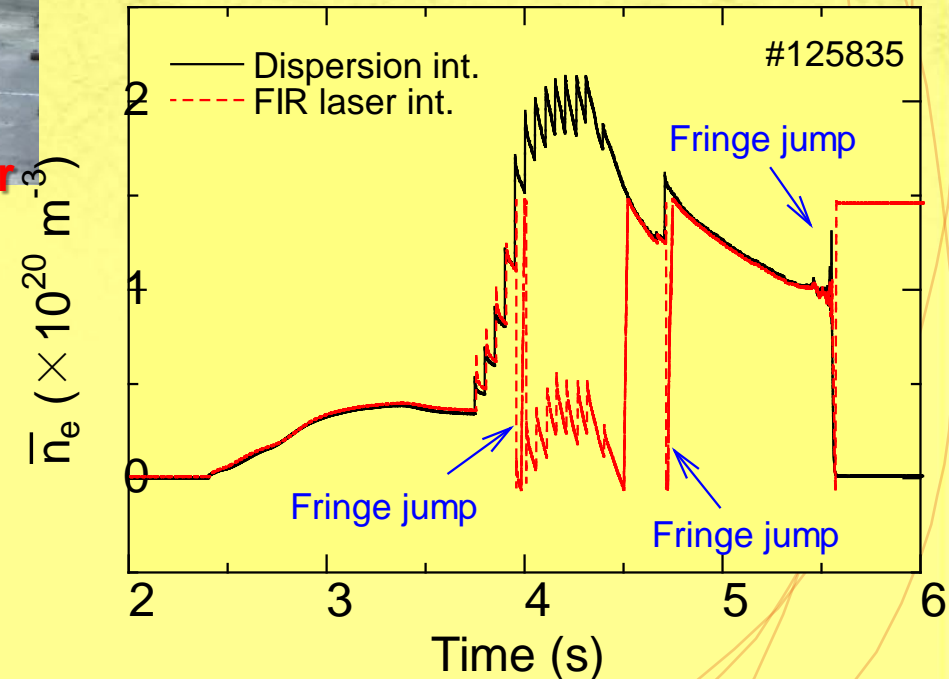
$\phi$ : initial phase

**Phases due to mechanical vibrations are cancelled automatically and only those due to plasma dispersion remain in the interference signal.**

# 3. CO<sub>2</sub> laser (10 μm) DI on LHD



- Line density resolution on LHD:  
 $8 \times 10^{17} \text{ m}^{-2}$  ( $2.5 \times 10^{17} \text{ m}^{-3}$ ) for 3000 s  
 $4 \times 10^{17} \text{ m}^{-2}$  ( $1.3 \times 10^{17} \text{ m}^{-3}$ ) for 100 s
- Temporal resolution: 100 μs
- Latency: 100 μs



Fringe shift @ 10.6 μm > 1 fringe: risk of fringe jump  
 However, number of fringe shift is small (~ 3 fringes), fast sampling (100 kHz on LHD) can track the fringe shift and can avoid the fringe jumps.

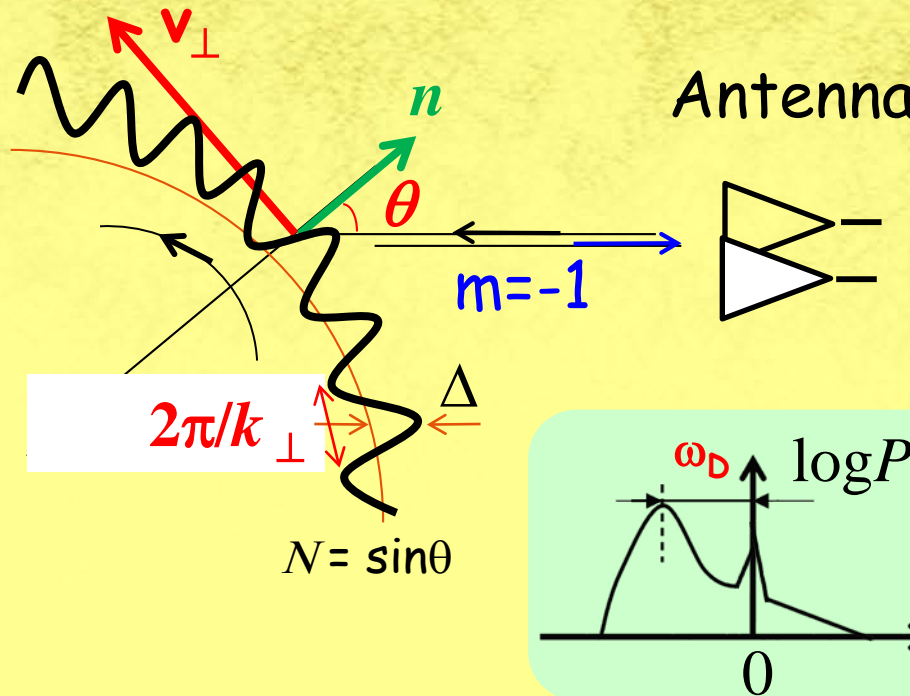
# Contents

- はじめに
- 干渉計
  - マイクロ波干渉計、FIRレーザー干渉計、分散干渉計
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- 協同トムソン散乱
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# Doppler Reflectometer

Plasma



- wave vector is selected via Bragg condition :

$$k_{\perp} = 2 \cdot k_0 \sin(\theta)$$

- k-spectral resolution is defined by beam width :

$$\Delta k_{\perp} = \frac{2\sqrt{2}}{w} \sqrt{1 + \left( \frac{w^2 k_0}{\rho_{eff}} \right)^2}$$

- Doppler Shift:

$$\omega_D = -\mathbf{k} \cdot \mathbf{v}$$

$$\approx -k_{\perp} v_{\perp}$$

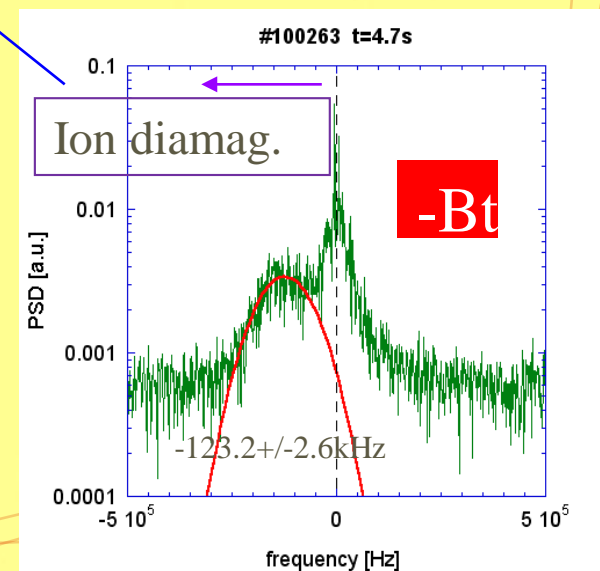
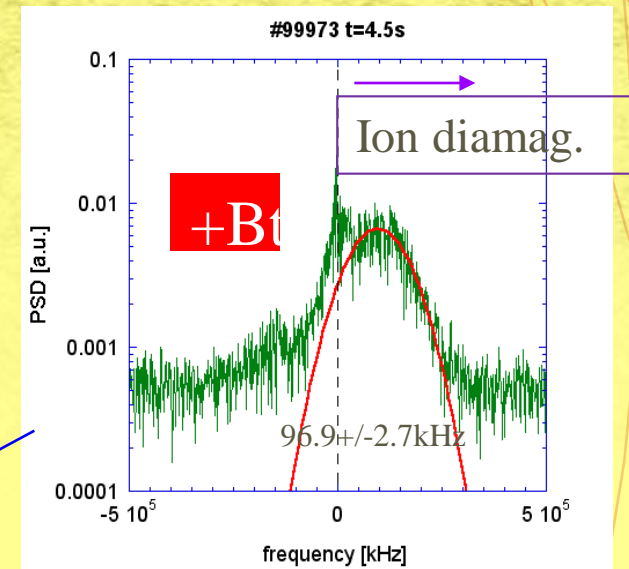
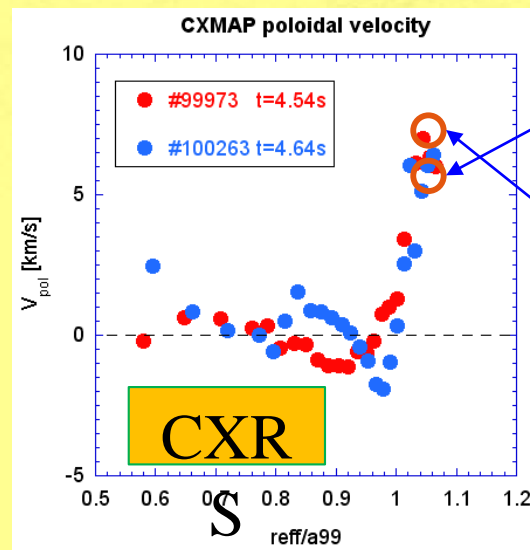
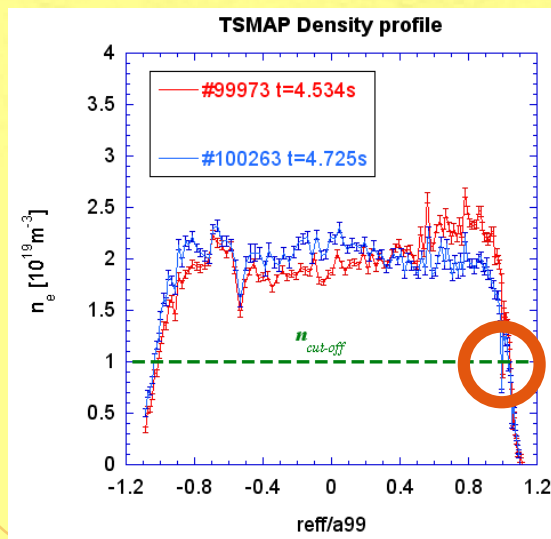
$$v_{\perp} = v_{phase} + v_{E \times B}$$

## strong points

- Observation wave number is selectable in ITG/TEM turbulence region.
- No request for special heating operation

# Example of Doppler RM measurement (Comparison of regular & reverse magnetic field direction)

- When the direction of magnetic field is inverted, the sign of Doppler shift frequency is also changed.



- #99973  $5.8 \pm 0.1 \text{ km/s}$
- #100263  $7.2 \pm 0.1 \text{ km/s}$

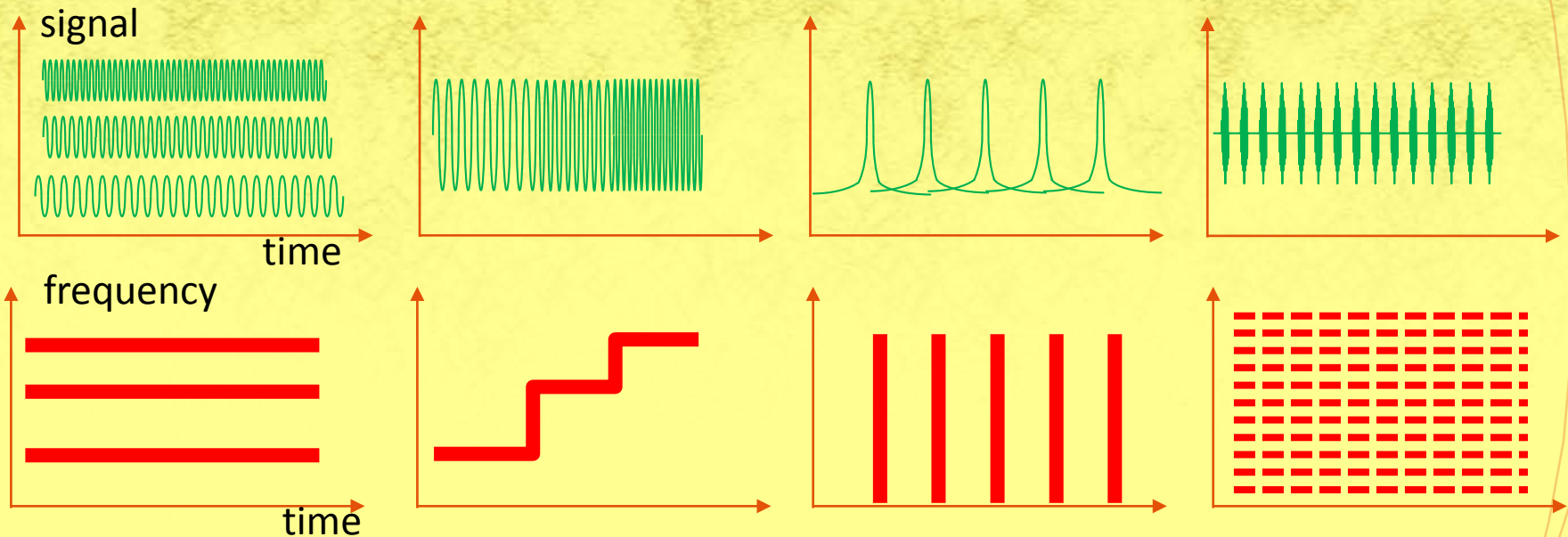
# How to make “multi-frequency channel” ?

Fixed-freq. multi source

Freq. Hopping

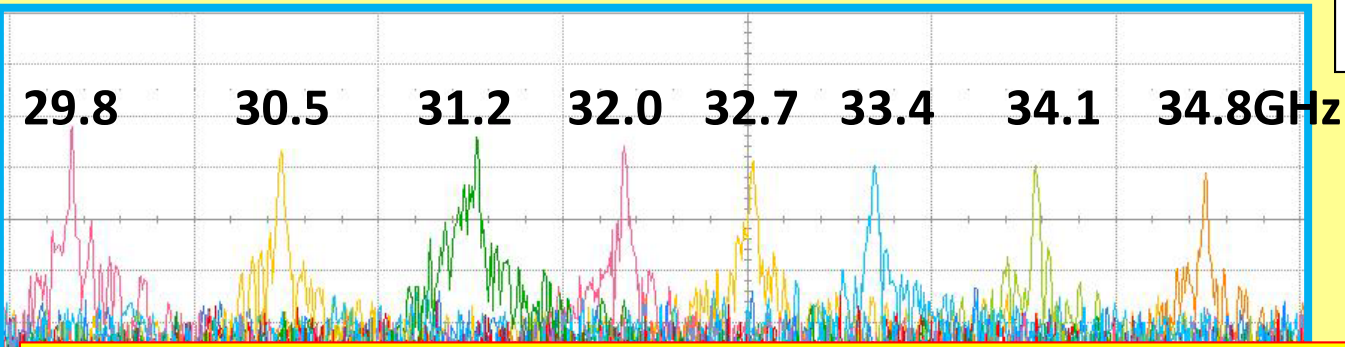
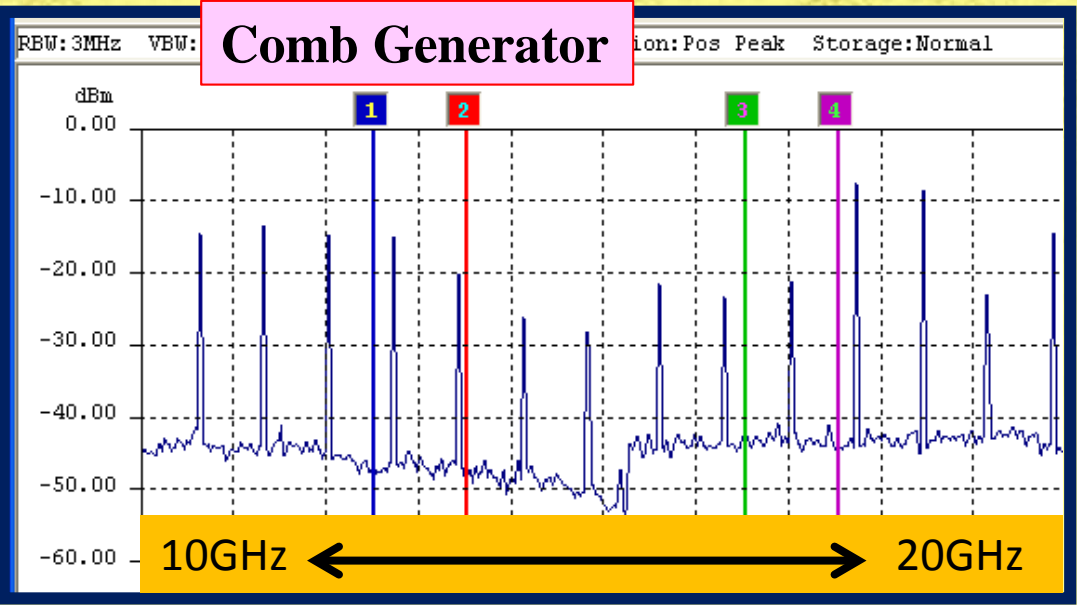
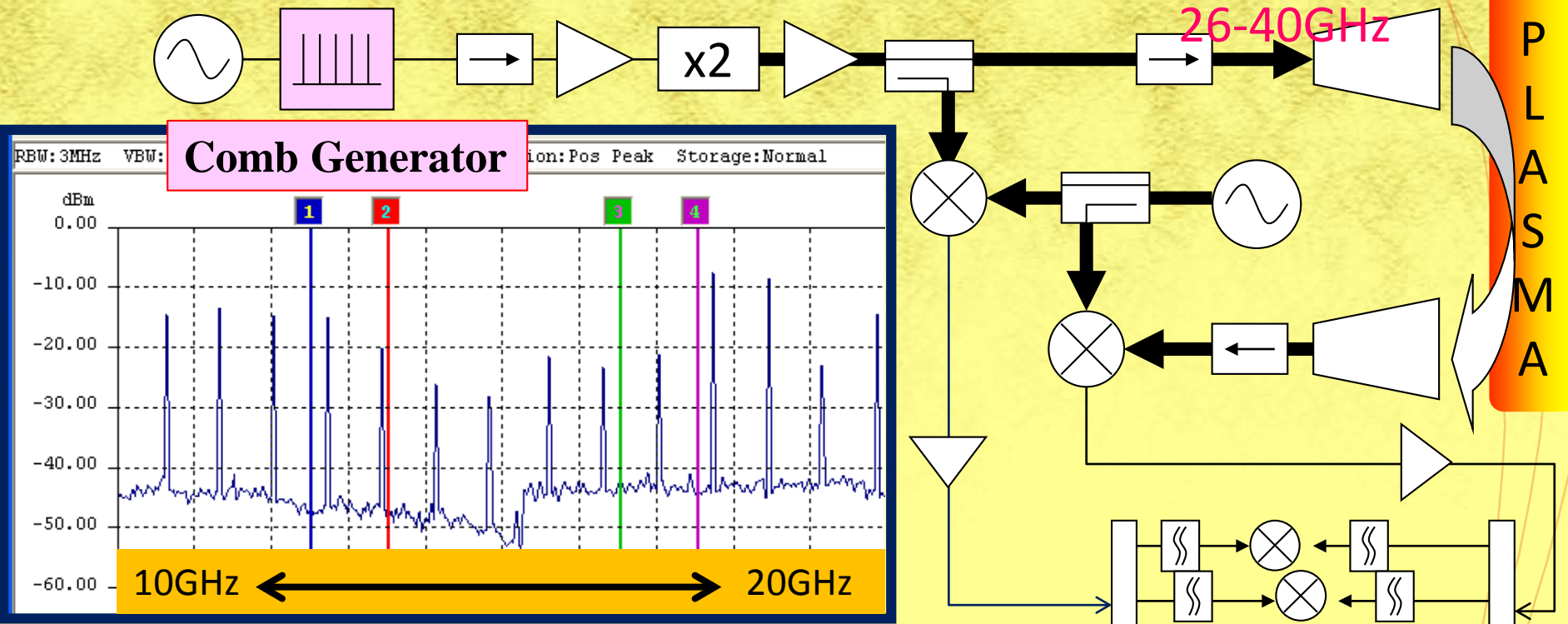
Ultrashort pulse

Frequency COMB



✓ “**Simultaneous**” measurement for studying the spatio-temporal behavior

# ka-band 7ch frequency comb reflectometer in LHD

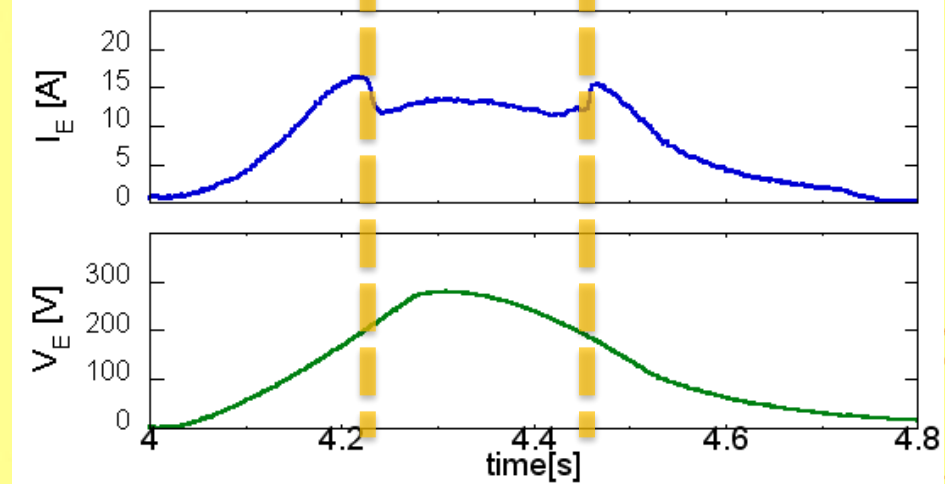
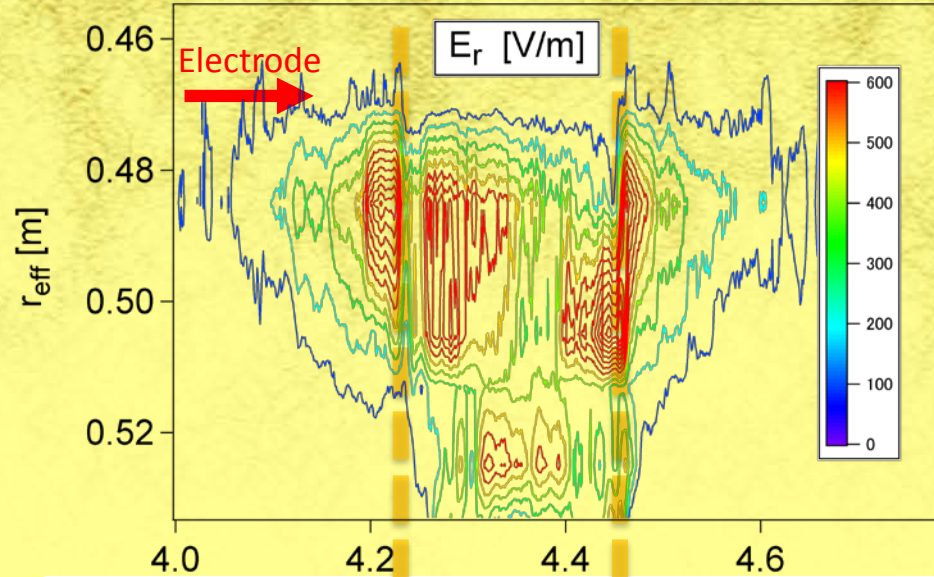
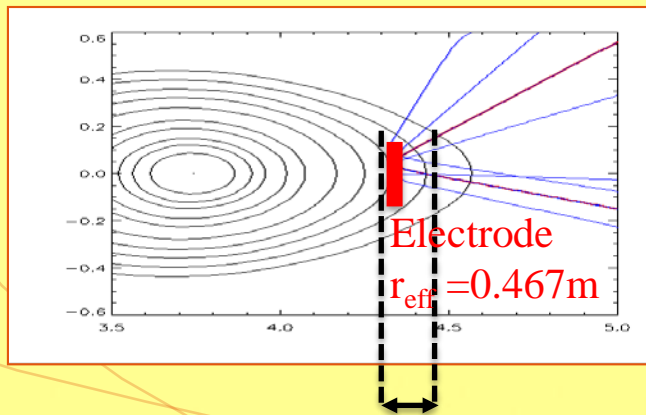
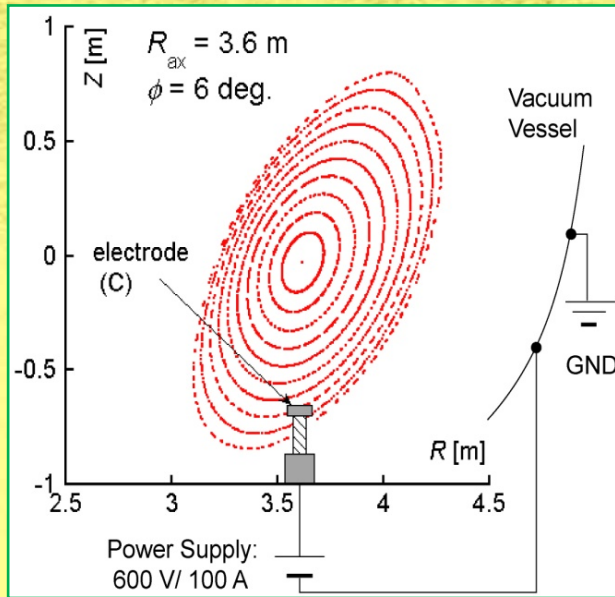


**ka-band (26-40GHz) every 0.7GHz → 20 peaks → Filter bank system (7ch)**

up to 20ch



# Radial electric field $E_r$ is controlled by the biasing electrode



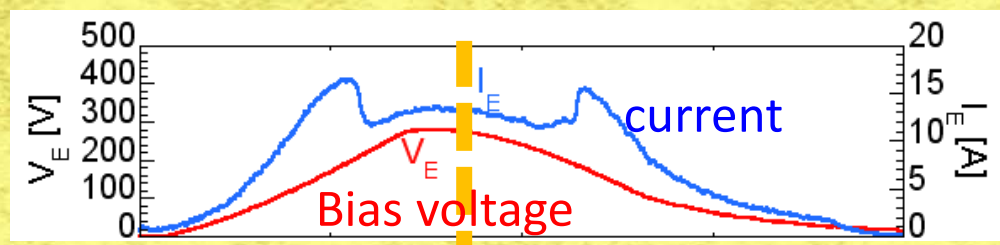
ECH: 0.8 MW Reflectometer

$r_{eff} \sim 0.45 \sim 0.53 \text{ m}$

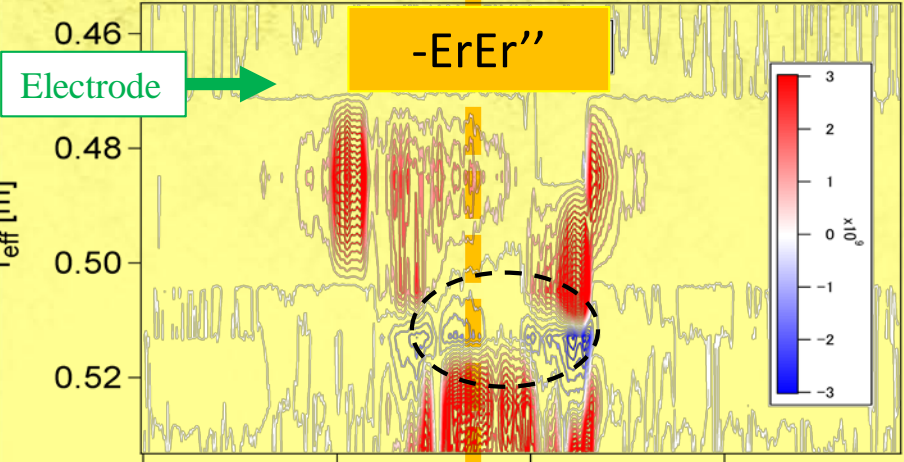
$a_{99} \sim 0.58 \text{ m}$

Strong  $E_r$  region jump outwards during ramp-up of bias voltage

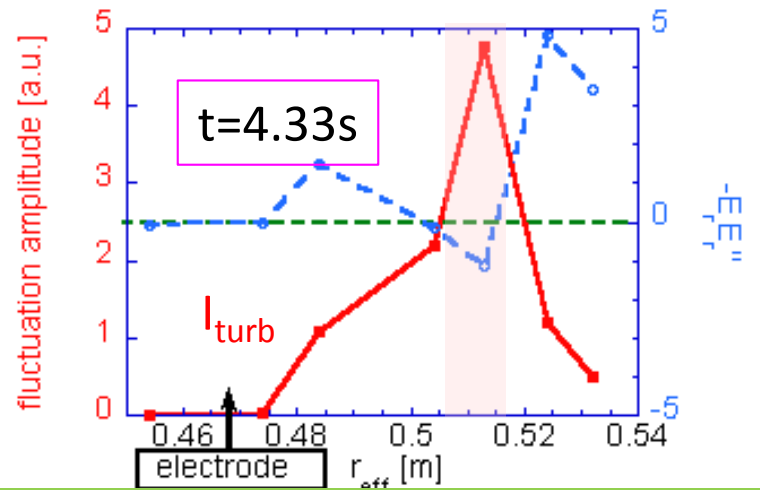
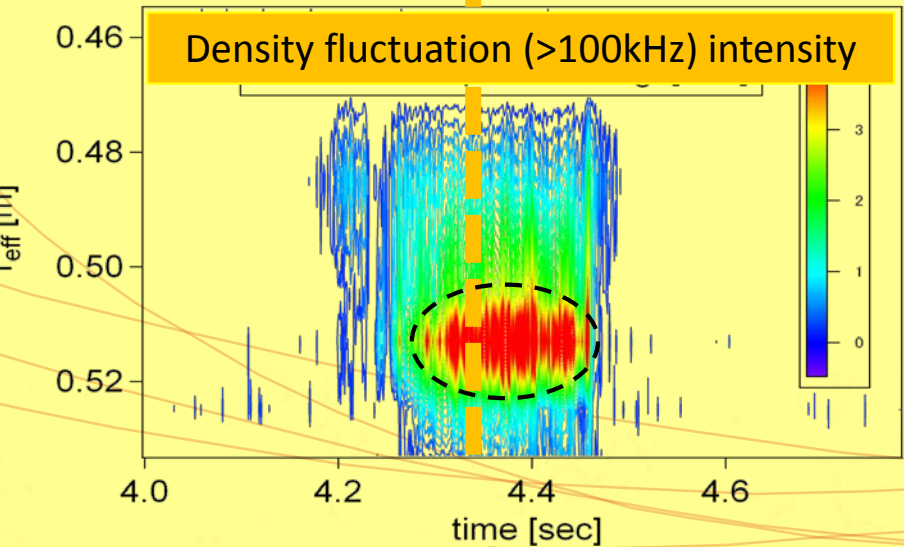
# Turbulence intensity correlates with $-Er Er''$



- The turbulence intensity enhanced in the region where  $-Er Er'' < 0$ .
- The turbulence intensity does not correlate with  $Er'$ .
- The results are not conflicted with the theory on the importance of  $-Er Er''$ .



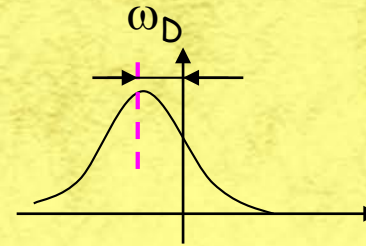
$$\frac{\partial I}{\partial t} = \gamma I - \omega_2 I^2 - \alpha(-E_r E_r'') I$$



*Meso-scale  $Er [Er'']$  is important for turbulence reduction*

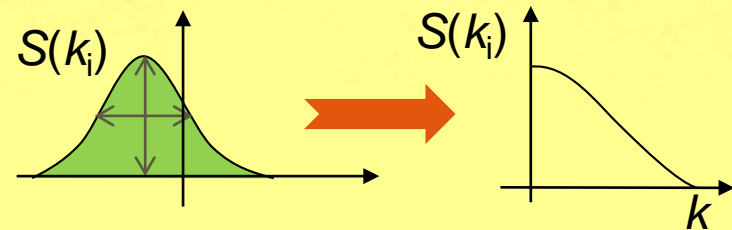
# Target parameters of Doppler RM

- ① Doppler shifted frequency  
→ poloidal velocity

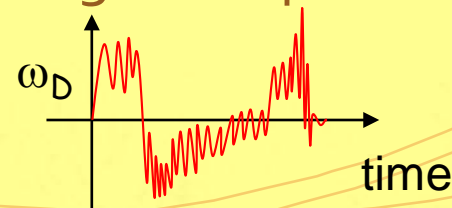


$$\omega_D = -\mathbf{k} \cdot \mathbf{v}$$
$$\approx -k_{\perp} v_{\perp}$$

- ② Integration in frequency domain  
→ wave number spectrum

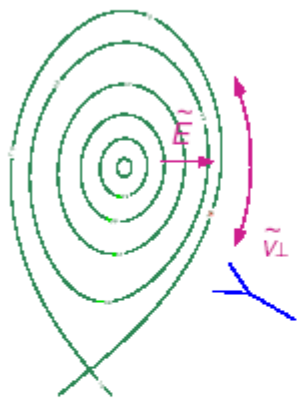


- ③ Temporal behavior of Doppler shift frequency  
→ velocity / frequency of background plasma (zonal flow, GAM, etc.)

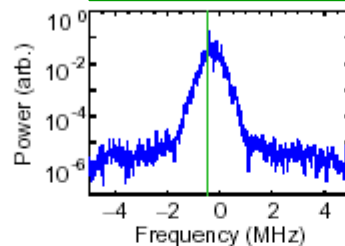


# ゾーナル流(GAM)計測

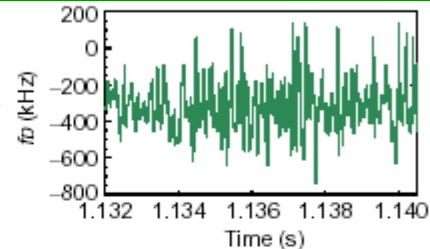
## Geodesic Acoustic Modes



周波数スペクトル



ドップラーシフトした周波数の時間変化

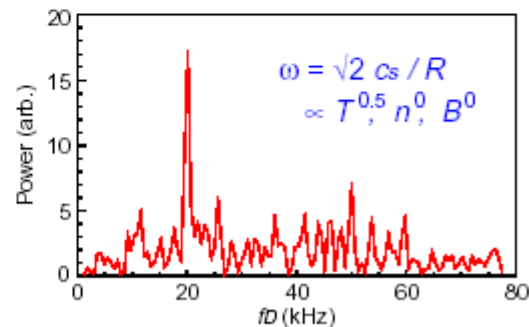


56GHz x-mode Doppler refl.

• Ohmic shot #16179  
 $\rho \sim 0.98$ ,  $T_e \sim 120\text{eV}$

FFT

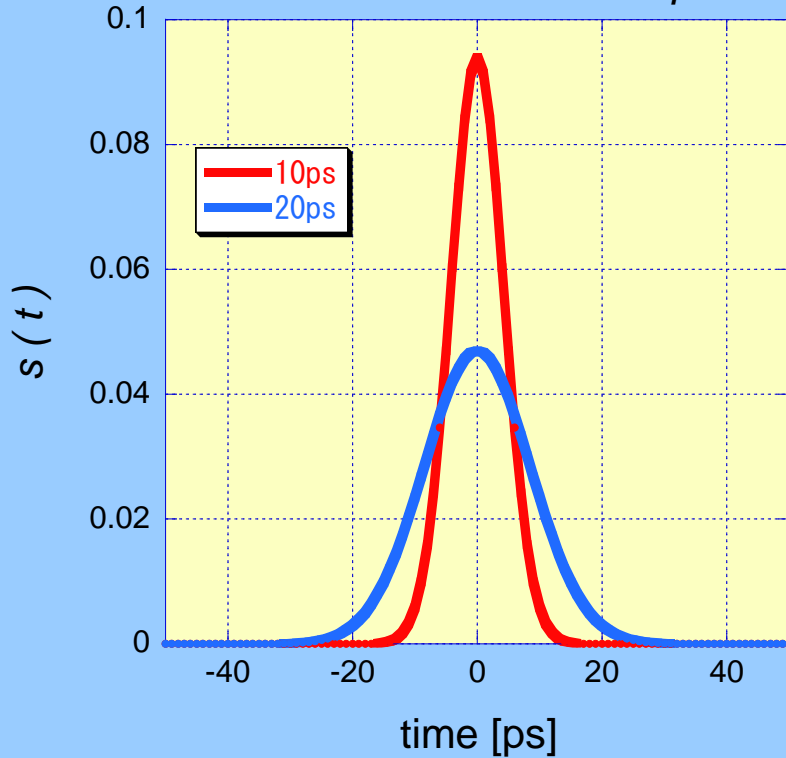
- Electrostatic (low  $m$ ) acoustic mode, i.e.  $\tilde{B} = 0$
- Low frequency. Large  $\tilde{E}$ , even for small  $\tilde{n}$
- Mechanism  
 $\tilde{E} \rightarrow \tilde{v}_\perp = \tilde{E} \times \mathbf{B} / B^2$  and  $\tilde{n} \propto -\nabla \cdot \tilde{v}_\perp$   
 $\tilde{n} \rightarrow \tilde{J} = B \times \nabla \tilde{n}$  which transports charge  
 $\rightarrow$  acts against  $\tilde{E} \rightarrow$  "poloidal" oscillation
- Linked with zonal flows, predicted by codes



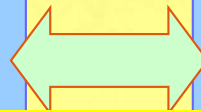
- 背景流 (~ 径電場) の揺らぎを計測。

# Ultrashort Pulse

*Impulse*

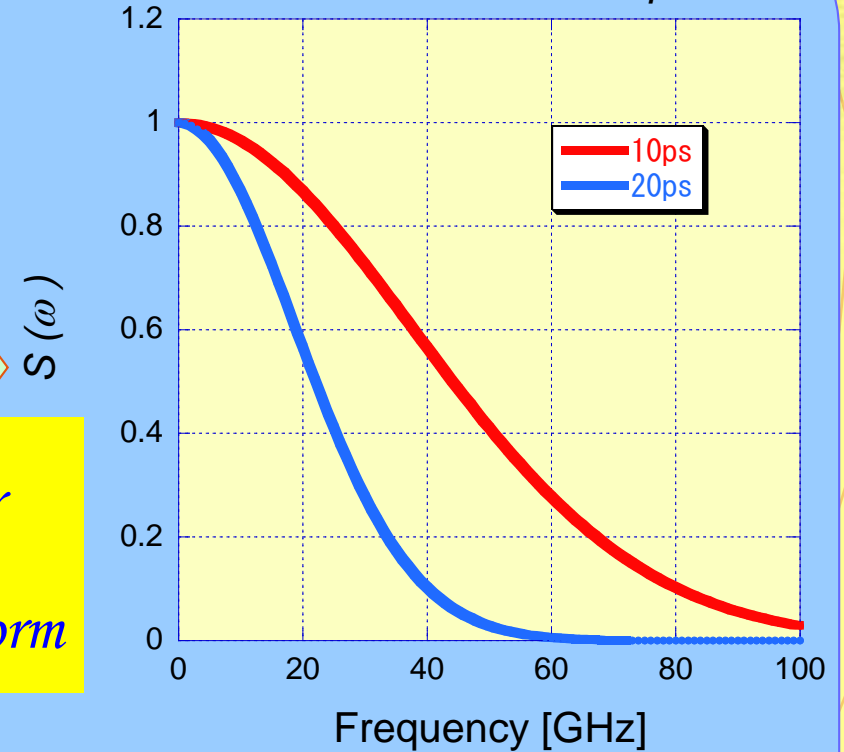


$$s(t) = \frac{1}{\sqrt{2\pi\sigma}} \exp\left(-\frac{t^2}{2\sigma^2}\right)$$



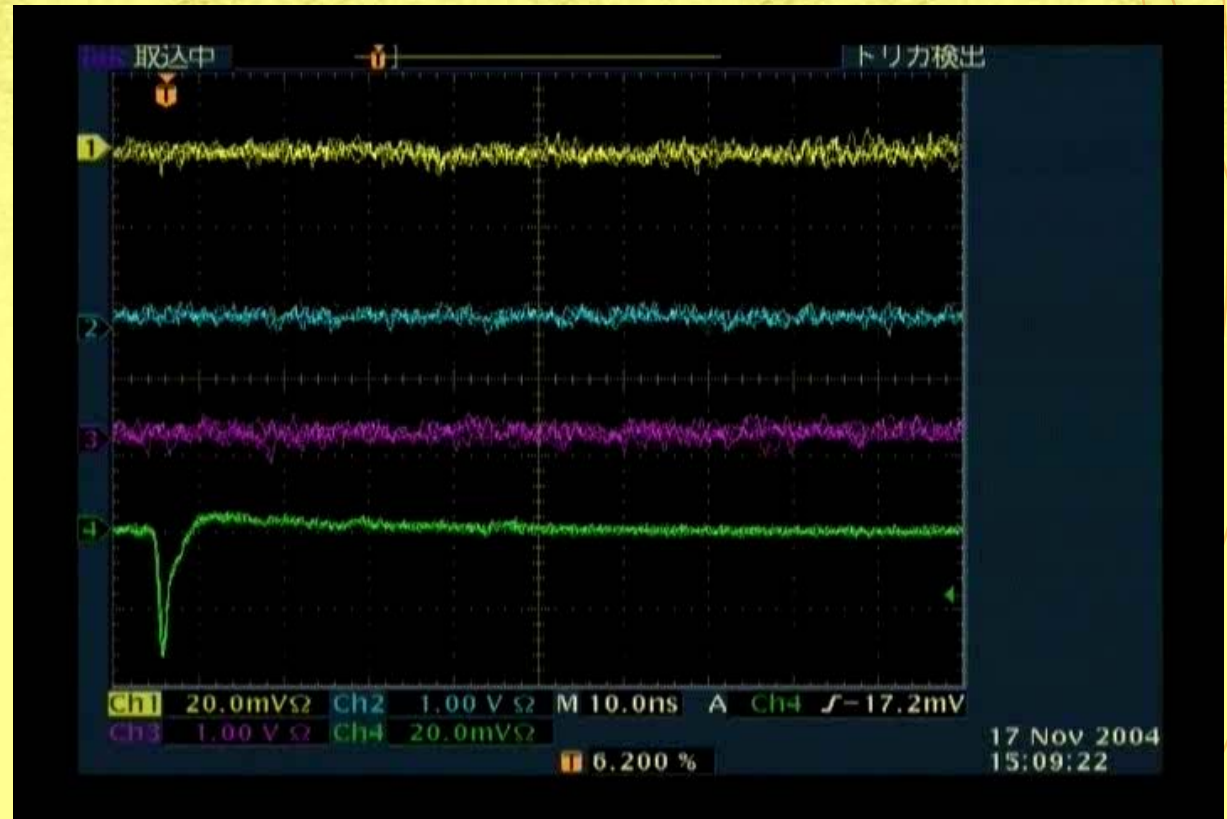
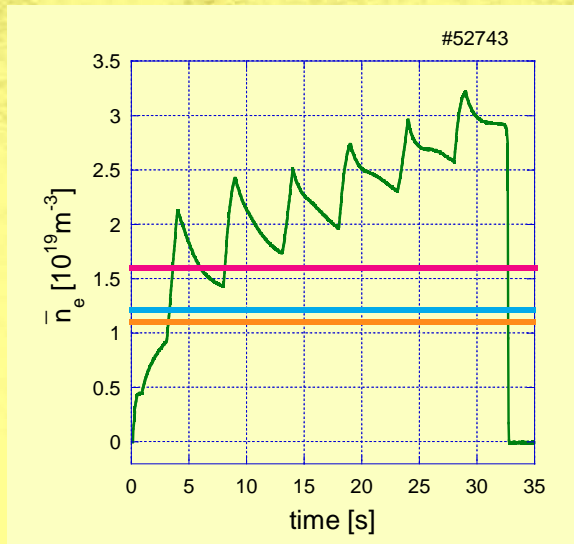
*Fourier  
Transform*

*Spectrum*



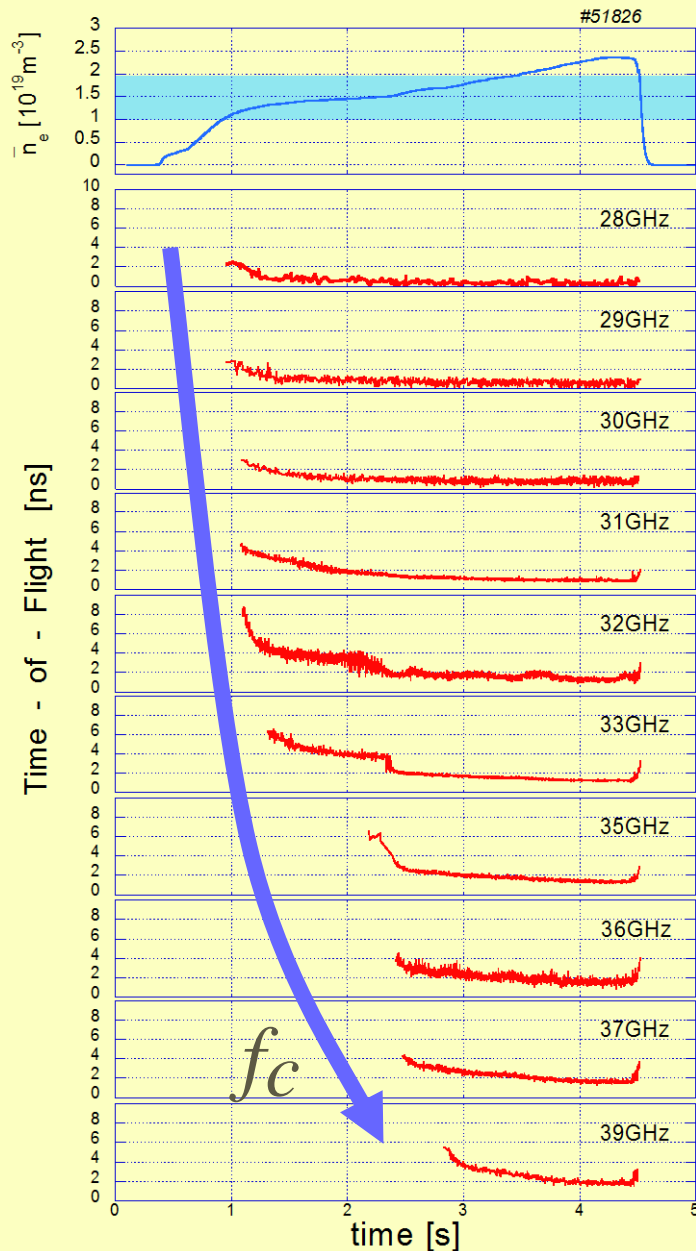
$$S(\omega) = \exp\left(-\frac{\omega^2\sigma^2}{2}\right)$$

# Example of Reflected Signal

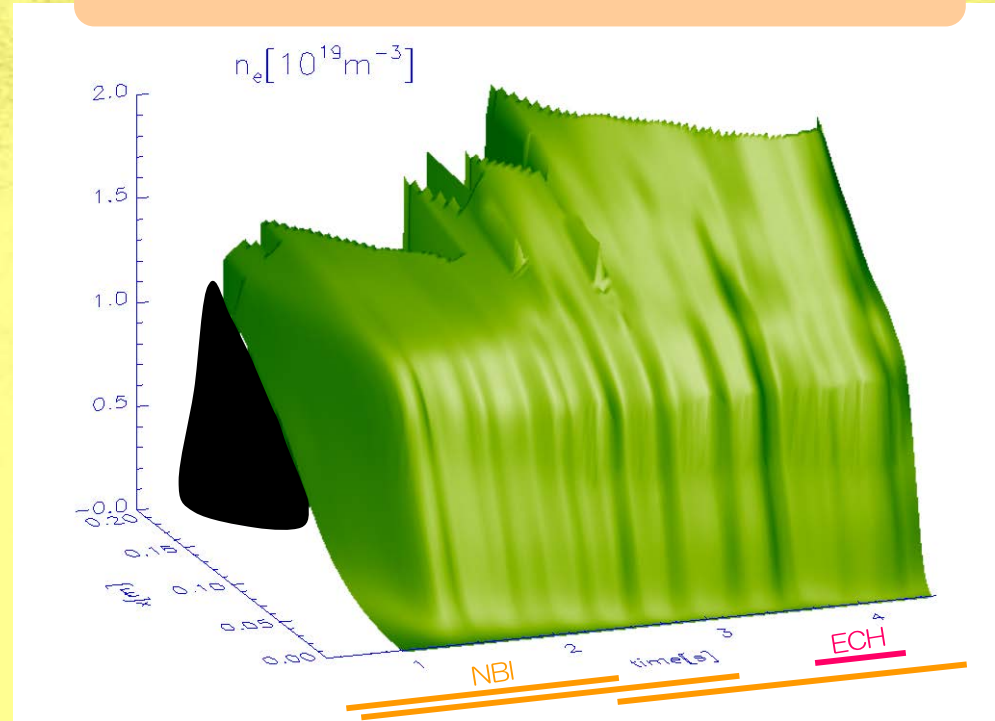


Yellow : 31GHz  
Blue : 32GHz  
Red : 36GHz  
Green : Reference

# Density Profile Measurement

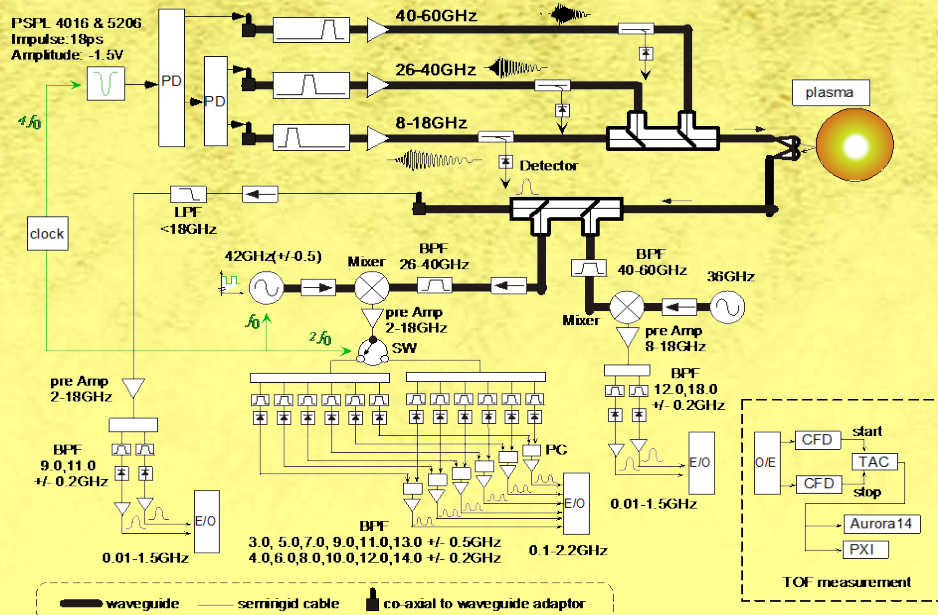


## Reconstructed $n_e$ profile

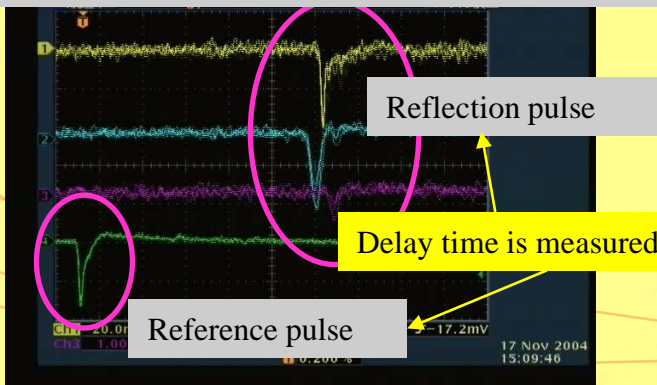
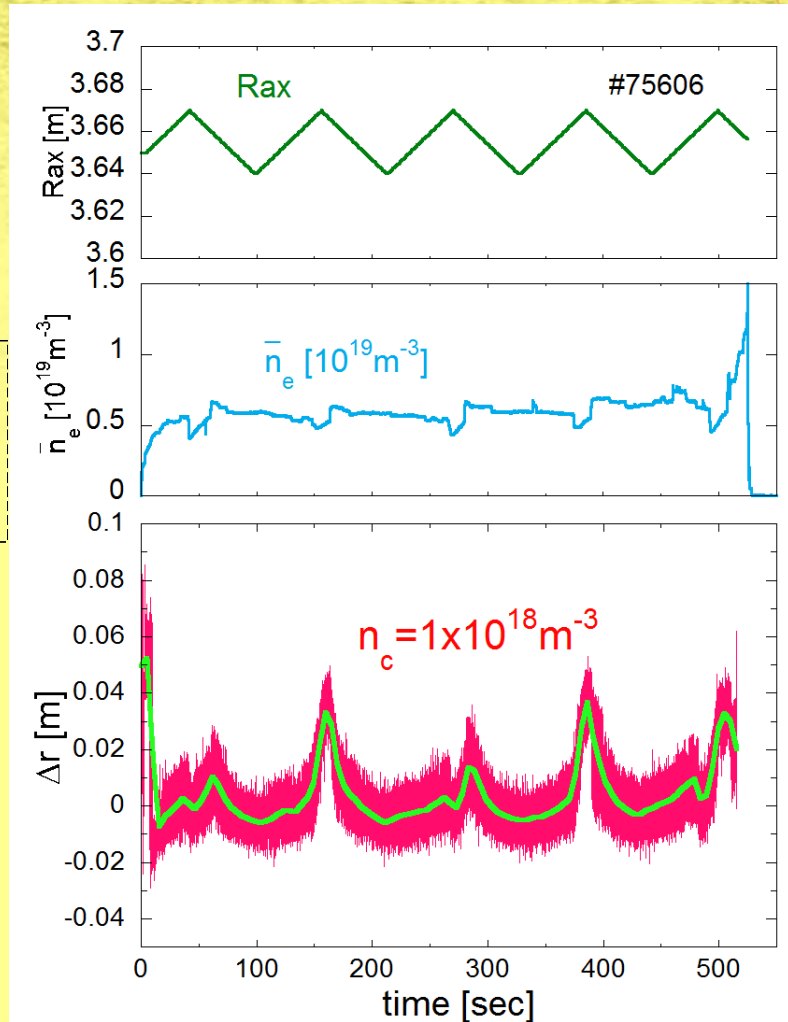


- Here, time-of-flight is defined by the traveling time between plasma edge and each cutoff layer.
- Each reflected pulse is appeared, when the corresponding cutoff layer is generated in the plasma.

# Edge position monitor in LHD



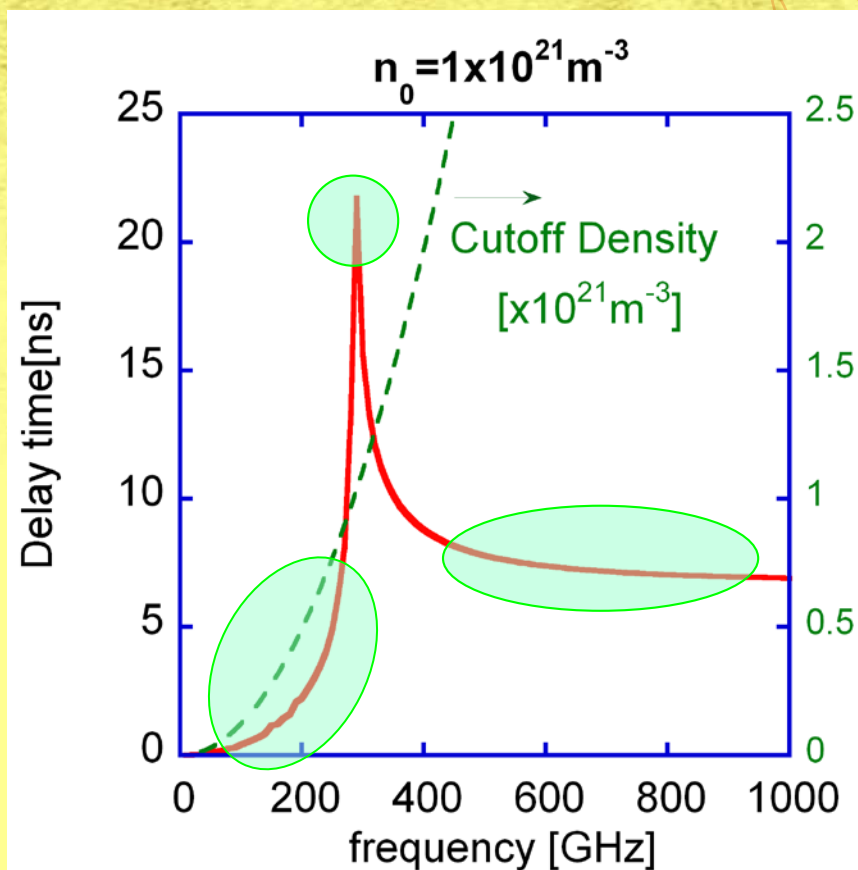
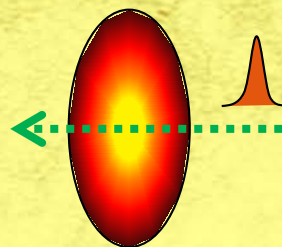
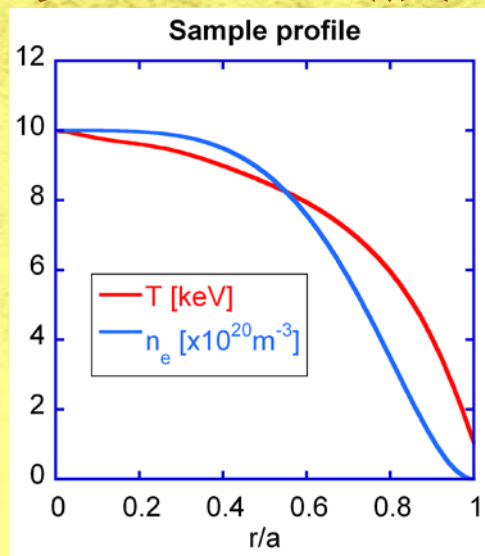
- Impulse (23ps pulse width) is used as a broad band source (8-60GHz).
- Time-of-Flight measurements are done for density profile measurement.



**1x10<sup>18</sup>m<sup>-3</sup>の密度層の位置を  
~500secにわたり、精度<1cmで計測可能**



# テラヘルツ波パルスを用いた計測をする



- カットオフ周波数よりも高いプローブ周波数を用いたDelayometry計測から

➡ **線平均密度**  $\bar{n}_e$

- 広帯域周波数をプローブすることで、Delay timeが最大となる周波数から

➡ **ピーク密度**  $n_{e\_max}$

- 最大カットオフ周波数以下の信号による反射計測から

➡ **密度分布**  $n_e(\rho)$

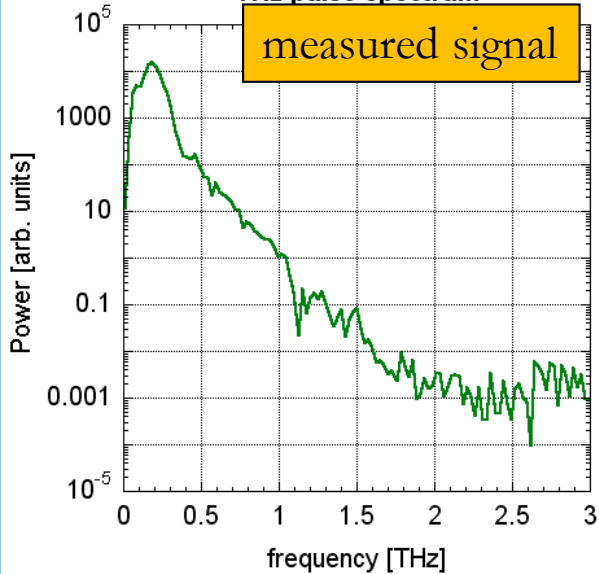
## メリット:

- ・原理的に位相トビがない。
- ・計測値の履歴が不要。
- ➔ **長時間運転時に重要**

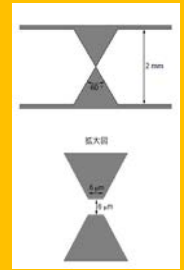
# NIFS THz-TDS system

THz pulse spectrum

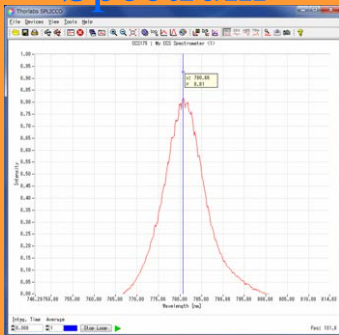
measured signal



Hamamatsu Photonics K.K.  
model: G10620-12 (bow-tie)



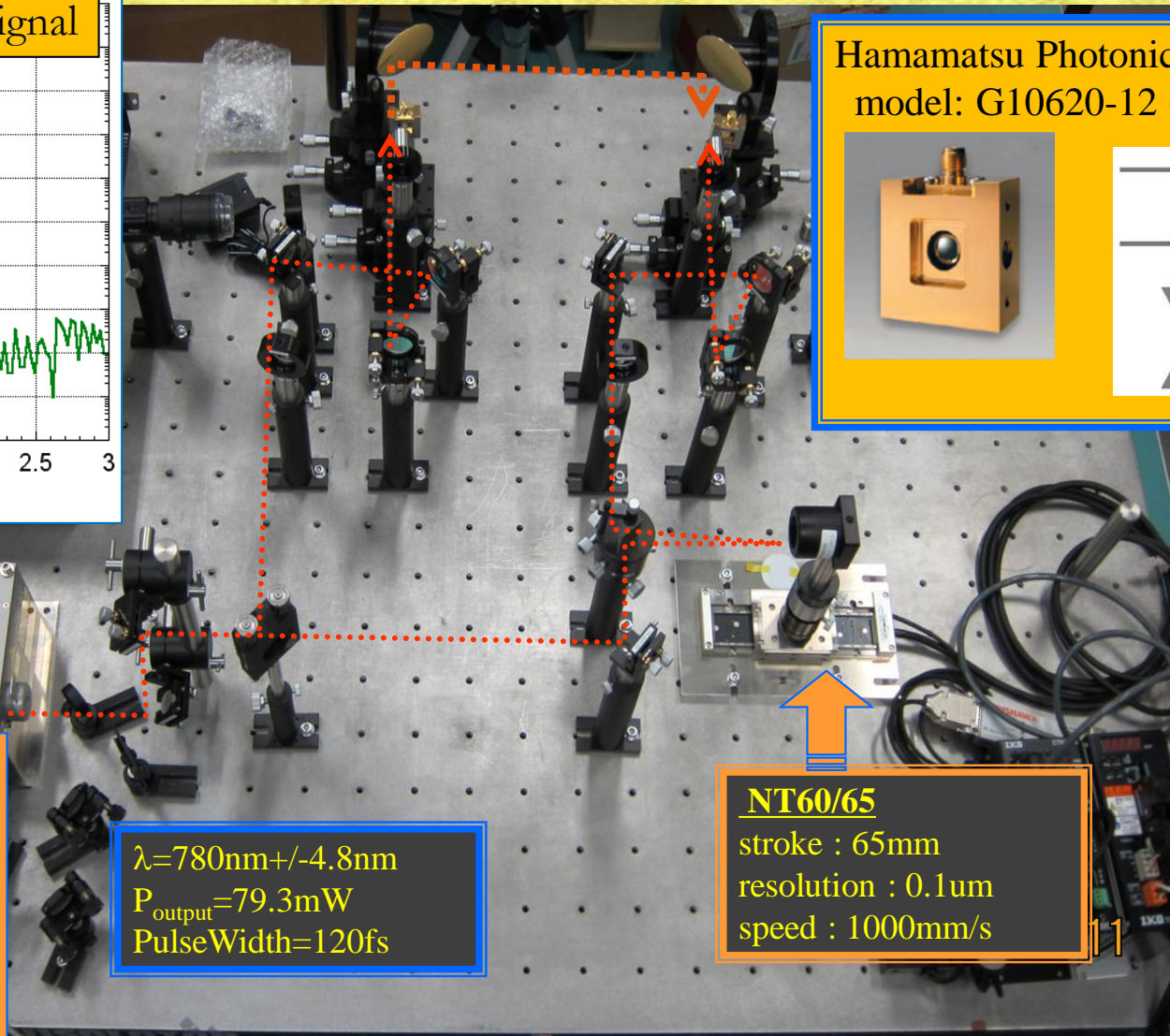
Spectrum



$\lambda=780\text{nm}\pm 4.8\text{nm}$   
 $P_{\text{output}}=79.3\text{mW}$   
PulseWidth=120fs

NT60/65

stroke : 65mm  
resolution : 0.1 $\mu\text{m}$   
speed : 1000mm/s



# Contents

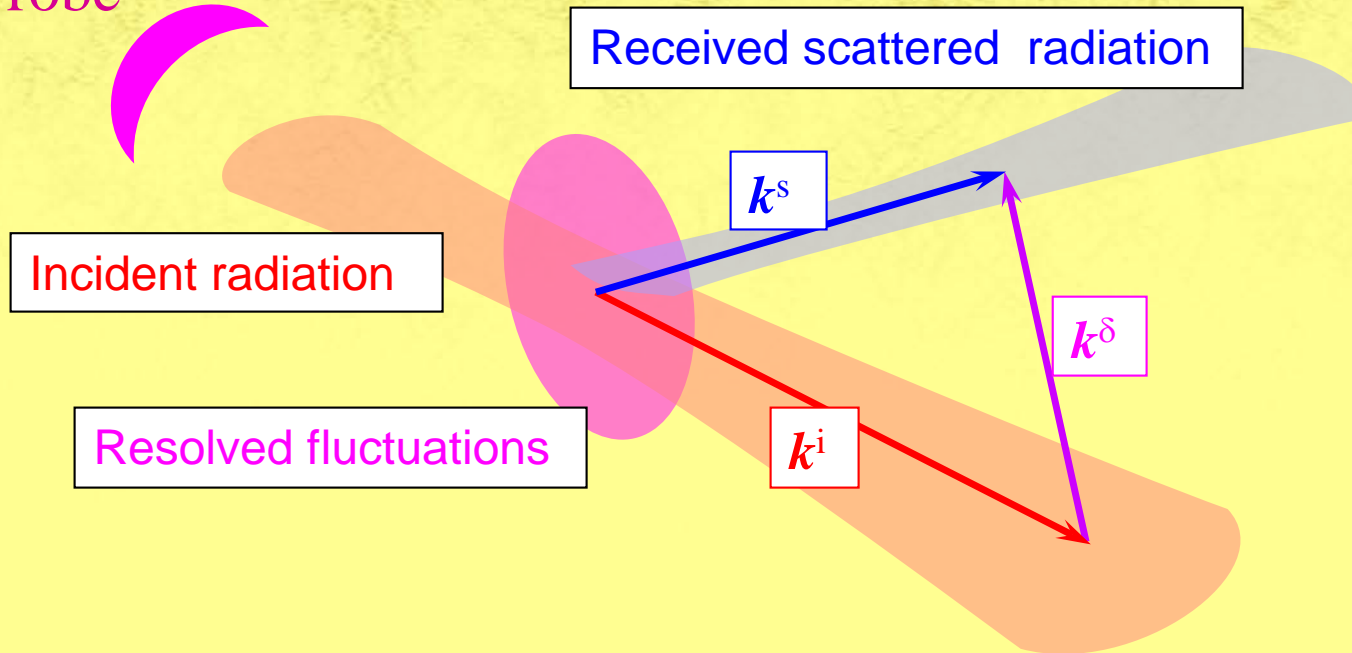
- はじめに
- 干渉計
  - マイクロ波干渉計、FIRレーザー干渉計、分散干渉計
- 反射計
  - ドップラー反射計、パルスレーダー
- 協同トムソン散乱
- まとめ



# Collective Thomson scattering geometry

Probe

Receiver



Collective Thomson scattering resolves velocity component along  $k^\delta$  :

$$f^{(1)}(u) = \int \delta(u - \hat{\mathbf{k}}^\delta \cdot \mathbf{v}) f(\mathbf{v}) d\mathbf{v}$$

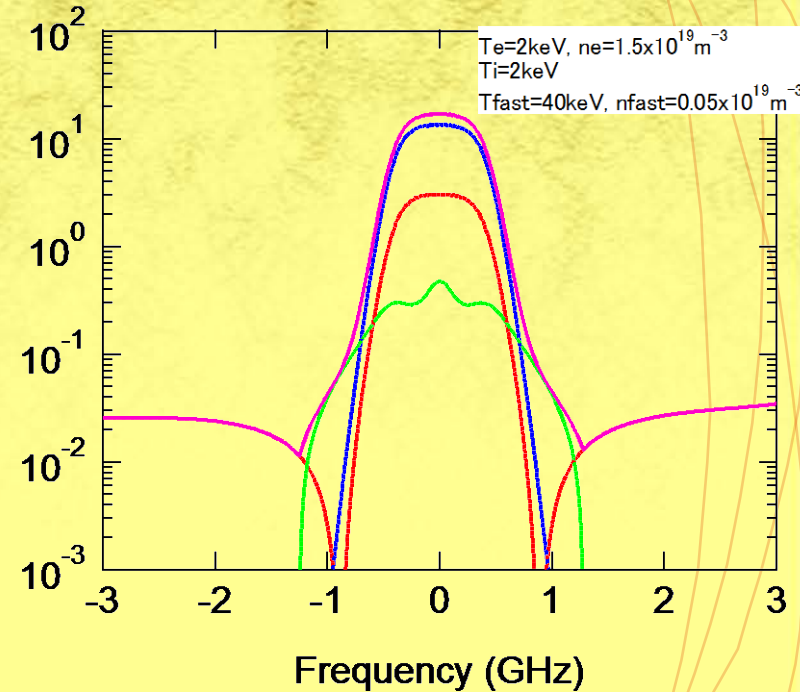
# Feature of CTS spectrum for electrons, ions, and fast ions

- Scattered radiation is written as

$$P_s \propto n_e S(k, \omega) = \text{Electron} + \text{Ion} + \text{Fast Ion}$$

$$S(k, \omega) = \left| 1 - \frac{H_e}{\varepsilon_L} \right|^2 \frac{2\pi^{1/2}}{|k_{\parallel}|v_e} \sum_{l=-\infty}^{\infty} \exp(-k_{\perp}^2 \rho_e^2) I_l(k_{\perp}^2 \rho_e^2) \exp\left(-\frac{(\omega - l\Omega_e)^2}{k_{\parallel}^2 v_e^2}\right) \\ + \left| \frac{H_e}{\varepsilon_L} \right|^2 \frac{2\pi^{1/2} Z_i^2 n_i}{n_e |k_{\parallel}| v_i} \sum_{l=-\infty}^{\infty} \exp(-k_{\perp}^2 \rho_i^2) I_l(k_{\perp}^2 \rho_i^2) \exp\left(-\frac{(\omega - l\Omega_i)^2}{k_{\parallel}^2 v_i^2}\right) \\ + \left| \frac{H_e}{\varepsilon_L} \right|^2 \frac{2\pi Z_{ene}^2 n_{ene}}{n_e |\vec{k}| v_{ene}} f_{ene}^{(1)}\left(\frac{\omega}{k}\right)$$

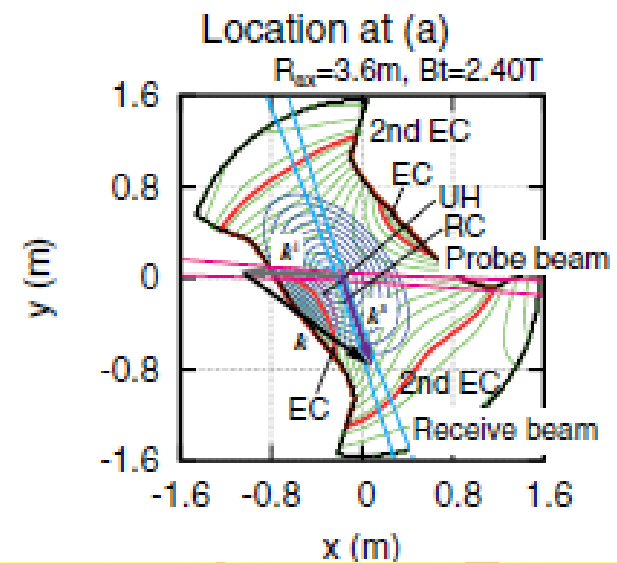
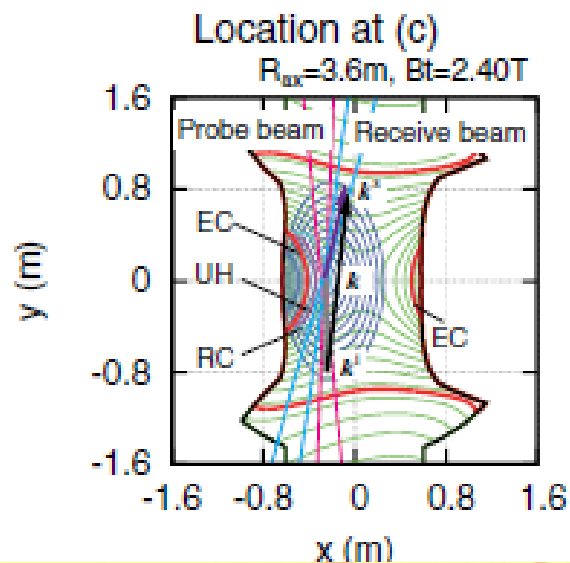
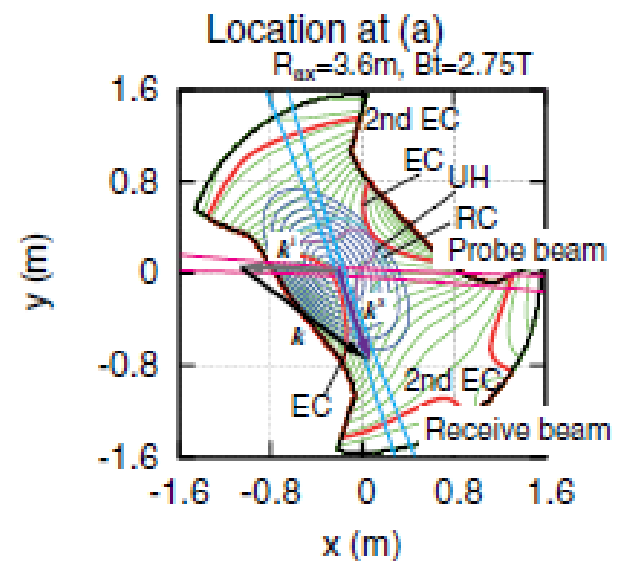
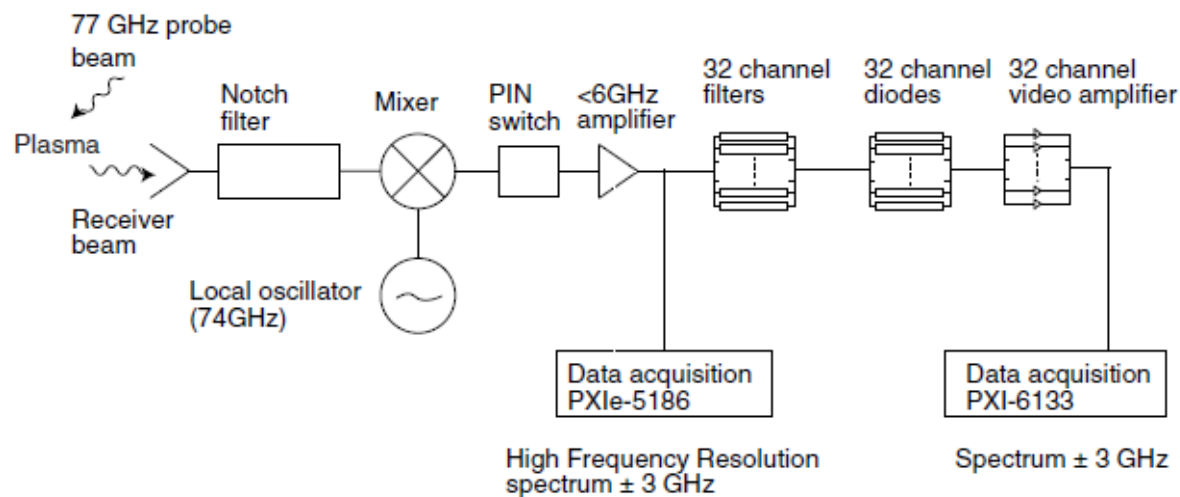
Scattered radiation (eV)



In collective regime, the CTS spectrum spread is dominated by the ion feature.

Measured frequency shift corresponds to the charged particle velocity.

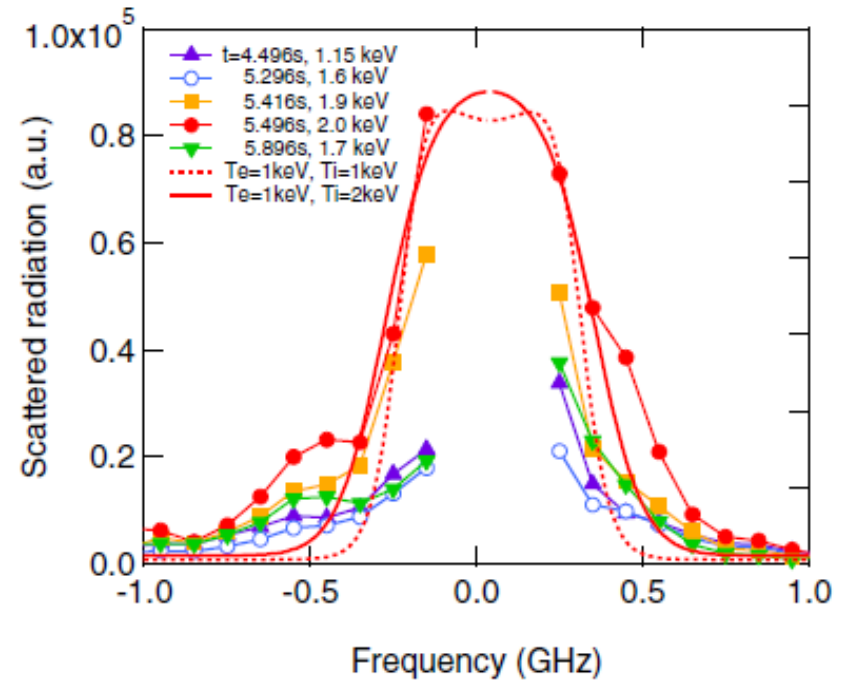
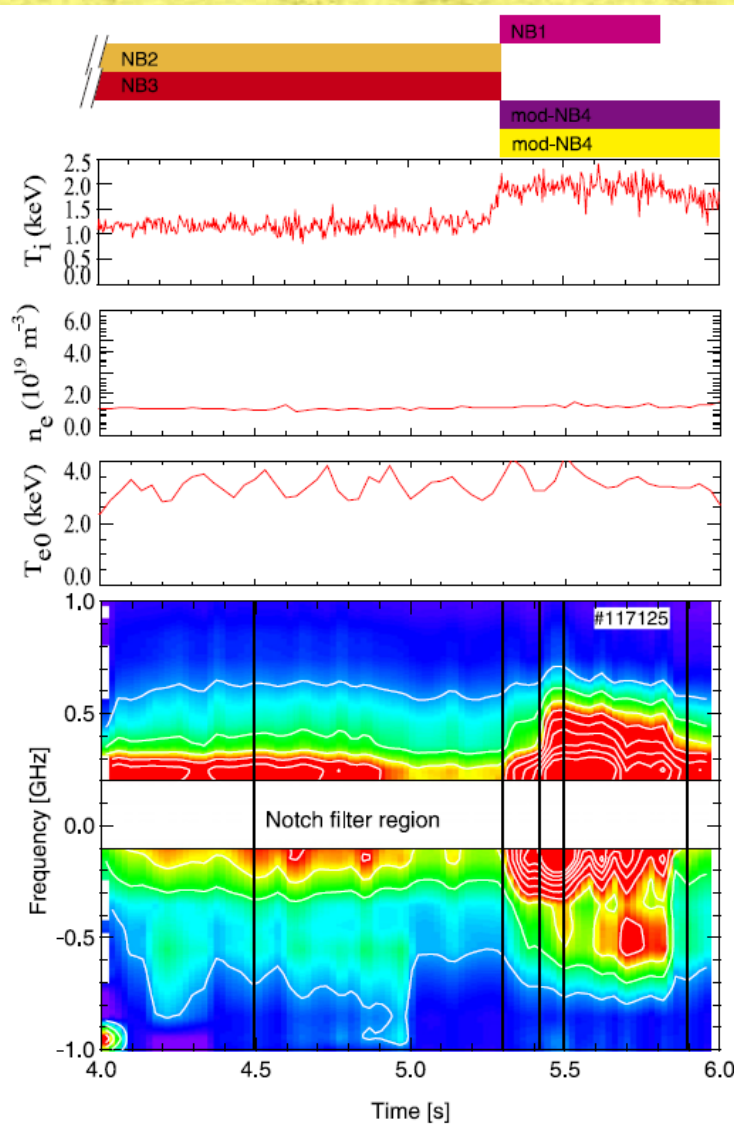
The distribution function is obtained from measured CTS spectrum.



# Measured CTS spectrum during NB injection

M. Nishiura *et al*

Nucl. Fusion 54 (2014) 023006



**Figure 10.** Measured CTS spectrum in the bulk-ion region. The measured  $T_i$  from Ar Doppler broadening is indicated for each time trend. The calculated CTS spectra are denoted by the dotted and the solid curves for  $T_e = 1$  keV and  $T_i = 1$  and 2 keV, respectively.

# IBW in TEXTOR (CTS)

S. B. Korsholm, PRL 106, 165004 (2011)

calculation

experiment

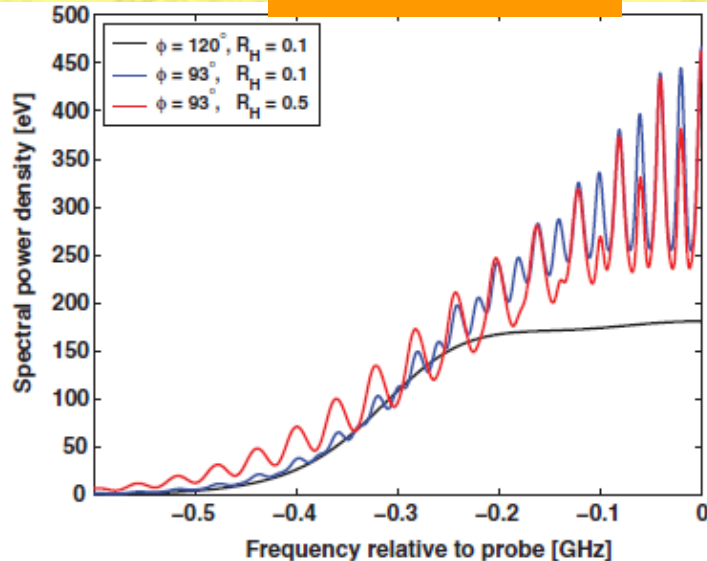


FIG. 1 (color). Calculated CTS spectra for a geometry with  $\mathbf{k}^\delta$  close to perpendicular to  $\mathbf{B}$ ,  $\phi = 93^\circ$  in a typical TEXTOR plasma for  $R_H = 0.1$  (blue) and  $R_H = 0.5$  (red). For comparison a calculated CTS spectrum for  $\phi = 120^\circ$  (black) and  $R_H = 0.1$ .

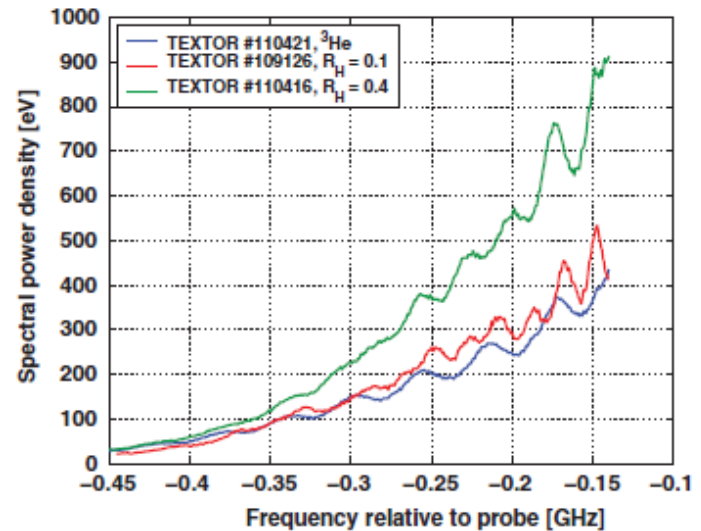
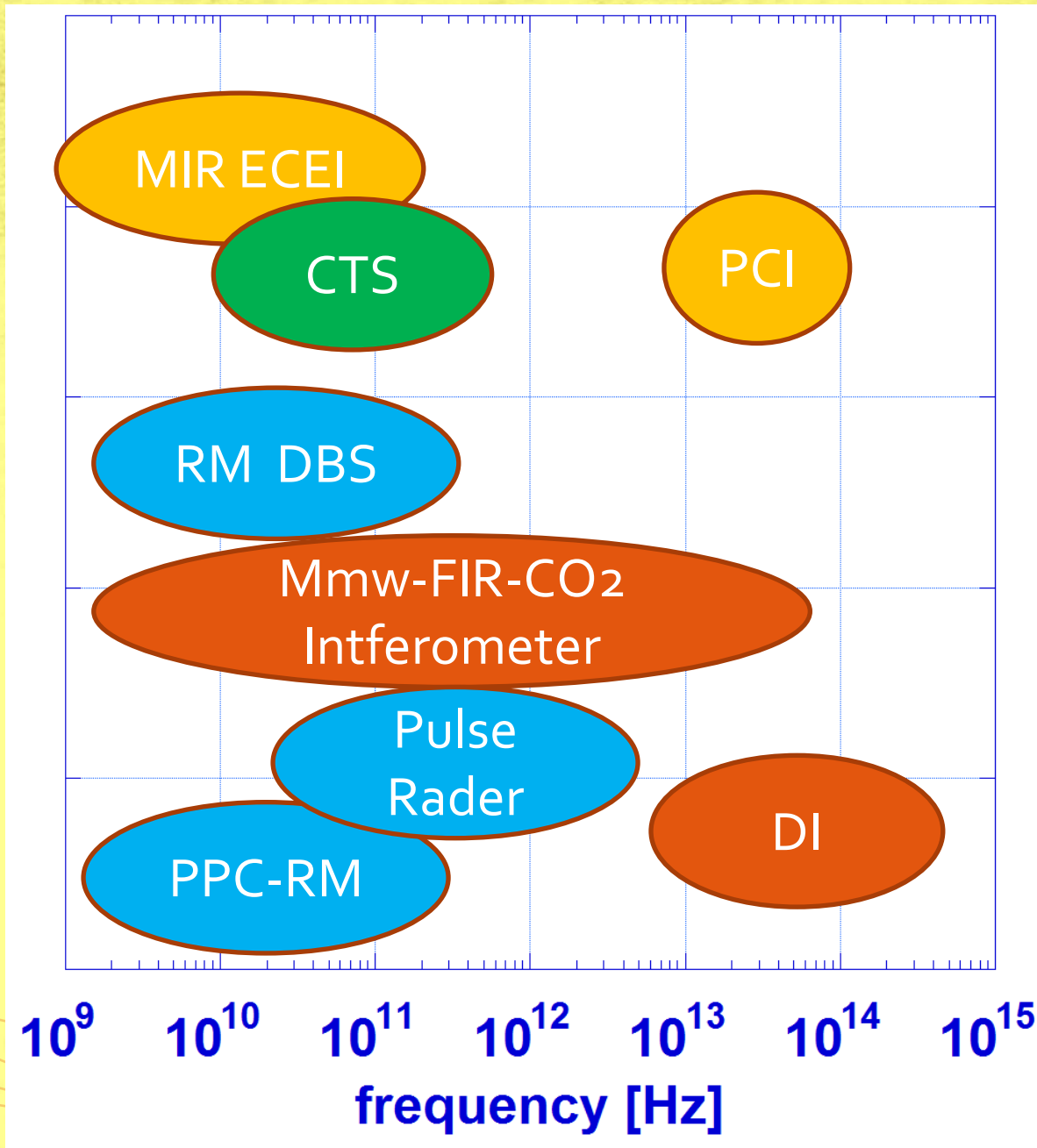


FIG. 3 (color). Measured CTS spectra in TEXTOR for a  $^3\text{He}$  fueled plasma (green, discharge no. 110421), a deuterium dominated plasma (red, discharge no. 109126) and a plasma with 40% hydrogen (blue, discharge no. 110416). The spacing between the ICS peaks corresponds to the ion cyclotron frequencies of  $^3\text{He}$ , D, and H, respectively.

- 元素によるIBW周波数の違いから、燃料比を推定する。



精緻



安定

# まとめ

- マイクロ波、ミリ波、テラヘルツ波という領域の電磁波を用いたプラズマ計測は、歴史が長い計測であり、技術は各種プラズマに最適化を施され、高度化・洗練されてきた。
- 今後の開発は2つの方向性になると思われる。一方は、先進的高精度化の方向性。もう一方は、プラズマ運転の、より直接的な制御ノブとしての計装化の方向性。



# 関連研究集会

- 「原型炉の運転制御に関するシンポジウム」
  - @3/12-13 : NIFS
- IRW12 (International Reflectometry Workshop)
  - @5/18-20 (締切: 3/27) : Julich (ドイツ)
- ITPA-DG (計測)
  - @5/19-22 : NIFS
- LAPD2015 (Laser Aided Plasma Diagnostics)
  - @9/27-10/1 (締切: 6/26) : 札幌

